

# Supplementary Materials for Hybrid Planning Using Learning and Model Checking for Autonomous Systems

## SUMMARY OF SUPPLEMENTARY MATERIALS

This document contains the hybrid planning algorithm and supplementary materials for the two case studies of learning-based hybrid planning. Structured as a series of questions and answers, this information can be used as further evidence of the studies' findings and for reproduction purposes.

The material starts with hybrid planning algorithm. Then for both case studies we provide the specific parameter values, planning specifications, and additional analyses on the dependencies between planning performances. In the end, we also provide visualizations of load traces in the first case study.

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## I. HYBRID PLANNING ALGORITHM

This section describes a general algorithm, executed in hybrid planners, that can be used in either existing condition-based approaches or our novel learning-based approach. This algorithm is an extension of the algorithm proposed by other researchers since our algorithm (a) can handle more than one reactive approach, (b) is not restricted to a specific combination of reactive and deliberative planning, and (c) not limited to the condition-based (i.e., constraint violations) approach. For the purposes of this paper, the algorithm serves as a standardized execution context of both HP approaches for the empirical study.

The goal of the hybrid planning algorithm (see Algorithm 1) is to determine a global plan of system adaptation (stored in variable  $\pi$ , protected from race conditions by a mutex  $\mu$ ) using a combination of some reactive planning approach ( $\rho_r \in \mathcal{F}$ ) and deliberative planning. A *plan* is a partial function  $P : S \rightarrow A$ ,

where  $S$  is a set of all possible states reachable from the current state, and  $A$  is a set of all possible adaptation tactics. A plan maps a state  $s \in S$  to a tactic  $a \in A$  to be executed in  $s$ . The input to the algorithm is a planning problem ( $\xi$ ) that contains the current state of the system ( $\xi.s_{curr}$ ).

**Algorithm 1** A general hybrid planning algorithm.

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1: global  $\pi \leftarrow null$                                 ▷ System's plan for execution
2: global  $\mu \leftarrow new\ Mutex$                       ▷ Mutex for  $\pi$ 
3: global  $\mathcal{T} \leftarrow new\ Thread$                   ▷ Deliberative thread
4: function HYBRIDPLANNING(Problem  $\xi$ , Planners  $\mathcal{F}$ , Planner  $\rho_d$ )
5:    $\mu.lock()$ 
6:   if  $\pi \neq null$  and  $\pi.has(\xi.s_{curr})$  then
7:      $\mu.unlock()$ 
8:     return                                     ▷ Replan only if needed
9:
10:    ▷ Pick an appropriate reactive planning approach
11:    Planner  $\rho_r = PICKREACTIVEPLANNING(\xi, \mathcal{F}, \rho_d)$ 
12:     $\pi \leftarrow \rho_r.PLAN(\xi)$                       ▷ Determine the reactive plan
13:     $\mu.unlock()$ 
14:
15:   if not  $\mathcal{T}.isRunning()$  then
16:      $\mathcal{T}.run [$                                 ▷ Deliberate in the background
17:        $\pi' \leftarrow \rho_d.PLAN(\xi)$ 
18:        $\mu.lock()$ 
19:        $\pi \leftarrow \pi'$ 
20:      $\mu.unlock() ]$ 

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To find a plan corresponding to the problem  $\xi$ , the HYBRIDPLANNING algorithm first refers to the existing plan (line 6). If a plan is present and matches the current state (i.e., contains  $\xi.s_{curr}$ ), then the algorithm does not change  $\pi$ . However, if the plan does not exist or  $\xi.s_{curr}$  is not in the plan, then the planner computes a suitable new plan (lines 10–20).

First, the algorithm needs to decide its instantaneous response (lines 10–13), which requires choosing an appropriate reactive planning approach  $\rho_r \in \mathcal{F}$ . This decision is made by the function PICKREACTIVEPLANNING, the role of which is to solve PLNSEL. This function can be implemented by checking predefined conditions on  $\xi$ , or by learning which reactive approach is (the most) suitable for a given planning problem.

Regardless of the above decision, deliberative planning (function DELIBERATIVEPLANNING) is started afterwards in

a separate thread or, generally, computation stream ( $\mathcal{T}$ , lines 16–18), in order to eventually arrive at a plan that is expected to yield higher utility than any of the reactive planning approaches. For a planning problem, deliberative planning is invoked once, allowing only one thread at a time. Once the computation of the deliberative plan is complete, the system’s plan is threadsafely updated to it (17–19). As discussed earlier, the structure of the plan enables a smooth transition (i.e., the global plan  $\pi$  is updated) from a reactive to a deliberative plan, thus resolving PLNCRD.

Algorithm 1 is implemented by a self-adaptive framework, which can use the global variables  $\pi$ ,  $\mu$ , and  $\mathcal{T}$  to configure HYBRIDPLANNING. For example, to find a reactive plan without stopping deliberative planning, the framework can lock  $\mu$ , set  $\pi$  to *null* and, if  $\mathcal{T}$  is still running, execute HYBRIDPLANNING. If needed, deliberative execution can be reset by stopping  $\mathcal{T}$ . Therefore, by setting the global variables appropriately, frameworks can apply the algorithm in various scenarios of self-repair and self-optimization.

A critical part of the hybrid planning logic is realized by the function PICKREACTIVEPLANNING, which solves PLNSEL in the above algorithm. In idealized conditions (when deliberative planning is always better than reactive planning, and PICKREACTIVEPLANNING picks the best reactive planning approach for a given  $\xi$ ), hybrid planning will never provide a lower expected utility compared to utilities provided by reactive and deliberative planning used alone. Intuitively, any reactive planner is no better than the choice of PICKREACTIVEPLANNING, and then it is dominated by a deliberative plan. The only way for deliberative planning to be better than hybrid planning is by avoiding inappropriate reactive planning invocation, which is also done by PICKREACTIVEPLANNING returning  $\rho_{wait}$ .

In practice, implementations of PICKREACTIVEPLANNING solve PLNSEL imperfectly, affecting the performance of HP. To solve PLNSEL, prior work used fixed conditions on the system’s state to decide whether to use reactive planning, evaluating a predicate  $P(\xi.s_{curr})$  defined by a domain expert. For instance, a reactive planner is used when the response time is above some threshold; otherwise, the system should wait. Learning-based approach is another potential implementation of PICKREACTIVEPLANNING.

## II. MATERIALS FOR THE CLOUD-BASED SYSTEM

This section contains the concrete parameters and specifications for the cloud-based load balancing system.

*Q: What Are the Exact Parameter Values for the Cloud-based System?*

In our experiments, the parameters values are the same as in our previous work where we evaluated condition-based hybrid planning [1]. We set the time-related parameters as follows: the systems evaluates the need for adaptation at each minute, and determines an action, if adaptation is needed. Some actions take time before their effect – any server boots up time is 2 minutes. The look-ahead horizon for deliberative planning (i.e.,  $\rho_{mdp}$ ) is chosen to be 5 minutes. This heuristic gives a long enough

horizon to go from one active server to three active servers, and one additional evaluation cycle to observe the resulting utility.

The system has three types of servers: A, B and C. Servers of type A are the most expensive, but have the highest capacity to handle requests. Servers of type C are the cheapest, but have the least request-handling capacity. The time to serve requests is normally distributed, depending on a server’s capacity. The costs and capacities are assigned according to Table I. The ratio between cost and capacity is constant, which is inspired by the cost model of AWS (<https://aws.amazon.com/ec2/pricing/on-demand>) where the system capacity improves in the same ratio as the increase in cost. In the experiments we have three dimmer levels and one server of each type.

Server type	Cost (units per minute)	Capacity (requests per minute)	
		With Optional Content	Without Optional Content
A	1.0	200	400
B	0.7	140	280
C	0.5	100	200

Table I  
COST/CAPACITY PARAMETERS FOR EACH SERVER TYPE.

In our experiments, the cost of a server can be covered by the revenue of handling  $1/10$  of its maximum capacity with optional content and the revenue of handling  $2/3$  of its maximum capacity without optional content. If the server cost per minute is  $C$ , capacity with optional content is  $c_O$  and without optional content is  $c_M$ , then the revenue for a server with optional content is  $R_O = \frac{10}{c_O}C$  and without optional content would be  $R_M = \frac{3/2}{c_M}C$ . For each request having response time above the threshold of 1 second, there is a penalty of -0.25 units. We assume the time for a server to serve a request is normally distributed with the mean as the server’s capacity and the variance as the maximum possible delay calculated using a variation of M/G/1/PS queueing model that supports different capacity servers operating in parallel.

When looking up the current state in a plan (Line 6 in the generalized HP algorithm, see Algorithm 1 in the main paper), the cloud-based system needs to deal with the possibility of not finding any matches; in such cases the plan fails and needs to be recomputed. As mentioned earlier, planning is done based on predicted request arrival rate; not the actual values. Since the prediction discretizes the values, it is very likely that the actual is not one of the discrete values. To account for this situation, we used a matching heuristic that needs to be applied to states in order not to discard plans in almost every transition. We use two criteria for states in a plan being matched to a given (current) state: (1) all state variables (except request arrival rate) have the same values; (2) the rate is within  $\min(0.5 * current\_rate, 100)$  of the current arrival rate. (We found that this criterion provides a reasonable balance between matching states and failing plans in our experiments.) If no state meeting both criteria is found in a plan, the matching fails. If several states meet both criteria, one that minimizes the difference between request arrival rates is picked.

We conducted the experiments on a Ubuntu 14.04 virtual machine having 8.5 GB RAM and 4 processors at 2.9 GHz. The state space for deterministic planning (i.e.,  $\rho_{det}$ ) varies between 25K to 100K, for deliberative planning (i.e.,  $\rho_{mdp}$ ) between 1.6 million and 2.8 million. The planning time for reactive planning  $\rho_{det}$  is considered negligible i.e., less than a second. The planning time for deliberative planning  $\rho_{mdp}$  varies between 35-45 seconds.

### III. MATERIALS FOR THE TEAM OF UAVS

This section contains the concrete parameters and specifications for the team of UAVs.

*Q: How to calculate the probabilities of the team being destroyed and detecting a target?*

The team configuration has an effect on the probability of being destroyed by a threat and the probability of detecting a target, which is important when deciding how to adapt. A threat can destroy the team only if both are in the same segment. However, a threat has range  $r_T$ , and its effectiveness is inversely proportional to the altitude of the team, denoted by  $\mathcal{A}$ . In addition, the formation of the team affects the probability of it being destroyed. The team can be in two different formations: loose ( $\phi = 0$ ), and tight ( $\phi = 1$ ). The latter reduces the probability of being destroyed by a factor of  $\psi$  [2]. When the team uses ( $E = 1$ ) electronic countermeasures (ECM), the probability of being destroyed is reduced by a factor of  $\alpha$ . Taking altitude, formation, and the use of ECM into account, the probability of the team being destroyed,  $d$  is given by (1).

$$d = \frac{\max(0, r_T - \mathcal{A})}{r_T} \left( (1 - \phi) + \frac{\phi}{\psi} \right) \left( (1 - E) + \frac{E}{\alpha} \right). \quad (1)$$

The probability of detecting a target with the downward-looking sensor, given that the target is in the segment being traversed by the UAVs, is inversely proportional to the altitude of the team [3]. Furthermore, flying in tight formation reduces the detection probability due to sensor occlusion or overlap, and the use of ECM also affects target detection, reducing the probability of detection by a factor of  $\beta$ . The probability  $g$  of detecting a target is given by (2).

$$g = \frac{\max(0, r_S - \mathcal{A})}{r_S} \left( (1 - \phi) + \frac{\phi}{\sigma} \right) \left( (1 - E) + \frac{E}{\beta} \right), \quad (2)$$

where  $r_S$  is the range of the sensor (i.e., at an altitude of  $r_S$  or higher, it is not possible to detect targets), and  $\sigma$  is the factor by which the detection probability is reduced due to flying in tight formation.

*Q: What Are the Exact Parameter Values for the Team of UAVs?*

We set the time-related parameters as follows: the systems evaluates the need for adaptation at each minute, and determines an action, if adaptation is needed. Some actions take time before their effect is observed – time to `IncAlt2/DecAlt2` and `IncAlt/DecAlt` is equal to 1 minute, which is also the duration that the team takes to cross a segment. For the team,

the horizon for reactive planning (i.e.,  $\rho_{mdps}$ ) and deliberative planning (i.e.,  $\rho_{mdpl}$ ) is 2 and 5, respectively.

We fixed the mission length for DARTSim at 40 segments. Total number of targets and threats are 20 and 10, respectively that are placed randomly depending on the random seed. Total number of altitude levels is 4, threat ( $r_T$ ) and target ( $r_S$ ) range is 3 and 4 respectively, the tight configuration reduces the probability of being destroyed (i.e.,  $\psi$ ) by factor 1.5. When using ECM the probability of being destroyed and target detection is reduced by a factor of 0.15, and 0.3, respectively. The threshold for the Manhattan distance is 1.0, which was decided after trying values 0.25, 0.5, 1.0, and 1.5. 1.0 provided the best performance for deliberative planning. The reward for surviving a segment is ( $\mu = 0.2$ ) and for detecting a target is ( $\lambda = 1$ ).

In hybrid planning modes, to identify an appropriate *Manhattan* distance to find the current state in an MDP policy, we evaluated the performance of deliberative mode with different distances as shown in Table II. We focused on the deliberative mode because, when using hybrid planning, Manhattan distance is used by deliberative planning. We finalized on Manhattan distance as 1.0 since deliberative mode detects maximum targets (i.e., 493) without being destroyed more compared to other distances.

Manhattan Distance	Targets	Destroyed
0.25	315	29
0.5	229	29
1.0	493	29
1.5	229	49

Table II  
PERFORMANCE OF DELIBERATIVE MODE ON 70 MISSIONS FOR DIFFERENT MANHATTAN DISTANCE.

When looking up the current state in a plan (i.e., Line 6 in Algorithm 1 in the main paper), DARTSim needs to deal with the possibility of not finding any matches; in such cases, the plan fails and needs to be recomputed. As mentioned earlier, planning is done based on probability for segments having a target and a threat; this probability is calculated by sampling the observations by target and threat sensors. However, when the team reaches a segment, the probability value can change due to additional data collected during the mission. To find the closest matching state corresponding to the current state, we use two criteria: (1) all state variables (except the target and threat probabilities in the current segment) have the same values, and (2) the *Manhattan* distance between the pairs of target and threat probabilities is less than a predefined threshold. If no state meeting both criteria is found in a plan, the matching fails. If several states meet both criteria, the one with the smallest distance is picked.

We conducted the experiments on a Ubuntu 14.04 virtual machine having 8.5 GB RAM and 4 processors at 2.9 GHz. The state space for the short-horizon MDP planning (i.e.,  $\rho_{mdps}$ ) varies between 75K to 250K, and for the long-horizon MDP planning  $\rho_{mdpl}$  between 3 million to 5 million. The planning time for reactive planning  $\rho_{mdps}$  is considered negligible i.e., less than a second. The planning time for deliberative planning  $\rho_{mdpl}$  varies between 40 and 60 seconds.

#### IV. MATERIALS FOR DATA ANALYSIS

This section contains auxiliary findings about HP from data analysis of both case studies.

##### *Q: What is the Dependency Between the Performance of Deliberative Planning and Hybrid Planning*

As discussed in the results of the main paper, as the performance of deliberative mode improves, the performance of the HP modes improves as well. This finding is further illustrated by Figure 1 for the cloud-based system and the UAV team; x-axis represents traces/missions sorted in ascending order in terms of aggregate utility (y-axis) accrued by deliberative mode. Intuitively, if a particular reactive approach (e.g.,  $\rho_{det}$  or  $\rho_{mdps}$ ) is not effective, the hybrid planner can choose another reactive approach (e.g.,  $\rho_{wait}$ ) in  $\mathcal{F}$ ; therefore, performance of HP is not tightly linked to a reactive approach.

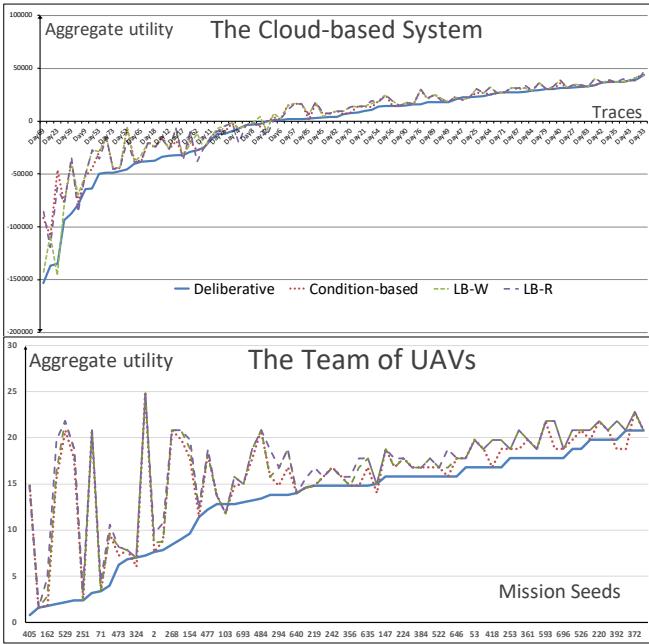


Figure 1. Performance of the hybrid planning modes improves with the performance of deliberative planning mode.

##### *Q: What is the Dependency Between the Performance of Reactive Planning and Hybrid Planning*

As stated in the results of the main paper, we discovered that the performance of reactive planning affects (with a positive correlation) the performance of hybrid planning. This dependency is moderated by the performance of the reactive planner, relative to other reactive planners. The better the reactive planner, the more influence it has on the hybrid planner.

We discovered this dependency by fitting a regression model to the utility of a hybrid planner  $U_{hp}$ , using the deliberative utility  $U_d$  and reactive utility  $U_r$  as independent variables. The fitting is done over all the traces/seeds in both case studies. Furthermore, to represent the moderating effect, these utilities were weighed with the following ratios:

- $U_d/U_{nw}$  for the deliberative utility, where  $U_{nw}$  is the utility of the NW-HP planner on that day. In this case,  $U_d$  is a proxy for the utility of the wait planner, which is invoked instead of reactive planner for  $U_{nw}$ . Thus, this ratio represents how much the reactive planning is better than waiting planning.

- $U_{nw}/U_d$  for the reactive utility, thus amplifying it on days when it is preferable to the wait planning, and reducing it on days when wait planning is preferable.

Thus, we arrive at the following regression model:

$$U_{hp} = a \cdot \frac{U_d}{U_{nw}} \cdot U_d + b \cdot \frac{U_{nw}}{U_d} \cdot U_r + c,$$

where  $a$ ,  $b$ , and  $c$  are regression coefficients determined by fitting the above function to the utility data. In the second case study we fit this exact function, and in the first case study we had to adjust the utility numbers such that none are negative or zero (otherwise the meaning of ratios is lost). Thus, we performed the following operation for the utility  $U$  of each type of planning:

$$U := U + \min(U) + 1.$$

In each fit model across both case studies the coefficients  $a$  and  $b$  were found positive. We tested the hypothesis that  $a$  and  $b$  are not zero with a t-test, yielding a highly significant result ( $p < 0.01$ ) that indeed the dependency exists.

## V. PRISM PLANNING SPECIFICATIONS

*Q: What are the Exact Planning Specifications for the Cloud-based System?*

Listing 1 and Listing 2 provide PRISM planning specifications for non-wait reactive (i.e., deterministic) and deliberative (i.e., MDP) planning (respectively) for a planning. These specifications have some constants (e.g., *MAX\_ARRIVALA\_CAPACITY*, *penalty*) that remain same for all the planning problems (i.e., specifications). However, there are variables (e.g., *ini\_servers\_A*, and *ini\_traffic\_A* that depend on the current state (i.e., initial state of the planning problem) of the system. These specifications also include modeling of the environment for this particular problem.

*Deterministic Planning Specification:* The listing below is the PRISM specification for deterministic planning  $\rho_{det}$ , which ignores uncertainty in the request arrival rate by assuming it to be constant at the current value. In the specification, inter-arrival time (the inverse of average request arrival rate) between two consecutive requests is used for environment modeling. For instance, in the statement “formula *stateValue* = 0.0163126” the request arrival rate will be 61 ( $= 1/0.0163126$ ) requests per minute.

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1 mdp
2
3 const double addServer_LATENCY = 120;
4 const int HORIZON = 5;
5 const double PERIOD = 60;
6 const int DIMMER_LEVELS = 3;
7 const int ini_dimmer = 1;
8 const int MAX_SERVERS_A = 1;
9 const int MAX_SERVERS_B = 1;
10 const int MAX_SERVERS_C = 1;
11 const int ini_servers_A = 1;
12 const int ini_servers_B = 0;
13 const int ini_servers_C = 0;
14 const int ini_addServerA_state = 0;
15 const int ini_addServerB_state = 0;
16 const int ini_addServerC_state = 0;
17 const double SERVERA_COST = 1;
18 const double SERVERB_COST = 0.7;
19 const double SERVERC_COST = 0.5;
20 const double MAX_ARRIVALA_CAPACITY = 200;
21 const double MAX_ARRIVALA_CAPACITY_LOW = 400;
22 const double MAX_ARRIVALB_CAPACITY = 140;
23 const double MAX_ARRIVALB_CAPACITY_LOW = 280;
24 const double MAX_ARRIVALC_CAPACITY = 100;
25 const double MAX_ARRIVALC_CAPACITY_LOW = 200;
26 const double penalty = -0.25;
27 const int ini_traffic_A = 4;
28 const int ini_traffic_B = 0;
29 const int ini_traffic_C = 0;
30 const double interArrivalScaleFactorForDecision = 1; // 1 has no effect
31
32 // The request arrival rate remains constant at the current value
33 formula stateValue = 0.0163126;
34
35
36 module clk
37   time : [0..HORIZON + 1] init 0;
38   readyToTick : bool init true;
39   [tick] readyToTick & time < HORIZON + 1 -> 1 : (time' = time + 1) &
39     (readyToTick'=false);
40   [tack] !readyToTick -> 1 : (readyToTick=true);
41 endmodule
42
43 label "final" = time = HORIZON + 1;
44 formula sys_go = readyToTick;
45
46 module controller
47   active_servers_A : [0..MAX_SERVERS_A] init ini_servers_A;
48   active_servers_B : [0..MAX_SERVERS_B] init ini_servers_B;
49   active_servers_C : [0..MAX_SERVERS_C] init ini_servers_C;

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dimmer : [1..DIMMER_LEVELS] init ini_dimmer;
traffic_A : [0..4] init ini_traffic_A;
traffic_B : [0..4] init ini_traffic_B;
traffic_C : [0..4] init ini_traffic_C;

[addServerA_complete] active_servers_A < MAX_SERVERS_A -> 1 :
  (active_servers_A' = active_servers_A + 1);
[addServerB_complete] active_servers_B < MAX_SERVERS_B -> 1 :
  (active_servers_B' = active_servers_B + 1);
[addServerC_complete] active_servers_C < MAX_SERVERS_C -> 1 :
  (active_servers_C' = active_servers_C + 1);

[removeServerA_start] active_servers_A > 0 -> 1 : (active_servers_A' =
  active_servers_A - 1);
[removeServerB_start] active_servers_B > 0 -> 1 : (active_servers_B' =
  active_servers_B - 1);
[removeServerC_start] active_servers_C > 0 -> 1 : (active_servers_C' =
  active_servers_C - 1);

[increaseDimmer_start] dimmer < DIMMER_LEVELS -> 1 : (dimmer' =
  dimmer + 1);
[decreaseDimmer_start] dimmer > 1 -> 1 : (dimmer' = dimmer - 1);

//A-B-C
//Possible values 0-25-50-75-100

// 100-0-0
[divert_100_0_0] active_servers_A > 0
  -> 1 : (traffic_A' = 4) & (traffic_B' = 0) & (traffic_C' = 0);
// 75-25-0
[divert_75_25_0] active_servers_A > 0 & active_servers_B > 0
  -> 1 : (traffic_A' = 3) & (traffic_B' = 1) & (traffic_C' = 0);
// 75-0-25
[divert_75_0_25] active_servers_A > 0 & active_servers_C > 0
  -> 1 : (traffic_A' = 3) & (traffic_B' = 0) & (traffic_C' = 1);
// 50-50-0
[divert_50_50_0] active_servers_A > 0 & active_servers_B > 0
  -> 1 : (traffic_A' = 2) & (traffic_B' = 2) & (traffic_C' = 0);
// 50-0-50
[divert_50_0_50] active_servers_A > 0 & active_servers_C > 0
  -> 1 : (traffic_A' = 2) & (traffic_B' = 0) & (traffic_C' = 2);
// 50-25-25
[divert_50_25_25] active_servers_A > 0 & active_servers_B > 0 &
  active_servers_C > 0
  -> 1 : (traffic_A' = 2) & (traffic_B' = 1) & (traffic_C' = 1);
// 25-75-0
[divert_25_75_0] active_servers_A > 0 & active_servers_B > 0
  -> 1 : (traffic_A' = 1) & (traffic_B' = 3) & (traffic_C' = 0);
// 25-0-75
[divert_25_0_75] active_servers_A > 0 & active_servers_C > 0
  -> 1 : (traffic_A' = 1) & (traffic_B' = 0) & (traffic_C' = 3);
// 25-50-25
[divert_25_50_25] active_servers_A > 0 & active_servers_B > 0 &
  active_servers_C > 0
  -> 1 : (traffic_A' = 1) & (traffic_B' = 2) & (traffic_C' = 1);
// 25-25-50
[divert_25_25_50] active_servers_A > 0 & active_servers_B > 0 &
  active_servers_C > 0
  -> 1 : (traffic_A' = 1) & (traffic_B' = 1) & (traffic_C' = 2);
// 0-100-0
[divert_0_100_0] active_servers_B > 0
  -> 1 : (traffic_A' = 0) & (traffic_B' = 4) & (traffic_C' = 0);
// 0-0-100
[divert_0_0_100] active_servers_C > 0
  -> 1 : (traffic_A' = 0) & (traffic_B' = 0) & (traffic_C' = 4);
// 0-75-25
[divert_0_75_25] active_servers_B > 0 & active_servers_C > 0
  -> 1 : (traffic_A' = 0) & (traffic_B' = 3) & (traffic_C' = 1);
// 0-25-75
[divert_0_25_75] active_servers_B > 0 & active_servers_C > 0
  -> 1 : (traffic_A' = 0) & (traffic_B' = 1) & (traffic_C' = 3);
// 0-50-50
[divert_0_50_50] active_servers_B > 0 & active_servers_C > 0
  -> 1 : (traffic_A' = 0) & (traffic_B' = 2) & (traffic_C' = 2);
endmodule

```



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262 [divert_25_25_50] sys_go & divert_traffic_applicable
263   -> 1 : (divert_go' = false);
264 // 0-100-0
265 [divert_0_100_0] sys_go & divert_traffic_applicable
266   -> 1 : (divert_go' = false);
267 // 0-0-100
268 [divert_0_0_100] sys_go & divert_traffic_applicable
269   -> 1 : (divert_go' = false);
270 // 0-75-25
271 [divert_0_75_25] sys_go & divert_traffic_applicable
272   -> 1 : (divert_go' = false);
273 // 0-25-75
274 [divert_0_25_75] sys_go & divert_traffic_applicable
275   -> 1 : (divert_go' = false);
276 // 0-50-50
277 [divert_0_50_50] sys_go & divert_traffic_applicable
278   -> 1 : (divert_go' = false);
279
280 [tick] !divert_go -> 1 : (divert_go' = true);
281 endmodule
282
283 module increaseDimmer
284   increaseDimmer_go : bool init true;
285   increaseDimmer_used : bool init false;
286
287 [increaseDimmer_start] sys_go & increaseDimmer_go
288   & increase_dimmer_applicable // applicability conditions
289   -> (increaseDimmer_go' = false) & (increaseDimmer_used' = true);
290
291 // tactic applicable but not used
292 [pass_inc_dimmer] sys_go & increaseDimmer_go // can go
293   -> (increaseDimmer_go' = false);
294
295 [tick] !increaseDimmer_go -> 1 : (increaseDimmer_go' = true) &
296   (increaseDimmer_used' = false);
297 endmodule
298
299 // tactic
300 module decreaseDimmer
301   decreaseDimmer_go : bool init true;
302   decreaseDimmer_used : bool init false;
303
304 [decreaseDimmer_start] sys_go & decreaseDimmer_go
305   & decrease_dimmer_applicable // applicability conditions
306   -> (decreaseDimmer_go' = false) & (decreaseDimmer_used' =
307     true);
308
309 // tactic applicable but not used
310 [pass_dec_dimmer] sys_go & decreaseDimmer_go // can go
311   -> (decreaseDimmer_go' = false);
312
313 [tick] !decreaseDimmer_go -> 1 : (decreaseDimmer_go' = true) &
314   (decreaseDimmer_used' = false);
315
316 //***** Queueing network with each server having queueing model of M/G/1/PS *****
317 formula dimmerFactor = (dimmer - 1) / (DIMMER_LEVELS - 1);
318 formula interarrivalMean = stateValue * interArrivalScaleFactorForDecision;
319
320 formula Pa = (traffic_A * 25)/100;
321 formula Pb = (traffic_B * 25)/100;
322 formula Pc = (traffic_C * 25)/100;
323
324 formula loaded_servers = (Pa != 0 ? 1 : 0) + (Pb != 0 ? 1 : 0) + (Pc != 0 ? 1 :
325   0);
326
327 formula service_rate_A = dimmerFactor *
328   (MAX_ARRIVALA_CAPACITY_LOW)
329   + (1 - dimmerFactor) * (MAX_ARRIVALA_CAPACITY);
330 formula service_rate_B = dimmerFactor *
331   (MAX_ARRIVALB_CAPACITY_LOW)
332   + (1 - dimmerFactor) * (MAX_ARRIVALB_CAPACITY);
333 formula service_rate_C = dimmerFactor *
334   (MAX_ARRIVALC_CAPACITY_LOW)
335   + (1 - dimmerFactor) * (MAX_ARRIVALC_CAPACITY);
336
337 formula rhoA = Pa/(service_rate_A*interarrivalMean);
338 formula rhoB = Pb/(service_rate_B*interarrivalMean);
339 formula rhoC = Pc/(service_rate_C*interarrivalMean);
340 formula overloaded = (rhoA >= 1 | rhoB >= 1 | rhoC >= 1);
341
342 formula rt_A = 1/(service_rate_A - (throughput*Pa));
343 formula rt_B = 1/(service_rate_B - (throughput*Pb));
344 formula rt_C = 1/(service_rate_C - (throughput*Pc));
345
346 // Response time to clients utility function
347 const double RT_THRESHOLD = 1.0;
348
349 formula expected_wait_time = (Pa*rt_A + Pb*rt_B + Pc*rt_C);
350 formula rt = (interarrivalMean = 0 ? 0 : (overloaded ? RT_THRESHOLD + 2
351   : expected_wait_time));
352
353 const double NORMAL_A_REVENUE = (SERVERA_COST /
354   MAX_ARRIVALA_CAPACITY) * 10;
355 const double DIMMER_A_REVENUE = (SERVERA_COST /
356   MAX_ARRIVALA_CAPACITY_LOW) * 3 / 2;
357 const double NORMAL_B_REVENUE = (SERVERB_COST /
358   MAX_ARRIVALB_CAPACITY) * 10;
359 const double DIMMER_B_REVENUE = (SERVERB_COST /
360   MAX_ARRIVALB_CAPACITY_LOW) * 3 / 2;
361 const double NORMAL_C_REVENUE = (SERVERC_COST /
362   MAX_ARRIVALC_CAPACITY) * 10;
363 const double DIMMER_C_REVENUE = (SERVERC_COST /
364   MAX_ARRIVALC_CAPACITY_LOW) * 3 / 2;
365
366 const double DIMMER_REVENUE = DIMMER_A_REVENUE +
367   DIMMER_B_REVENUE + DIMMER_C_REVENUE;
368 const double NORMAL_REVENUE = NORMAL_A_REVENUE +
369   NORMAL_B_REVENUE + NORMAL_C_REVENUE;
370
371 formula serverA_cost = ((addServerA_state > 0 ? 1 : 0) +
372   active_servers_A) * SERVERA_COST;
373 formula serverB_cost = ((addServerB_state > 0 ? 1 : 0) +
374   active_servers_B) * SERVERB_COST;
375 formula serverC_cost = ((addServerC_state > 0 ? 1 : 0) +
376   active_servers_C) * SERVERC_COST;
377 formula cost = serverA_cost + serverB_cost + serverC_cost;
378 formula throughput = 1/interarrivalMean;
379
380 formula basicUtilityA = throughput * Pa * (dimmerFactor *
381   DIMMER_A_REVENUE + (1 - dimmerFactor) *
382   NORMAL_A_REVENUE);
383 formula basicUtilityB = throughput * Pb * (dimmerFactor *
384   DIMMER_B_REVENUE + (1 - dimmerFactor) *
385   NORMAL_B_REVENUE);
386 formula basicUtilityC = throughput * Pc * (dimmerFactor *
387   DIMMER_C_REVENUE + (1 - dimmerFactor) *
388   NORMAL_C_REVENUE);
389
390 formula basicUtility = basicUtilityA + basicUtilityB + basicUtilityC;
391 formula active_servers = active_servers_A + active_servers_B +
392   active_servers_C;
393 formula poweredServers = (addServerA_state > 0 ? 1 : 0) +
394   (addServerB_state > 0 ? 1 : 0) + (addServerC_state > 0 ? 1 : 0) +
395   active_servers;
396 formula MAX_SERVERS = MAX_SERVERS_A + MAX_SERVERS_B +
397   MAX_SERVERS_C;
398
399 formula MAX_SERVER_COST = MAX_SERVERS_A * SERVERA_COST +
400   MAX_SERVERS_B * SERVERB_COST +
401   MAX_SERVERS_C * SERVERC_COST;
402
403 formula netPenalty = stateValue > 0 ? penalty / stateValue : 0;
404
405 formula uTotal = (overloaded & (poweredServers < MAX_SERVERS |
406   dimmer < DIMMER_LEVELS | active_servers != loaded_servers)) ?
407   -(1000) // avoid unstable solutions
408   (((rt > RT_THRESHOLD | rt <= 0) ? netPenalty :
409     basicUtility) - cost);
410
411 rewards "util"
412   // 10000000.0 is added to avoid a negative value during calculation;
413   // negative utility is not supported by PRISM.
414   [tack] true : 10000000.0 + (PERIOD)*(uTotal);
415 endrewards

```

Listing 1. PRISM specification for deterministic planning

*MDP Planning Specification:* In contrast to deterministic planning (i.e.,  $\rho_{det}$ ), MDP planning (i.e.,  $\rho_{mdp}$ ) considers predicted (uncertain) values of request arrival rate. For  $\rho_{mdp}$ , we create an environment model using future values of inter-arrival time (the inverse of average request arrival rate) between two consecutive requests. When deliberative planning (i.e.,  $\rho_{mdp}$ ) is triggered, a time-series predictor feeds predicted values as an environment model formulating an MDP, mapping each possible interarrival rate to an outcome of a probabilistic action taken by the environment. The specification has environment modeled as an MDP for the planning horizon (i.e., 5) for MDP planning.

```

1  mdp
2
3  const double addServer_LATENCY = 120;
4  const int HORIZON = 5;
5  const double PERIOD = 60;
6  const int DIMMER_LEVELS = 3;
7  const int ini_dimmer = 1;
8  const int MAX_SERVERS_A = 1;
9  const int MAX_SERVERS_B = 1;
10 const int MAX_SERVERS_C = 1;
11 const int ini_servers_A = 1;
12 const int ini_servers_B = 0;
13 const int ini_servers_C = 0;
14 const int ini_addServerA_state = 0;
15 const int ini_addServerB_state = 0;
16 const int ini_addServerC_state = 0;
17 const double SERVERA_COST = 1;
18 const double SERVERB_COST = 0.7;
19 const double SERVERC_COST = 0.5;
20 const double MAX_ARRIVALA_CAPACITY = 200;
21 const double MAX_ARRIVALA_CAPACITY_LOW = 400;
22 const double MAX_ARRIVALB_CAPACITY = 140;
23 const double MAX_ARRIVALB_CAPACITY_LOW = 280;
24 const double MAX_ARRIVALC_CAPACITY = 100;
25 const double MAX_ARRIVALC_CAPACITY_LOW = 200;
26 const double penalty = -0.25;
27 const int ini_traffic_A = 4;
28 const int ini_traffic_B = 0;
29 const int ini_traffic_C = 0;
30 const double interArrivalScaleFactorForDecision = 1; // 1 has no effect
31
32 // Model of the environment as an MDP. Values from the time series
   predictor
33 // have been used to get the interarrival time.
34 module environment
35 s : [0..201] init 0;
36 [tick] s = 0 ->
37   0.185 : (s' = 1)
38   + 0.63 : (s' = 2)
39   + 0.185 : (s' = 3);
40 [tick] s = 3 ->
41   0.185 : (s' = 4)
42   + 0.63 : (s' = 5)
43   + 0.185 : (s' = 6);
44 [tick] s = 6 ->
45   0.185 : (s' = 7)
46   + 0.63 : (s' = 8)
47   + 0.185 : (s' = 9);
48 [tick] s = 9 ->
49   0.185 : (s' = 10)
50   + 0.63 : (s' = 11)
51   + 0.185 : (s' = 12);
52 [tick] s = 12 ->
53   1 : (s' = 13);
54 [tick] s = 11 ->
55   1 : (s' = 14);
56 [tick] s = 10 ->
57   1 : (s' = 15);
58 [tick] s = 8 ->
59   0.185 : (s' = 16)
60   + 0.63 : (s' = 17)
61   + 0.185 : (s' = 18);
62 [tick] s = 18 ->
63   1 : (s' = 19);
64 [tick] s = 17 ->
65   1 : (s' = 20);
66 [tick] s = 16 ->
67   1 : (s' = 21);
68 [tick] s = 7 ->
69   0.185 : (s' = 22)
70   + 0.63 : (s' = 23)
71   + 0.185 : (s' = 24);
72 [tick] s = 24 ->
73   1 : (s' = 25);
74 [tick] s = 23 ->
75   1 : (s' = 26);
76 [tick] s = 22 ->
77   1 : (s' = 27);
78 [tick] s = 5 ->
79   0.185 : (s' = 28)
80   + 0.63 : (s' = 29)
81   + 0.185 : (s' = 30);
82 [tick] s = 30 ->
83   0.185 : (s' = 31)
84   + 0.63 : (s' = 32)
85   + 0.185 : (s' = 33);
86 [tick] s = 33 ->
87   1 : (s' = 34);
88 [tick] s = 32 ->
89   1 : (s' = 35);
90 [tick] s = 31 ->
91   1 : (s' = 36);
92 [tick] s = 29 ->
93   0.185 : (s' = 37)
94   + 0.63 : (s' = 38)
95   + 0.185 : (s' = 39);
96 [tick] s = 39 ->
97   1 : (s' = 40);
98 [tick] s = 38 ->
99   1 : (s' = 41);
100 [tick] s = 37 ->
101   1 : (s' = 42);
102 [tick] s = 28 ->
103   0.185 : (s' = 43)
104   + 0.63 : (s' = 44)
105   + 0.185 : (s' = 45);
106 [tick] s = 45 ->
107   1 : (s' = 46);
108 [tick] s = 44 ->
109   1 : (s' = 47);
110 [tick] s = 43 ->
111   1 : (s' = 48);
112 [tick] s = 4 ->
113   0.185 : (s' = 49)
114   + 0.63 : (s' = 50)
115   + 0.185 : (s' = 51);
116 [tick] s = 51 ->
117   0.185 : (s' = 52)
118   + 0.63 : (s' = 53)
119   + 0.185 : (s' = 54);
120 [tick] s = 54 ->
121   1 : (s' = 55);
122 [tick] s = 53 ->
123   1 : (s' = 56);
124 [tick] s = 52 ->
125   1 : (s' = 57);
126 [tick] s = 50 ->
127   0.185 : (s' = 58)
128   + 0.63 : (s' = 59)
129   + 0.185 : (s' = 60);
130 [tick] s = 60 ->
131   1 : (s' = 61);
132 [tick] s = 59 ->
133   1 : (s' = 62);
134 [tick] s = 58 ->
135   1 : (s' = 63);
136 [tick] s = 49 ->
137   0.185 : (s' = 64)
138   + 0.63 : (s' = 65)
139   + 0.185 : (s' = 66);
140 [tick] s = 66 ->
141   1 : (s' = 67);
142 [tick] s = 65 ->
143   1 : (s' = 68);
144 [tick] s = 64 ->
145   1 : (s' = 69);
146 [tick] s = 2 ->
147   0.185 : (s' = 70)
148   + 0.63 : (s' = 71)

```

```

149      + 0.185 : (s' = 72);
150      [tick] s = 72 ->
151          0.185 : (s' = 73)
152          + 0.63 : (s' = 74)
153          + 0.185 : (s' = 75);
154      [tick] s = 75 ->
155          0.185 : (s' = 76)
156          + 0.63 : (s' = 77)
157          + 0.185 : (s' = 78);
158      [tick] s = 78 ->
159          1 : (s' = 79);
160      [tick] s = 77 ->
161          1 : (s' = 80);
162      [tick] s = 76 ->
163          1 : (s' = 81);
164      [tick] s = 74 ->
165          0.185 : (s' = 82)
166          + 0.63 : (s' = 83)
167          + 0.185 : (s' = 84);
168      [tick] s = 84 ->
169          1 : (s' = 85);
170      [tick] s = 83 ->
171          1 : (s' = 86);
172      [tick] s = 82 ->
173          1 : (s' = 87);
174      [tick] s = 73 ->
175          0.185 : (s' = 88)
176          + 0.63 : (s' = 89)
177          + 0.185 : (s' = 90);
178      [tick] s = 90 ->
179          1 : (s' = 91);
180      [tick] s = 89 ->
181          1 : (s' = 92);
182      [tick] s = 88 ->
183          1 : (s' = 93);
184      [tick] s = 71 ->
185          0.185 : (s' = 94)
186          + 0.63 : (s' = 95)
187          + 0.185 : (s' = 96);
188      [tick] s = 96 ->
189          0.185 : (s' = 97)
190          + 0.63 : (s' = 98)
191          + 0.185 : (s' = 99);
192      [tick] s = 99 ->
193          1 : (s' = 100);
194      [tick] s = 98 ->
195          1 : (s' = 101);
196      [tick] s = 97 ->
197          1 : (s' = 102);
198      [tick] s = 95 ->
199          0.185 : (s' = 103)
200          + 0.63 : (s' = 104)
201          + 0.185 : (s' = 105);
202      [tick] s = 105 ->
203          1 : (s' = 106);
204      [tick] s = 104 ->
205          1 : (s' = 107);
206      [tick] s = 103 ->
207          1 : (s' = 108);
208      [tick] s = 94 ->
209          0.185 : (s' = 109)
210          + 0.63 : (s' = 110)
211          + 0.185 : (s' = 111);
212      [tick] s = 111 ->
213          1 : (s' = 112);
214      [tick] s = 110 ->
215          1 : (s' = 113);
216      [tick] s = 109 ->
217          1 : (s' = 114);
218      [tick] s = 70 ->
219          0.185 : (s' = 115)
220          + 0.63 : (s' = 116)
221          + 0.185 : (s' = 117);
222      [tick] s = 117 ->
223          0.185 : (s' = 118)
224          + 0.63 : (s' = 119)
225          + 0.185 : (s' = 120);
226      [tick] s = 120 ->
227          1 : (s' = 121);
228      [tick] s = 119 ->
229          1 : (s' = 122);
230      [tick] s = 118 ->
231          1 : (s' = 123);

232      [tick] s = 116 ->
233          0.185 : (s' = 124)
234          + 0.63 : (s' = 125)
235          + 0.185 : (s' = 126);
236      [tick] s = 126 ->
237          1 : (s' = 127);
238      [tick] s = 125 ->
239          1 : (s' = 128);
240      [tick] s = 124 ->
241          1 : (s' = 129);
242      [tick] s = 115 ->
243          0.185 : (s' = 130)
244          + 0.63 : (s' = 131)
245          + 0.185 : (s' = 132);
246      [tick] s = 132 ->
247          1 : (s' = 133);
248      [tick] s = 131 ->
249          1 : (s' = 134);
250      [tick] s = 130 ->
251          1 : (s' = 135);
252      [tick] s = 1 ->
253          0.185 : (s' = 136)
254          + 0.63 : (s' = 137)
255          + 0.185 : (s' = 138);
256      [tick] s = 138 ->
257          0.185 : (s' = 139)
258          + 0.63 : (s' = 140)
259          + 0.185 : (s' = 141);
260      [tick] s = 141 ->
261          0.185 : (s' = 142)
262          + 0.63 : (s' = 143)
263          + 0.185 : (s' = 144);
264      [tick] s = 144 ->
265          1 : (s' = 145);
266      [tick] s = 143 ->
267          1 : (s' = 146);
268      [tick] s = 142 ->
269          1 : (s' = 147);
270      [tick] s = 140 ->
271          0.185 : (s' = 148)
272          + 0.63 : (s' = 149)
273          + 0.185 : (s' = 150);
274      [tick] s = 150 ->
275          1 : (s' = 151);
276      [tick] s = 149 ->
277          1 : (s' = 152);
278      [tick] s = 148 ->
279          1 : (s' = 153);
280      [tick] s = 139 ->
281          0.185 : (s' = 154)
282          + 0.63 : (s' = 155)
283          + 0.185 : (s' = 156);
284      [tick] s = 156 ->
285          1 : (s' = 157);
286      [tick] s = 155 ->
287          1 : (s' = 158);
288      [tick] s = 154 ->
289          1 : (s' = 159);
290      [tick] s = 137 ->
291          0.185 : (s' = 160)
292          + 0.63 : (s' = 161)
293          + 0.185 : (s' = 162);
294      [tick] s = 162 ->
295          0.185 : (s' = 163)
296          + 0.63 : (s' = 164)
297          + 0.185 : (s' = 165);
298      [tick] s = 165 ->
299          1 : (s' = 166);
300      [tick] s = 164 ->
301          1 : (s' = 167);
302      [tick] s = 163 ->
303          1 : (s' = 168);
304      [tick] s = 161 ->
305          0.185 : (s' = 169)
306          + 0.63 : (s' = 170)
307          + 0.185 : (s' = 171);
308      [tick] s = 171 ->
309          1 : (s' = 172);
310      [tick] s = 170 ->
311          1 : (s' = 173);
312      [tick] s = 169 ->
313          1 : (s' = 174);
314      [tick] s = 160 ->

```

```

315    0.185 : (s' = 175)
316    + 0.63 : (s' = 176)
317    + 0.185 : (s' = 177);
318 [tick] s = 177 ->
319   1 : (s' = 178);
320 [tick] s = 176 ->
321   1 : (s' = 179);
322 [tick] s = 175 ->
323   1 : (s' = 180);
324 [tick] s = 136 ->
325   0.185 : (s' = 181)
326   + 0.63 : (s' = 182)
327   + 0.185 : (s' = 183);
328 [tick] s = 183 ->
329   0.185 : (s' = 184)
330   + 0.63 : (s' = 185)
331   + 0.185 : (s' = 186);
332 [tick] s = 186 ->
333   1 : (s' = 187);
334 [tick] s = 185 ->
335   1 : (s' = 188);
336 [tick] s = 184 ->
337   1 : (s' = 189);
338 [tick] s = 182 ->
339   0.185 : (s' = 190)
340   + 0.63 : (s' = 191)
341   + 0.185 : (s' = 192);
342 [tick] s = 192 ->
343   1 : (s' = 193);
344 [tick] s = 191 ->
345   1 : (s' = 194);
346 [tick] s = 190 ->
347   1 : (s' = 195);
348 [tick] s = 181 ->
349   0.185 : (s' = 196)
350   + 0.63 : (s' = 197)
351   + 0.185 : (s' = 198);
352 [tick] s = 198 ->
353   1 : (s' = 199);
354 [tick] s = 197 ->
355   1 : (s' = 200);
356 [tick] s = 196 ->
357   1 : (s' = 201);
358 [tick] (s = 13 | s = 14 | s = 15 | s = 19 | s = 20 | s = 21 | s = 25 | s = 26 | s =
27 | s = 34 | s = 35 | s = 36 | s = 40 | s = 41 | s = 42 | s = 46 | s = 47 |
s = 48 | s = 55 | s = 56 | s = 57 | s = 61 | s = 62 | s = 63 | s = 67 | s =
68 | s = 69 | s = 79 | s = 80 | s = 81 | s = 85 | s = 86 | s = 87 | s = 91 |
s = 92 | s = 93 | s = 100 | s = 101 | s = 102 | s = 106 | s = 107 | s =
108 | s = 112 | s = 113 | s = 114 | s = 121 | s = 122 | s = 123 | s = 127 |
| s = 128 | s = 129 | s = 133 | s = 134 | s = 135 | s = 145 | s = 146 | s =
147 | s = 151 | s = 152 | s = 153 | s = 157 | s = 158 | s = 159 | s = 166 |
| s = 167 | s = 168 | s = 172 | s = 173 | s = 174 | s = 178 | s = 179 | s =
180 | s = 187 | s = 188 | s = 189 | s = 193 | s = 194 | s = 195 | s = 199 |
| s = 200 | s = 201) -> 1 : true;
359 endmodule
360 formula stateValue = (s = 0 ? 0.0176932 : 0) +
361   (s = 3 ? 0.0214149 : 0) +
362   (s = 6 ? 0.0270787 : 0) +
363   (s = 9 ? 0.0333291 : 0) +
364   (s = 12 ? 0.0407615 : 0) +
365   (s = 13 ? 0.0387364 : 0) +
366   (s = 11 ? 0.0321959 : 0) +
367   (s = 14 ? 0.0311986 : 0) +
368   (s = 10 ? 0.0236303 : 0) +
369   (s = 15 ? 0.0236609 : 0) +
370   (s = 8 ? 0.0266955 : 0) +
371   (s = 18 ? 0.0328878 : 0) +
372   (s = 19 ? 0.0318075 : 0) +
373   (s = 17 ? 0.0263583 : 0) +
374   (s = 20 ? 0.0260615 : 0) +
375   (s = 16 ? 0.0198287 : 0) +
376   (s = 21 ? 0.0203155 : 0) +
377   (s = 7 ? 0.0200618 : 0) +
378   (s = 24 ? 0.0256958 : 0) +
379   (s = 25 ? 0.0254786 : 0) +
380   (s = 23 ? 0.0205206 : 0) +
381   (s = 26 ? 0.0209244 : 0) +
382   (s = 22 ? 0.0153454 : 0) +
383   (s = 27 ? 0.0163702 : 0) +
384   (s = 5 ? 0.0217113 : 0) +
385   (s = 30 ? 0.0273884 : 0) +
386   (s = 33 ? 0.0336873 : 0) +
387   (s = 34 ? 0.0325111 : 0) +
388   (s = 32 ? 0.026968 : 0) +
389   (s = 35 ? 0.0265981 : 0) +
390   (s = 31 ? 0.0202487 : 0) +
391   (s = 36 ? 0.0206851 : 0) +
392   (s = 29 ? 0.0219722 : 0) +
393   (s = 39 ? 0.0276628 : 0) +
394   (s = 40 ? 0.0272095 : 0) +
395   (s = 38 ? 0.0222018 : 0) +
396   (s = 41 ? 0.0224038 : 0) +
397   (s = 37 ? 0.0167408 : 0) +
398   (s = 42 ? 0.0175982 : 0) +
399   (s = 28 ? 0.0165561 : 0) +
400   (s = 45 ? 0.0223769 : 0) +
401   (s = 46 ? 0.0225579 : 0) +
402   (s = 44 ? 0.0174356 : 0) +
403   (s = 47 ? 0.0182096 : 0) +
404   (s = 43 ? 0.0124943 : 0) +
405   (s = 48 ? 0.0138613 : 0) +
406   (s = 4 ? 0.016344 : 0) +
407   (s = 51 ? 0.0221892 : 0) +
408   (s = 54 ? 0.0278924 : 0) +
409   (s = 55 ? 0.0274116 : 0) +
410   (s = 53 ? 0.0223928 : 0) +
411   (s = 56 ? 0.0225719 : 0) +
412   (s = 52 ? 0.0168932 : 0) +
413   (s = 57 ? 0.0177322 : 0) +
414   (s = 50 ? 0.017249 : 0) +
415   (s = 60 ? 0.0230006 : 0) +
416   (s = 61 ? 0.0231068 : 0) +
417   (s = 59 ? 0.0180454 : 0) +
418   (s = 62 ? 0.0187462 : 0) +
419   (s = 58 ? 0.0130901 : 0) +
420   (s = 63 ? 0.0143856 : 0) +
421   (s = 49 ? 0.0123087 : 0) +
422   (s = 66 ? 0.0189053 : 0) +
423   (s = 67 ? 0.0195029 : 0) +
424   (s = 65 ? 0.0136979 : 0) +
425   (s = 68 ? 0.0149204 : 0) +
426   (s = 64 ? 0.00849053 : 0) +
427   (s = 69 ? 0.0103379 : 0) +
428   (s = 2 ? 0.0163126 : 0) +
429   (s = 72 ? 0.0221616 : 0) +
430   (s = 75 ? 0.0278631 : 0) +
431   (s = 78 ? 0.0342389 : 0) +
432   (s = 79 ? 0.0329965 : 0) +
433   (s = 77 ? 0.0273858 : 0) +
434   (s = 80 ? 0.0269657 : 0) +
435   (s = 76 ? 0.0205326 : 0) +
436   (s = 81 ? 0.0209349 : 0) +
437   (s = 74 ? 0.0223684 : 0) +
438   (s = 84 ? 0.0280829 : 0) +
439   (s = 85 ? 0.0275792 : 0) +
440   (s = 83 ? 0.0225505 : 0) +
441   (s = 86 ? 0.0227107 : 0) +
442   (s = 82 ? 0.0170181 : 0) +
443   (s = 87 ? 0.0178422 : 0) +
444   (s = 73 ? 0.0168738 : 0) +
445   (s = 90 ? 0.0226608 : 0) +
446   (s = 91 ? 0.0228078 : 0) +
447   (s = 89 ? 0.0177152 : 0) +
448   (s = 92 ? 0.0184556 : 0) +
449   (s = 88 ? 0.0127696 : 0) +
450   (s = 93 ? 0.0141035 : 0) +
451   (s = 71 ? 0.0172213 : 0) +
452   (s = 96 ? 0.0229754 : 0) +
453   (s = 99 ? 0.0287337 : 0) +
454   (s = 100 ? 0.0281519 : 0) +
455   (s = 98 ? 0.0230846 : 0) +
456   (s = 101 ? 0.0231807 : 0) +
457   (s = 97 ? 0.0174355 : 0) +
458   (s = 102 ? 0.0182095 : 0) +
459   (s = 95 ? 0.018021 : 0) +
460   (s = 105 ? 0.0237147 : 0) +
461   (s = 106 ? 0.0237352 : 0) +
462   (s = 104 ? 0.0187248 : 0) +
463   (s = 107 ? 0.019344 : 0) +
464   (s = 103 ? 0.0137348 : 0) +
465   (s = 108 ? 0.0149529 : 0) +
466   (s = 94 ? 0.0130667 : 0) +
467   (s = 111 ? 0.0194823 : 0) +
468   (s = 112 ? 0.0200107 : 0) +
469   (s = 110 ? 0.0143649 : 0) +
470   (s = 113 ? 0.0155074 : 0) +

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471      (s = 109 ? 0.00924753 : 0) +
472      (s = 114 ? 0.0110041 : 0) +
473      (s = 70 ? 0.0122811 : 0) +
474      (s = 117 ? 0.0188846 : 0) +
475      (s = 120 ? 0.0245369 : 0) +
476      (s = 121 ? 0.0244587 : 0) +
477      (s = 119 ? 0.0194847 : 0) +
478      (s = 122 ? 0.0200128 : 0) +
479      (s = 118 ? 0.0144325 : 0) +
480      (s = 123 ? 0.0155668 : 0) +
481      (s = 116 ? 0.0136736 : 0) +
482      (s = 126 ? 0.0199571 : 0) +
483      (s = 127 ? 0.0204285 : 0) +
484      (s = 125 ? 0.014899 : 0) +
485      (s = 128 ? 0.0159774 : 0) +
486      (s = 124 ? 0.009841 : 0) +
487      (s = 129 ? 0.0115263 : 0) +
488      (s = 115 ? 0.00846263 : 0) +
489      (s = 132 ? 0.0162147 : 0) +
490      (s = 133 ? 0.0171352 : 0) +
491      (s = 131 ? 0.0103134 : 0) +
492      (s = 134 ? 0.011942 : 0) +
493      (s = 130 ? 0.00441199 : 0) +
494      (s = 135 ? 0.0067488 : 0) +
495      (s = 1 ? 0.0112104 : 0) +
496      (s = 138 ? 0.0180987 : 0) +
497      (s = 141 ? 0.0237876 : 0) +
498      (s = 144 ? 0.0296178 : 0) +
499      (s = 145 ? 0.0289299 : 0) +
500      (s = 143 ? 0.0237994 : 0) +
501      (s = 146 ? 0.0238097 : 0) +
502      (s = 142 ? 0.0179809 : 0) +
503      (s = 147 ? 0.0186894 : 0) +
504      (s = 140 ? 0.0187931 : 0) +
505      (s = 150 ? 0.0244486 : 0) +
506      (s = 151 ? 0.024381 : 0) +
507      (s = 149 ? 0.0194042 : 0) +
508      (s = 152 ? 0.0199419 : 0) +
509      (s = 148 ? 0.0143597 : 0) +
510      (s = 153 ? 0.0155028 : 0) +
511      (s = 139 ? 0.0137985 : 0) +
512      (s = 156 ? 0.0200562 : 0) +
513      (s = 157 ? 0.0205157 : 0) +
514      (s = 155 ? 0.015009 : 0) +
515      (s = 158 ? 0.0160741 : 0) +
516      (s = 154 ? 0.0099617 : 0) +
517      (s = 159 ? 0.0116325 : 0) +
518      (s = 137 ? 0.0127314 : 0) +
519      (s = 162 ? 0.0192249 : 0) +
520      (s = 165 ? 0.0248675 : 0) +
521      (s = 166 ? 0.0247496 : 0) +
522      (s = 164 ? 0.0197842 : 0) +
523      (s = 167 ? 0.0202763 : 0) +
524      (s = 163 ? 0.0147008 : 0) +
525      (s = 168 ? 0.015803 : 0) +
526      (s = 161 ? 0.0140698 : 0) +
527      (s = 171 ? 0.0202733 : 0) +
528      (s = 172 ? 0.0207067 : 0) +
529      (s = 170 ? 0.0152477 : 0) +
530      (s = 173 ? 0.0162842 : 0) +
531      (s = 169 ? 0.0102221 : 0) +
532      (s = 174 ? 0.0118617 : 0) +
533      (s = 160 ? 0.00891477 : 0) +
534      (s = 177 ? 0.016513 : 0) +
535      (s = 178 ? 0.0173977 : 0) +
536      (s = 176 ? 0.0107112 : 0) +
537      (s = 179 ? 0.0122921 : 0) +
538      (s = 175 ? 0.00490948 : 0) +
539      (s = 180 ? 0.00718659 : 0) +
540      (s = 136 ? 0.00736404 : 0) +
541      (s = 183 ? 0.0155067 : 0) +
542      (s = 186 ? 0.0214635 : 0) +
543      (s = 187 ? 0.0217541 : 0) +
544      (s = 185 ? 0.0165121 : 0) +
545      (s = 188 ? 0.0173969 : 0) +
546      (s = 184 ? 0.0115608 : 0) +
547      (s = 189 ? 0.0130397 : 0) +
548      (s = 182 ? 0.0093466 : 0) +
549      (s = 192 ? 0.0168019 : 0) +
550      (s = 193 ? 0.0176519 : 0) +
551      (s = 191 ? 0.0110913 : 0) +
552      (s = 194 ? 0.0126265 : 0) +
553      (s = 190 ? 0.0053806 : 0) +
554      (s = 195 ? 0.00760117 : 0) +
555      (s = 181 ? 0.0031865 : 0) +
556      (s = 198 ? 0.0129875 : 0) +
557      (s = 199 ? 0.0142952 : 0) +
558      (s = 197 ? 0.00567036 : 0) +
559      (s = 200 ? 0.00785617 : 0) +
560      (s = 196 ? 0 : 0) +
561      (s = 201 ? 0.00286625 : 0);
562
563
564 module clk
565   time : [0..HORIZON + 1] init 0;
566   readyToTick : bool init true;
567   [tick] readyToTick & time < HORIZON + 1 -> 1 : (time' = time + 1) &
568     (readyToTick'=false);
569   [task] !readyToTick -> 1 : (readyToTick'=true);
570 endmodule
571
572 label "final" = time = HORIZON + 1;
573 formula sys_go = readyToTick;
574
575 module controller
576   active_servers_A : [0..MAX_SERVERS_A] init ini_servers_A;
577   active_servers_B : [0..MAX_SERVERS_B] init ini_servers_B;
578   active_servers_C : [0..MAX_SERVERS_C] init ini_servers_C;
579   dimmer : [1..DIMMER_LEVELS] init ini_dimmer;
580
581   traffic_A : [0..4] init ini_traffic_A;
582   traffic_B : [0..4] init ini_traffic_B;
583   traffic_C : [0..4] init ini_traffic_C;
584
585   [addServerA_complete] active_servers_A < MAX_SERVERS_A -> 1 :
586     (active_servers_A' = active_servers_A + 1);
587   [addServerB_complete] active_servers_B < MAX_SERVERS_B -> 1 :
588     (active_servers_B' = active_servers_B + 1);
589   [addServerC_complete] active_servers_C < MAX_SERVERS_C -> 1 :
590     (active_servers_C' = active_servers_C + 1);
591
592   [removeServerA_start] active_servers_A > 0 -> 1 : (active_servers_A' =
593     active_servers_A - 1);
594   [removeServerB_start] active_servers_B > 0 -> 1 : (active_servers_B' =
595     active_servers_B - 1);
596   [removeServerC_start] active_servers_C > 0 -> 1 : (active_servers_C' =
597     active_servers_C - 1);
598
598   [increaseDimmer_start] dimmer < DIMMER_LEVELS -> 1 : (dimmer' =
599     dimmer + 1);
600   [decreaseDimmer_start] dimmer > 1 -> 1 : (dimmer' = dimmer - 1);
601
602 //A-B-C
603 //Possible values 0-25-50-75-100
604
605 // 100-0-0
606   [divert_100_0_0] active_servers_A > 0 -> 1 : (traffic_A' = 0) &
607     (traffic_B' = 0) & (traffic_C' = 0);
608 // 75-25-0
609   [divert_75_25_0] active_servers_A > 0 & active_servers_B > 0 -> 1 :
610     (traffic_A' = 3) & (traffic_B' = 1) & (traffic_C' = 0);
611 // 75-0-25
612   [divert_75_0_25] active_servers_A > 0 & active_servers_C > 0 -> 1 :
613     (traffic_A' = 3) & (traffic_B' = 0) & (traffic_C' = 1);
614 // 50-50-0
615   [divert_50_50_0] active_servers_A > 0 & active_servers_B > 0 &
616     active_servers_C > 0 -> 1 : (traffic_A' = 2) & (traffic_B' = 2) & (traffic_C' = 0);
617 // 50-0-50
618   [divert_50_0_50] active_servers_A > 0 & active_servers_C > 0 -> 1 :
619     (traffic_A' = 2) & (traffic_B' = 0) & (traffic_C' = 2);
620 // 50-25-25
621   [divert_50_25_25] active_servers_A > 0 & active_servers_B > 0 &
622     active_servers_C > 0 -> 1 : (traffic_A' = 2) & (traffic_B' = 1) & (traffic_C' = 1);
623 // 25-75-0
624   [divert_25_75_0] active_servers_A > 0 & active_servers_B > 0 -> 1 :
625     (traffic_A' = 1) & (traffic_B' = 3) & (traffic_C' = 0);
626 // 25-0-75
627   [divert_25_0_75] active_servers_A > 0 & active_servers_C > 0 -> 1 :
628     (traffic_A' = 1) & (traffic_B' = 0) & (traffic_C' = 3);
629 // 25-50-25
630   [divert_25_50_25] active_servers_A > 0 & active_servers_B > 0 &
631     active_servers_C > 0 -> 1 : (traffic_A' = 1) & (traffic_B' = 2) & (traffic_C' = 1);
632 // 25-25-50

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627 [divert_25_25_50] active_servers_A > 0 & active_servers_B > 0 &
628     active_servers_C > 0
629     -> 1 : (traffic_A' = 1) & (traffic_B' = 1) & (traffic_C' = 2);
630 // 0-100-0
631 [divert_0_100_0] active_servers_B > 0
632     -> 1 : (traffic_A' = 0) & (traffic_B' = 4) & (traffic_C' = 0);
633 // 0-0-100
634 [divert_0_0_100] active_servers_C > 0
635     -> 1 : (traffic_A' = 0) & (traffic_B' = 0) & (traffic_C' = 4);
636 // 0-75-25
637 [divert_0_75_25] active_servers_B > 0 & active_servers_C > 0
638     -> 1 : (traffic_A' = 0) & (traffic_B' = 3) & (traffic_C' = 1);
639 // 0-25-75
640 [divert_0_25_75] active_servers_B > 0 & active_servers_C > 0
641     -> 1 : (traffic_A' = 0) & (traffic_B' = 1) & (traffic_C' = 3);
642 // 0-50-50
643 [divert_0_50_50] active_servers_B > 0 & active_servers_C > 0
644     -> 1 : (traffic_A' = 0) & (traffic_B' = 2) & (traffic_C' = 2);
645 endmodule
646
647 formula addServerA_applicable = active_servers_A < MAX_SERVERS_A
648     & !removeServer_used
649     & addServerB_state = 0 & addServerC_state = 0;
650 formula addServerB_applicable = active_servers_B < MAX_SERVERS_B
651     & !removeServer_used
652     & addServerA_state = 0 & addServerC_state = 0;
653 formula addServerC_applicable = active_servers_C < MAX_SERVERS_C
654     & !removeServer_used
655     & addServerA_state = 0 & addServerB_state = 0;
656 formula removeServerA_applicable = active_servers_A > 0 &
657     addServerA_state = 0 & active_servers > 1
658     & addServerB_state = 0 & addServerC_state = 0;
659 formula removeServerB_applicable = active_servers_B > 0 &
660     addServerB_state = 0 & active_servers > 1
661     & addServerA_state = 0 & addServerC_state = 0;
662 formula removeServerC_applicable = active_servers_C > 0 &
663     addServerC_state = 0 & active_servers > 1
664     & addServerA_state = 0 & addServerB_state = 0;
665 formula increaseDimmer_compatible = !decreaseDimmer_used;
666 formula decreaseDimmer_compatible = lincreaseDimmer_used;
667 formula increase_dimmer_applicable = dimmer < DIMMER_LEVELS &
668     increaseDimmer_compatible;
669 formula decrease_dimmer_applicable = dimmer > 1 &
670     decreaseDimmer_compatible;
671
672 const int addServer_LATENCY_PERIODS = ceil(addServer_LATENCY /
673     PERIOD);
674
675 // This remove server constraints that only one server could be removed in
676 // one monitoring cycle.
677 module removeServer
678     removeServer_go : bool init true;
679     removeServer_used : bool init false;
680
681     [removeServerA_start] sys_go & removeServer_go
682         & removeServerA_applicable // applicability conditions
683         -> (removeServer_go' = false) & (removeServer_used' = true);
684
685     [removeServerB_start] sys_go & removeServer_go
686         & removeServerB_applicable // applicability conditions
687         -> (removeServer_go' = false) & (removeServer_used' = true);
688
689     [removeServerC_start] sys_go & removeServer_go
690         & removeServerC_applicable // applicability conditions
691         -> (removeServer_go' = false) & (removeServer_used' = true);
692
693 // Case when remove server tactic is applicable but not used
694 [pass_remove_server] sys_go & removeServer_go // can go
695     -> (removeServer_go' = false);
696
697 [tick] !removeServer_go -> 1 : (removeServer_go' = true) &
698     (removeServer_used' = false);
699 endmodule
700
701 module addServer
702     addServerA_state : [0..addServer_LATENCY_PERIODS] init
703         ini_addServerA_state;
704     addServerB_state : [0..addServer_LATENCY_PERIODS] init
705         ini_addServerB_state;
706     addServerC_state : [0..addServer_LATENCY_PERIODS] init
707         ini_addServerC_state;
708
709     ini_addServerC_state;
710
711 addServer_go : bool init true;
712
713 // tactic applicable, start it
714 [addServerA_start] sys_go & addServer_go // can go
715     & addServerA_state = 0 // tactic has not been started
716     & addServerA_applicable
717     -> (addServerA_state' = 1) & (addServer_go' = false);
718
719 // tactic applicable, start it
720 [addServerB_start] sys_go & addServer_go // can go
721     & addServerB_state = 0 // tactic has not been started
722     & addServerB_applicable
723     -> (addServerB_state' = 1) & (addServer_go' = false);
724
725 // tactic applicable, start it
726 [addServerC_start] sys_go & addServer_go // can go
727     & addServerC_state = 0 // tactic has not been started
728     & addServerC_applicable
729     -> (addServerC_state' = 1) & (addServer_go' = false);
730
731 // progress of the tactic
732 [progressA] sys_go & addServer_go
733     & addServerA_state > 0 & addServerA_state <
734         addServer_LATENCY_PERIODS
735     -> 1 : (addServerA_state' = addServerA_state + 1) &
736         (addServer_go' = false);
737
738 [progressB] sys_go & addServer_go
739     & addServerB_state > 0 & addServerB_state <
740         addServer_LATENCY_PERIODS
741     -> 1 : (addServerB_state' = addServerB_state + 1) &
742         (addServer_go' = false);
743
744 [progressC] sys_go & addServer_go
745     & addServerC_state > 0 & addServerC_state <
746         addServer_LATENCY_PERIODS
747     -> 1 : (addServerC_state' = addServerC_state + 1) &
748         (addServer_go' = false);
749
750 // completion of the tactic
751 [addServerA_complete] sys_go & addServer_go
752     & addServerA_state = addServer_LATENCY_PERIODS //
753         completed
754     -> 1 : (addServerA_state' = 0) & (addServer_go' = true); // so that
755         it can start again at this time if needed
756
757 [addServerB_complete] sys_go & addServer_go
758     & addServerB_state = addServer_LATENCY_PERIODS //
759         completed
760     -> 1 : (addServerB_state' = 0) & (addServer_go' = true); // so that
761         it can start again at this time if needed
762
763 [addServerC_complete] sys_go & addServer_go
764     & addServerC_state = addServer_LATENCY_PERIODS //
765         completed
766     -> 1 : (addServerC_state' = 0) & (addServer_go' = true); // so that
767         it can start again at this time if needed
768
769 [tick] !addServer_go -> 1 : (addServer_go' = true);
770 endmodule
771
772 // Make sure that divert traffic is executed at the end i.e.after adding or
773 // removing the servers.
774 formula divert_traffic_applicable = divert_go & !addServer_go &
775     !removeServer_go & !lincreaseDimmer_go & !decreaseDimmer_go;
776
777 module divert_traffic
778     divert_go : bool init true;
779
780     //A-B-C
781     //Possible values 0-25-50-75-100
782
783     // 100-0-0
784 [divert_100_0_0] sys_go & divert_traffic_applicable

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764     -> 1 : (divert_go' = false);
765 // 75-25-0
766 [divert_75_25_0] sys_go & divert_traffic_applicable
767     -> 1 : (divert_go' = false);
768 // 75-0-25
769 [divert_75_0_25] sys_go & divert_traffic_applicable
770     -> 1 : (divert_go' = false);
771 // 50-50-0
772 [divert_50_50_0] sys_go & divert_traffic_applicable
773     -> 1 : (divert_go' = false);
774 // 50-0-50
775 [divert_50_0_50] sys_go & divert_traffic_applicable
776     -> 1 : (divert_go' = false);
777 // 50-25-25
778 [divert_50_25_25] sys_go & divert_traffic_applicable
779     -> 1 : (divert_go' = false);
780 // 25-75-0
781 [divert_25_75_0] sys_go & divert_traffic_applicable
782     -> 1 : (divert_go' = false);
783 // 25-0-75
784 [divert_25_0_75] sys_go & divert_traffic_applicable
785     -> 1 : (divert_go' = false);
786 // 25-50-25
787 [divert_25_50_25] sys_go & divert_traffic_applicable
788     -> 1 : (divert_go' = false);
789 // 25-25-50
790 [divert_25_25_50] sys_go & divert_traffic_applicable
791     -> 1 : (divert_go' = false);
792 // 0-100-0
793 [divert_0_100_0] sys_go & divert_traffic_applicable
794     -> 1 : (divert_go' = false);
795 // 0-0-100
796 [divert_0_0_100] sys_go & divert_traffic_applicable
797     -> 1 : (divert_go' = false);
798 // 0-75-25
799 [divert_0_75_25] sys_go & divert_traffic_applicable
800     -> 1 : (divert_go' = false);
801 // 0-25-75
802 [divert_0_25_75] sys_go & divert_traffic_applicable
803     -> 1 : (divert_go' = false);
804 // 0-50-50
805 [divert_0_50_50] sys_go & divert_traffic_applicable
806     -> 1 : (divert_go' = false);

807 [tick] !divert_go -> 1 : (divert_go' = true);
808 endmodule

809 module increaseDimmer
810   increaseDimmer_go : bool init true;
811   increaseDimmer_used : bool init false;
812
813   [increaseDimmer_start] sys_go & increaseDimmer_go
814     & increase_dimmer_applicable // applicability conditions
815     -> (increaseDimmer_go' = false) & (increaseDimmer_used' = true);
816
817   // tactic applicable but not used
818   [pass_inc_dimmer] sys_go & increaseDimmer_go // can go
819     -> (increaseDimmer_go' = false);
820
821   [tick] !increaseDimmer_go -> 1 : (increaseDimmer_go' = true) &
822     (increaseDimmer_used' = false);
823 endmodule

824 // tactic
825 module decreaseDimmer
826   decreaseDimmer_go : bool init true;
827   decreaseDimmer_used : bool init false;
828
829   [decreaseDimmer_start] sys_go & decreaseDimmer_go
830     & decrease_dimmer_applicable // applicability conditions
831     -> (decreaseDimmer_go' = false) & (decreaseDimmer_used' =
832       true);
833
834   // tactic applicable but not used
835   [pass_dec_dimmer] sys_go & decreaseDimmer_go // can go
836     -> (decreaseDimmer_go' = false);
837
838   [tick] !decreaseDimmer_go -> 1 : (decreaseDimmer_go' = true) &
839     (decreaseDimmer_used' = false);
840 endmodule

841 //***** Queuing network with each server having queueing model of M/G/1/PS
842 // Queuing network with each server having queueing model of M/G/1/PS
843
844 //*****
845 formula dimmerFactor = (dimmer - 1) / (DIMMER_LEVELS - 1);
846 formula interarrivalMean = stateValue * interArrivalScaleFactorForDecision;
847
848 formula Pa = (traffic_A * 25)/100;
849 formula Pb = (traffic_B * 25)/100;
850 formula Pc = (traffic_C * 25)/100;
851
852 formula loaded_servers = (Pa != 0 ? 1 : 0) + (Pb != 0 ? 1 : 0) + (Pc != 0 ? 1 :
853   0);
854
855 formula service_rate_A = dimmerFactor *
856   (MAX_ARRIVALA_CAPACITY_LOW +
857   (1 - dimmerFactor) * (MAX_ARRIVALA_CAPACITY));
858 formula service_rate_B = dimmerFactor *
859   (MAX_ARRIVALB_CAPACITY_LOW +
860   (1 - dimmerFactor) * (MAX_ARRIVALB_CAPACITY));
861 formula service_rate_C = dimmerFactor *
862   (MAX_ARRIVALC_CAPACITY_LOW +
863   (1 - dimmerFactor) * (MAX_ARRIVALC_CAPACITY));
864
864 formula rhoA = Pa/(service_rate_A*interarrivalMean);
865 formula rhoB = Pb/(service_rate_B*interarrivalMean);
866 formula rhoC = Pc/(service_rate_C*interarrivalMean);
867
867 formula overloaded = (rhoA >= 1 | rhoB >= 1 | rhoC >= 1);
868
868 formula rt_A = 1/(service_rate_A - (throughput*Pa));
869 formula rt_B = 1/(service_rate_B - (throughput*Pb));
870 formula rt_C = 1/(service_rate_C - (throughput*Pc));
871
871 // Response time to clients utility function
872 const double RT_THRESHOLD = 1.0;
873
874 formula expected_wait_time = (Pa*rt_A + Pb*rt_B + Pc*rt_C);
875 formula rt = (interarrivalMean = 0 ? 0 : (overloaded ? RT_THRESHOLD + 2 :
876   expected_wait_time));
877
877 const double NORMAL_A_REVENUE = (SERVERA_COST /
878   MAX_ARRIVALA_CAPACITY) * 10;
879 const double DIMMER_A_REVENUE = (SERVERA_COST /
880   MAX_ARRIVALA_CAPACITY_LOW) * 3 / 2;
881 const double NORMAL_B_REVENUE = (SERVERB_COST /
882   MAX_ARRIVALB_CAPACITY) * 10;
883 const double DIMMER_B_REVENUE = (SERVERB_COST /
884   MAX_ARRIVALB_CAPACITY_LOW) * 3 / 2;
885 const double NORMAL_C_REVENUE = (SERVERC_COST /
886   MAX_ARRIVALC_CAPACITY) * 10;
887 const double DIMMER_C_REVENUE = (SERVERC_COST /
888   MAX_ARRIVALC_CAPACITY_LOW) * 3 / 2;
889
889 const double DIMMER_REVENUE = DIMMER_A_REVENUE +
890   DIMMER_B_REVENUE + DIMMER_C_REVENUE;
891
891 const double NORMAL_REVENUE = NORMAL_A_REVENUE +
892   NORMAL_B_REVENUE + NORMAL_C_REVENUE;
893
893 formula serverA_cost = ((addServerA_state > 0 ? 1 : 0) +
894   active_servers_A) * SERVERA_COST;
895 formula serverB_cost = ((addServerB_state > 0 ? 1 : 0) +
896   active_servers_B) * SERVERB_COST;
897 formula serverC_cost = ((addServerC_state > 0 ? 1 : 0) +
898   active_servers_C) * SERVERC_COST;
899 formula cost = serverA_cost + serverB_cost + serverC_cost;
900
900 formula throughput = 1/interarrivalMean;
901
901 formula basicUtilityA = throughput * Pa * (dimmerFactor *
902   DIMMER_A_REVENUE + (1 - dimmerFactor) *
903   NORMAL_A_REVENUE);
904 formula basicUtilityB = throughput * Pb * (dimmerFactor *
905   DIMMER_B_REVENUE + (1 - dimmerFactor) *
906   NORMAL_B_REVENUE);
907 formula basicUtilityC = throughput * Pc * (dimmerFactor *
908   DIMMER_C_REVENUE + (1 - dimmerFactor) *
909   NORMAL_C_REVENUE);
910
910 formula basicUtility = basicUtilityA + basicUtilityB + basicUtilityC;
911 formula active_servers = active_servers_A + active_servers_B +
912   active_servers_C;
913 formula poweredServers = (addServerA_state > 0 ? 1 : 0) +
914   (addServerB_state > 0 ? 1 : 0) + (addServerC_state > 0 ? 1 : 0) +
915   active_servers;
916 formula MAX_SERVERS = MAX_SERVERS_A + MAX_SERVERS_B +

```

```

903 MAX_SERVERS_C;
904
905 formula MAX_SERVER_COST = MAX_SERVERS_A * SERVERA_COST
906     + MAX_SERVERS_B * SERVERB_COST
907     + MAX_SERVERS_C * SERVERC_COST;
908
909 formula netPenalty = stateValue > 0 ? penalty / stateValue : 0;
910
911 formula uTotal = (overloaded & (poweredServers < MAX_SERVERS |
912     dimmer < DIMMER_LEVELS | active_servers != loaded_servers))
913     ? -(1000) // avoid unstable solutions
914     : (((rt > RT_THRESHOLD | rt <= 0) ? netPenalty :
915         basicUtility) - cost);
916
917 rewards "util"
918     // 100000000.0 is added to avoid a negative value during calculation;
919     // negative utility is not supported by PRISM.
920     [tack] true : 100000000.0 + (PERIOD)*(uTotal);
921 endrewards

```

Listing 2. PRISM specification for MDP planning

*Q: What are the Exact Planning Specification for the Team of UAVs?*

Listing 3 and Listing 4 provide PRISM planning specifications for non-wait reactive (i.e., the short-horizon MDP with a subset of actions) and deliberative (i.e., the long-horizon MDP) planning (respectively) for a planning. These specifications have some constants (e.g., *threatRange*, *sensorRange*) that remain same for all the planning problems (i.e., specifications). However, there are variables (e.g., current altitude *ini\_a*, and formation *ini\_f* that depend on the current state (i.e., initial state of the planning problem) of the system. These specifications also include modeling of the environment for this particular problem.

*Short Horizon MDP Planning Specification:* Reactive planning  $\rho_{mdps}$  plans with a shorter horizon compared to deliberative planning  $\rho_{mdpl}$ . Moreover, while planning,  $\rho_{mdps}$  do not consider adaptation actions *IncAlt*, *DecAlt*, and *EcmOn*, and *EcmOff*.

```

1  mdp
2  const double PERIOD = 60;
3  const int HORIZON = 2; // Planning horizon for reactive planning
4  const double IncAlt_LATENCY = 60;
5  const double DecAlt_LATENCY = 60;
6  const int MAX_ALT_LEVEL = 3;
7  const double destructionFormationFactor = 1.5;
8  const double threatRange = 3;
9  const double detectionFormationFactor = 1.2;
10 const double sensorRange = 4;
11 const int init_a = 0;
12 const int init_c = 0;
13 const int init_f = 0;
14 const bool ECM_ENABLED = false; // ECM is not enabled for reactive
15   planning
16 const bool ONE_LEVEL_ENABLED = false; // This is not enabled for
17   reactive planning
18 const bool TWO_LEVEL_ENABLED = true; // Two level increase/decrease
19   altitude enabled
20 const int ini_IncAlt_state = 0;
21 const int ini_DecAlt_state = 0;
22 const int ini_IncAlt2_state = 0;
23 const int ini_DecAlt2_state = 0;
24 const double ecm_threat_prob = 0.15;
25 const double ecm_target_prob = 0.3;
26 const double survival_reward = 1;
27
28 //*****
29 // CLOCK
30 //*****
31 const int TO_TICK = 0;
32 const int TO_TICK2 = 1; // intermediate tick for constraint satisf. update
33 const int TO_TACK = 2;
34
35 label "final" = time = HORIZON & clockstep=TO_TICK;
36 formula sys_go = clockstep=TO_TICK;
37
38 module clk
39   time : [0..HORIZON] init 0;
40   clockstep : [0..2] init TO_TICK;
41
42   [tick] clockstep=TO_TICK & time < HORIZON -> 1: (time'=time+1) &
43       (clockstep'=TO_TICK2);
44   [tick2] clockstep=TO_TICK2 -> 1: (clockstep'=TO_TACK);
45   [tack] clockstep=TO_TACK -> 1: (clockstep'=TO_TICK);
46 endmodule
47
48 module env
49   s : [0..45] init 0;
50   [tick] s = 0 ->
51       0.034225 : (s' = 1)
52       + 0.11655 : (s' = 2)
53       + 0.034225 : (s' = 3)
54       + 0.11655 : (s' = 4)
55       + 0.3969 : (s' = 5)
56       + 0.11655 : (s' = 6)

```

```

54    + 0.034225 : (s' = 7)
55    + 0.11655 : (s' = 8)
56    + 0.034225 : (s' = 9);
57 [tick] s = 1 ->
58    0.034225 : (s' = 10)
59    + 0.11655 : (s' = 11)
60    + 0.034225 : (s' = 12)
61    + 0.11655 : (s' = 13)
62    + 0.3969 : (s' = 14)
63    + 0.11655 : (s' = 15)
64    + 0.034225 : (s' = 16)
65    + 0.11655 : (s' = 17)
66    + 0.034225 : (s' = 18);
67 [tick] s = 2 ->
68    0.034225 : (s' = 10)
69    + 0.11655 : (s' = 11)
70    + 0.034225 : (s' = 12)
71    + 0.11655 : (s' = 13)
72    + 0.3969 : (s' = 14)
73    + 0.11655 : (s' = 15)
74    + 0.034225 : (s' = 16)
75    + 0.11655 : (s' = 17)
76    + 0.034225 : (s' = 18);
77 [tick] s = 3 ->
78    0.034225 : (s' = 10)
79    + 0.11655 : (s' = 11)
80    + 0.034225 : (s' = 12)
81    + 0.11655 : (s' = 13)
82    + 0.3969 : (s' = 14)
83    + 0.11655 : (s' = 15)
84    + 0.034225 : (s' = 16)
85    + 0.11655 : (s' = 17)
86    + 0.034225 : (s' = 18);
87 [tick] s = 4 ->
88    0.034225 : (s' = 10)
89    + 0.11655 : (s' = 11)
90    + 0.034225 : (s' = 12)
91    + 0.11655 : (s' = 13)
92    + 0.3969 : (s' = 14)
93    + 0.11655 : (s' = 15)
94    + 0.034225 : (s' = 16)
95    + 0.11655 : (s' = 17)
96    + 0.034225 : (s' = 18);
97 [tick] s = 5 ->
98    0.034225 : (s' = 10)
99    + 0.11655 : (s' = 11)
100   + 0.034225 : (s' = 12)
101   + 0.11655 : (s' = 13)
102   + 0.3969 : (s' = 14)
103   + 0.11655 : (s' = 15)
104   + 0.034225 : (s' = 16)
105   + 0.11655 : (s' = 17)
106   + 0.034225 : (s' = 18);
107 [tick] s = 6 ->
108   0.034225 : (s' = 10)
109   + 0.11655 : (s' = 11)
110   + 0.034225 : (s' = 12)
111   + 0.11655 : (s' = 13)
112   + 0.3969 : (s' = 14)
113   + 0.11655 : (s' = 15)
114   + 0.034225 : (s' = 16)
115   + 0.11655 : (s' = 17)
116   + 0.034225 : (s' = 18);
117 [tick] s = 7 ->
118   0.034225 : (s' = 10)
119   + 0.11655 : (s' = 11)
120   + 0.034225 : (s' = 12)
121   + 0.11655 : (s' = 13)
122   + 0.3969 : (s' = 14)
123   + 0.11655 : (s' = 15)
124   + 0.034225 : (s' = 16)
125   + 0.11655 : (s' = 17)
126   + 0.034225 : (s' = 18);
127 [tick] s = 8 ->
128   0.034225 : (s' = 10)
129   + 0.11655 : (s' = 11)
130   + 0.034225 : (s' = 12)
131   + 0.11655 : (s' = 13)
132   + 0.3969 : (s' = 14)
133   + 0.11655 : (s' = 15)
134   + 0.034225 : (s' = 16)
135   + 0.11655 : (s' = 17)
136   + 0.034225 : (s' = 18);
137 [tick] s = 9 ->
138   0.034225 : (s' = 10)
139   + 0.11655 : (s' = 11)
140   + 0.034225 : (s' = 12)
141   + 0.11655 : (s' = 13)
142   + 0.3969 : (s' = 14)
143   + 0.11655 : (s' = 15)
144   + 0.034225 : (s' = 16)
145   + 0.11655 : (s' = 17)
146   + 0.034225 : (s' = 18);
147 [tick] s = 10 ->
148   0.034225 : (s' = 19)
149   + 0.11655 : (s' = 20)
150   + 0.034225 : (s' = 21)
151   + 0.11655 : (s' = 22)
152   + 0.3969 : (s' = 23)
153   + 0.11655 : (s' = 24)
154   + 0.034225 : (s' = 25)
155   + 0.11655 : (s' = 26)
156   + 0.034225 : (s' = 27);
157 [tick] s = 11 ->
158   0.034225 : (s' = 19)
159   + 0.11655 : (s' = 20)
160   + 0.034225 : (s' = 21)
161   + 0.11655 : (s' = 22)
162   + 0.3969 : (s' = 23)
163   + 0.11655 : (s' = 24)
164   + 0.034225 : (s' = 25)
165   + 0.11655 : (s' = 26)
166   + 0.034225 : (s' = 27);
167 [tick] s = 12 ->
168   0.034225 : (s' = 19)
169   + 0.11655 : (s' = 20)
170   + 0.034225 : (s' = 21)
171   + 0.11655 : (s' = 22)
172   + 0.3969 : (s' = 23)
173   + 0.11655 : (s' = 24)
174   + 0.034225 : (s' = 25)
175   + 0.11655 : (s' = 26)
176   + 0.034225 : (s' = 27);
177 [tick] s = 13 ->
178   0.034225 : (s' = 19)
179   + 0.11655 : (s' = 20)
180   + 0.034225 : (s' = 21)
181   + 0.11655 : (s' = 22)
182   + 0.3969 : (s' = 23)
183   + 0.11655 : (s' = 24)
184   + 0.034225 : (s' = 25)
185   + 0.11655 : (s' = 26)
186   + 0.034225 : (s' = 27);
187 [tick] s = 14 ->
188   0.034225 : (s' = 19)
189   + 0.11655 : (s' = 20)
190   + 0.034225 : (s' = 21)
191   + 0.11655 : (s' = 22)
192   + 0.3969 : (s' = 23)
193   + 0.11655 : (s' = 24)
194   + 0.034225 : (s' = 25)
195   + 0.11655 : (s' = 26)
196   + 0.034225 : (s' = 27);
197 [tick] s = 15 ->
198   0.034225 : (s' = 19)
199   + 0.11655 : (s' = 20)
200   + 0.034225 : (s' = 21)
201   + 0.11655 : (s' = 22)
202   + 0.3969 : (s' = 23)
203   + 0.11655 : (s' = 24)
204   + 0.034225 : (s' = 25)
205   + 0.11655 : (s' = 26)
206   + 0.034225 : (s' = 27);
207 [tick] s = 16 ->
208   0.034225 : (s' = 19)
209   + 0.11655 : (s' = 20)
210   + 0.034225 : (s' = 21)
211   + 0.11655 : (s' = 22)
212   + 0.3969 : (s' = 23)
213   + 0.11655 : (s' = 24)
214   + 0.034225 : (s' = 25)
215   + 0.11655 : (s' = 26)
216   + 0.034225 : (s' = 27);
217 [tick] s = 17 ->
218   0.034225 : (s' = 19)
219   + 0.11655 : (s' = 20)

```

```

220      + 0.034225 : (s' = 21)
221      + 0.11655 : (s' = 22)
222      + 0.3969 : (s' = 23)
223      + 0.11655 : (s' = 24)
224      + 0.034225 : (s' = 25)
225      + 0.11655 : (s' = 26)
226      + 0.034225 : (s' = 27);
227 [tick] s = 18 ->
228      0.034225 : (s' = 19)
229      + 0.11655 : (s' = 20)
230      + 0.034225 : (s' = 21)
231      + 0.11655 : (s' = 22)
232      + 0.3969 : (s' = 23)
233      + 0.11655 : (s' = 24)
234      + 0.034225 : (s' = 25)
235      + 0.11655 : (s' = 26)
236      + 0.034225 : (s' = 27);
237 [tick] s = 19 ->
238      0.034225 : (s' = 28)
239      + 0.11655 : (s' = 29)
240      + 0.034225 : (s' = 30)
241      + 0.11655 : (s' = 31)
242      + 0.3969 : (s' = 32)
243      + 0.11655 : (s' = 33)
244      + 0.034225 : (s' = 34)
245      + 0.11655 : (s' = 35)
246      + 0.034225 : (s' = 36);
247 [tick] s = 20 ->
248      0.034225 : (s' = 28)
249      + 0.11655 : (s' = 29)
250      + 0.034225 : (s' = 30)
251      + 0.11655 : (s' = 31)
252      + 0.3969 : (s' = 32)
253      + 0.11655 : (s' = 33)
254      + 0.034225 : (s' = 34)
255      + 0.11655 : (s' = 35)
256      + 0.034225 : (s' = 36);
257 [tick] s = 21 ->
258      0.034225 : (s' = 28)
259      + 0.11655 : (s' = 29)
260      + 0.034225 : (s' = 30)
261      + 0.11655 : (s' = 31)
262      + 0.3969 : (s' = 32)
263      + 0.11655 : (s' = 33)
264      + 0.034225 : (s' = 34)
265      + 0.11655 : (s' = 35)
266      + 0.034225 : (s' = 36);
267 [tick] s = 22 ->
268      0.034225 : (s' = 28)
269      + 0.11655 : (s' = 29)
270      + 0.034225 : (s' = 30)
271      + 0.11655 : (s' = 31)
272      + 0.3969 : (s' = 32)
273      + 0.11655 : (s' = 33)
274      + 0.034225 : (s' = 34)
275      + 0.11655 : (s' = 35)
276      + 0.034225 : (s' = 36);
277 [tick] s = 23 ->
278      0.034225 : (s' = 28)
279      + 0.11655 : (s' = 29)
280      + 0.034225 : (s' = 30)
281      + 0.11655 : (s' = 31)
282      + 0.3969 : (s' = 32)
283      + 0.11655 : (s' = 33)
284      + 0.034225 : (s' = 34)
285      + 0.11655 : (s' = 35)
286      + 0.034225 : (s' = 36);
287 [tick] s = 24 ->
288      0.034225 : (s' = 28)
289      + 0.11655 : (s' = 29)
290      + 0.034225 : (s' = 30)
291      + 0.11655 : (s' = 31)
292      + 0.3969 : (s' = 32)
293      + 0.11655 : (s' = 33)
294      + 0.034225 : (s' = 34)
295      + 0.11655 : (s' = 35)
296      + 0.034225 : (s' = 36);
297 [tick] s = 25 ->
298      0.034225 : (s' = 28)
299      + 0.11655 : (s' = 29)
300      + 0.034225 : (s' = 30)
301      + 0.11655 : (s' = 31)
302      + 0.3969 : (s' = 32)
303      + 0.11655 : (s' = 33)
304      + 0.034225 : (s' = 34)
305      + 0.11655 : (s' = 35)
306      + 0.034225 : (s' = 36);
307 [tick] s = 26 ->
308      0.034225 : (s' = 28)
309      + 0.11655 : (s' = 29)
310      + 0.034225 : (s' = 30)
311      + 0.11655 : (s' = 31)
312      + 0.3969 : (s' = 32)
313      + 0.11655 : (s' = 33)
314      + 0.034225 : (s' = 34)
315      + 0.11655 : (s' = 35)
316      + 0.034225 : (s' = 36);
317 [tick] s = 27 ->
318      0.034225 : (s' = 28)
319      + 0.11655 : (s' = 29)
320      + 0.034225 : (s' = 30)
321      + 0.11655 : (s' = 31)
322      + 0.3969 : (s' = 32)
323      + 0.11655 : (s' = 33)
324      + 0.034225 : (s' = 34)
325      + 0.11655 : (s' = 35)
326      + 0.034225 : (s' = 36);
327 [tick] s = 28 ->
328      0.034225 : (s' = 37)
329      + 0.11655 : (s' = 38)
330      + 0.034225 : (s' = 39)
331      + 0.11655 : (s' = 40)
332      + 0.3969 : (s' = 41)
333      + 0.11655 : (s' = 42)
334      + 0.034225 : (s' = 43)
335      + 0.11655 : (s' = 44)
336      + 0.034225 : (s' = 45);
337 [tick] s = 29 ->
338      0.034225 : (s' = 37)
339      + 0.11655 : (s' = 38)
340      + 0.034225 : (s' = 39)
341      + 0.11655 : (s' = 40)
342      + 0.3969 : (s' = 41)
343      + 0.11655 : (s' = 42)
344      + 0.034225 : (s' = 43)
345      + 0.11655 : (s' = 44)
346      + 0.034225 : (s' = 45);
347 [tick] s = 30 ->
348      0.034225 : (s' = 37)
349      + 0.11655 : (s' = 38)
350      + 0.034225 : (s' = 39)
351      + 0.11655 : (s' = 40)
352      + 0.3969 : (s' = 41)
353      + 0.11655 : (s' = 42)
354      + 0.034225 : (s' = 43)
355      + 0.11655 : (s' = 44)
356      + 0.034225 : (s' = 45);
357 [tick] s = 31 ->
358      0.034225 : (s' = 37)
359      + 0.11655 : (s' = 38)
360      + 0.034225 : (s' = 39)
361      + 0.11655 : (s' = 40)
362      + 0.3969 : (s' = 41)
363      + 0.11655 : (s' = 42)
364      + 0.034225 : (s' = 43)
365      + 0.11655 : (s' = 44)
366      + 0.034225 : (s' = 45);
367 [tick] s = 32 ->
368      0.034225 : (s' = 37)
369      + 0.11655 : (s' = 38)
370      + 0.034225 : (s' = 39)
371      + 0.11655 : (s' = 40)
372      + 0.3969 : (s' = 41)
373      + 0.11655 : (s' = 42)
374      + 0.034225 : (s' = 43)
375      + 0.11655 : (s' = 44)
376      + 0.034225 : (s' = 45);
377 [tick] s = 33 ->
378      0.034225 : (s' = 37)
379      + 0.11655 : (s' = 38)
380      + 0.034225 : (s' = 39)
381      + 0.11655 : (s' = 40)
382      + 0.3969 : (s' = 41)
383      + 0.11655 : (s' = 42)
384      + 0.034225 : (s' = 43)
385      + 0.11655 : (s' = 44)

```

```

386     + 0.034225 : (s' = 45);
387 [tick] s = 34 ->
388     0.034225 : (s' = 37)
389     + 0.11655 : (s' = 38)
390     + 0.034225 : (s' = 39)
391     + 0.11655 : (s' = 40)
392     + 0.3969 : (s' = 41)
393     + 0.11655 : (s' = 42)
394     + 0.034225 : (s' = 43)
395     + 0.11655 : (s' = 44)
396     + 0.034225 : (s' = 45);
397 [tick] s = 35 ->
398     0.034225 : (s' = 37)
399     + 0.11655 : (s' = 38)
400     + 0.034225 : (s' = 39)
401     + 0.11655 : (s' = 40)
402     + 0.3969 : (s' = 41)
403     + 0.11655 : (s' = 42)
404     + 0.034225 : (s' = 43)
405     + 0.11655 : (s' = 44)
406     + 0.034225 : (s' = 45);
407 [tick] s = 36 ->
408     0.034225 : (s' = 37)
409     + 0.11655 : (s' = 38)
410     + 0.034225 : (s' = 39)
411     + 0.11655 : (s' = 40)
412     + 0.3969 : (s' = 41)
413     + 0.11655 : (s' = 42)
414     + 0.034225 : (s' = 43)
415     + 0.11655 : (s' = 44)
416     + 0.034225 : (s' = 45);
417 endmodule
418
419 // environment has 2 components. stateValue for threats and stateValue1 is
420 // for targets
421 formula stateValue = (s = 0 ? 0 : 0) +
422     (s = 1 ? 0.00605639 : 0) +
423     (s = 2 ? 0.00605639 : 0) +
424     (s = 3 ? 0.00605639 : 0) +
425     (s = 4 ? 0.0282836 : 0) +
426     (s = 5 ? 0.0282836 : 0) +
427     (s = 6 ? 0.0282836 : 0) +
428     (s = 7 ? 0.0778979 : 0) +
429     (s = 8 ? 0.0778979 : 0) +
430     (s = 9 ? 0.0778979 : 0) +
431     (s = 10 ? 0 : 0) +
432     (s = 11 ? 0 : 0) +
433     (s = 12 ? 0 : 0) +
434     (s = 13 ? 0 : 0) +
435     (s = 14 ? 0 : 0) +
436     (s = 15 ? 0 : 0) +
437     (s = 16 ? 0 : 0) +
438     (s = 17 ? 0 : 0) +
439     (s = 18 ? 0 : 0) +
440     (s = 19 ? 0.750751 : 0) +
441     (s = 20 ? 0.750751 : 0) +
442     (s = 21 ? 0.750751 : 0) +
443     (s = 22 ? 0.885424 : 0) +
444     (s = 23 ? 0.885424 : 0) +
445     (s = 24 ? 0.885424 : 0) +
446     (s = 25 ? 0.963485 : 0) +
447     (s = 26 ? 0.963485 : 0) +
448     (s = 27 ? 0.963485 : 0) +
449     (s = 28 ? 0.435626 : 0) +
450     (s = 29 ? 0.435626 : 0) +
451     (s = 30 ? 0.435626 : 0) +
452     (s = 31 ? 0.676196 : 0) +
453     (s = 32 ? 0.676196 : 0) +
454     (s = 33 ? 0.676196 : 0) +
455     (s = 34 ? 0.864925 : 0) +
456     (s = 35 ? 0.864925 : 0) +
457     (s = 36 ? 0.864925 : 0) +
458     (s = 37 ? 0.368403 : 0) +
459     (s = 38 ? 0.368403 : 0) +
460     (s = 39 ? 0.368403 : 0) +
461     (s = 40 ? 0.793701 : 0) +
462     (s = 41 ? 0.793701 : 0) +
463     (s = 42 ? 0.793701 : 0) +
464     (s = 43 ? 0.983048 : 0) +
465     (s = 44 ? 0.983048 : 0) +
466     (s = 45 ? 0.983048 : 0);
467
468 formula stateValue1 = (s = 0 ? 0 : 0) +
469     (s = 1 ? 0.830037 : 0) +
470     (s = 2 ? 0.904439 : 0) +
471     (s = 3 ? 0.954777 : 0) +
472     (s = 4 ? 0.830037 : 0) +
473     (s = 5 ? 0.904439 : 0) +
474     (s = 6 ? 0.954777 : 0) +
475     (s = 7 ? 0.830037 : 0) +
476     (s = 8 ? 0.904439 : 0) +
477     (s = 9 ? 0.954777 : 0) +
478     (s = 10 ? 0 : 0) +
479     (s = 11 ? 0 : 0) +
480     (s = 12 ? 0 : 0) +
481     (s = 13 ? 0 : 0) +
482     (s = 14 ? 0 : 0) +
483     (s = 15 ? 0 : 0) +
484     (s = 16 ? 0 : 0) +
485     (s = 17 ? 0 : 0) +
486     (s = 18 ? 0 : 0) +
487     (s = 19 ? 0.0156741 : 0) +
488     (s = 20 ? 0.0719057 : 0) +
489     (s = 21 ? 0.190204 : 0) +
490     (s = 22 ? 0.0156741 : 0) +
491     (s = 23 ? 0.0719057 : 0) +
492     (s = 24 ? 0.190204 : 0) +
493     (s = 25 ? 0.0156741 : 0) +
494     (s = 26 ? 0.0719057 : 0) +
495     (s = 27 ? 0.190204 : 0) +
496     (s = 28 ? 0 : 0) +
497     (s = 29 ? 0 : 0) +
498     (s = 30 ? 0 : 0) +
499     (s = 31 ? 0 : 0) +
500     (s = 32 ? 0 : 0) +
501     (s = 33 ? 0 : 0) +
502     (s = 34 ? 0 : 0) +
503     (s = 35 ? 0 : 0) +
504     (s = 36 ? 0 : 0) +
505     (s = 37 ? 0 : 0) +
506     (s = 38 ? 0 : 0) +
507     (s = 39 ? 0 : 0) +
508     (s = 40 ? 0 : 0) +
509     (s = 41 ? 0 : 0) +
510     (s = 42 ? 0 : 0) +
511     (s = 43 ? 0 : 0) +
512     (s = 44 ? 0 : 0) +
513     (s = 45 ? 0 : 0);
514
515 //***** SYSTEM *****
516 // SYSTEM
517 //*****
518
519 // Variable range and initialization
520 const a_MIN=0; const a_MAX=MAX_ALT_LEVEL; const a_INIT=init_a;
521 const f_MIN=0; const f_MAX=1; const f_INIT=init_f;
522 const c_MIN=0; const c_MAX=1; const c_INIT=init_c;
523
524 module sys
525   a : [a_MIN..a_MAX] init a_INIT;
526   f : [f_MIN..f_MAX] init f_INIT;
527   c : [c_MIN..c_MAX] init c_INIT;
528
529   [EcmOn_start] c=0 & ECM_ENABLED -> 1: (c'=c_EcmOn_impact);
530   [EcmOff_start] c=1 & ECM_ENABLED -> 1: (c'=c_EcmOff_impact);
531
532   [GoTight_start] f=0 -> 1: (a'=a_GoTight_impact)
533   & (f'=f_GoTight_impact);
534   [GoLoose_start] f=1 -> 1: (a'=a_GoLoose_impact)
535   & (f'=f_GoLoose_impact);
536
537   [IncAlt_complete] a < MAX_ALT_LEVEL & ONE_LEVEL_ENABLED ->
538   1: (a'=a_IncAlt_impact)
539   & (f'=f_IncAlt_impact);
540   [IncAlt2_complete] a < MAX_ALT_LEVEL-1 &
541   TWO_LEVEL_ENABLED -> 1: (a'=a_IncAlt2_impact);
542
543   [DecAlt_complete] a > 0 & ONE_LEVEL_ENABLED -> 1:
544   (a'=a_DecAlt_impact)
545   & (f'=f_DecAlt_impact);
546   [DecAlt2_complete] a > 1 & TWO_LEVEL_ENABLED -> 1:
547   (a'=a_DecAlt2_impact);
548
549 endmodule

```

```

547 formula c_EcmOn_impact = c + (1) >= c_MIN ? (c+(1)<=c_MAX? c+(1) :  
548   c_MAX) : c_MIN;  
549 formula c_EcmOff_impact = c + (-1) >= c_MIN ? (c+(-1)<=c_MAX?  
550   c+(-1) : c_MAX) : c_MIN;  
551 formula a_GoTight_impact = a + (0) >= a_MIN ? (a+(0)<=a_MAX? a+(0) :  
552   a_MAX) : a_MIN;  
553 formula f_GoTight_impact = f + (1) >= f_MIN ? (f+(1)<=f_MAX? f+(1) :  
554   f_MAX) : f_MIN;  
555 formula a_GoLoose_impact = a + (0) >= a_MIN ? (a+(0)<=a_MAX? a+(0) :  
556   a_MAX) : a_MIN;  
557 formula f_GoLoose_impact = f + (-1) >= f_MIN ? (f+(-1)<=f_MAX? f+(-1) :  
558   f_MAX) : f_MIN;  
559 formula a_IncAlt_impact = a + (1) >= a_MIN ? (a+(1)<=a_MAX? a+(1) :  
560   a_MAX) : a_MIN;  
561 formula f_IncAlt_impact = f + (0) >= f_MIN ? (f+(0)<=f_MAX? f+(0) :  
562   f_MAX) : f_MIN;  
563 formula a_DecAlt_impact = a + (-1) >= a_MIN ? (a+(-1)<=a_MAX?  
564   a+(-1) : a_MAX) : a_MIN;  
565 formula f_DecAlt_impact = f + (0) >= f_MIN ? (f+(0)<=f_MAX? f+(0) :  
566   f_MAX) : f_MIN;  
567 formula a_IncAlt2_impact = a + (2) >= a_MIN ? (a+(2)<=a_MAX? a+(2) :  
568   a_MAX) : a_MIN;  
569 formula a_DecAlt2_impact = a + (-2) >= a_MIN ? (a+(-2)<=a_MAX?  
570   a+(-2) : a_MAX) : a_MIN;  
571 // tactic concurrency rules  
572 formula IncAlt_used = IncAlt_state != 0;  
573 formula DecAlt_used = DecAlt_state != 0;  
574 formula IncAlt2_used = IncAlt2_state != 0;  
575 formula DecAlt2_used = DecAlt2_state != 0;  
576 formula EcmOn_compatible = !EcmOn_used;  
577 formula EcmOff_compatible = !EcmOff_used;  
578 formula GoTight_compatible = !GoLoose_used;  
579 formula GoLoose_compatible = !GoTight_used;  
580 formula IncAlt_compatible = (!DecAlt_used) & (!IncAlt2_used) &  
581   (!DecAlt2_used);  
582 formula DecAlt_compatible = (!IncAlt_used) & (!IncAlt2_used) &  
583   (!DecAlt2_used);  
584 formula IncAlt2_compatible = (!DecAlt_used) & (!DecAlt_used) &  
585   (!IncAlt2_used);  
586 formula DecAlt2_compatible = (!DecAlt_used) & (!IncAlt_used) &  
587   (!IncAlt2_used);  
588 // TACTIC: EcmOn  
589 // Applicability conditions  
590 formula EcmOn_applicable = EcmOn_compatible & c=0;  
591 module EcmOn  
592   EcmOn_used : bool init false;  
593   EcmOn_go : bool init true;  
594   // Tactic applicable, start it  
595   [EcmOn_start] sys_go & EcmOn_go & EcmOn_applicable &  
596     ECM_ENABLED -> (EcmOn_used'=true) & (EcmOn_go'=false);  
597   // Tactic applicable, but do not start it  
598   [EcmOn_pass] sys_go & EcmOn_go & EcmOn_applicable ->  
599     (EcmOn_go'=false);  
600   // Pass if the tactic is not applicable  
601   [EcmOn_invalid] sys_go & EcmOn_go & !EcmOn_applicable -> 1 :  
602     (EcmOn_go'=false);  
603   [tick] !EcmOn_go -> 1: (EcmOn_go'=true) & (EcmOn_used'=false);  
604 endmodule  
605 // TACTIC: EcmOff  
606 // Applicability conditions  
607 formula EcmOff_applicable = EcmOff_compatible & c=1;  
608 module EcmOff  
609   EcmOff_used : bool init false;  
610   EcmOff_go : bool init true;  
611   // Tactic applicable, start it  
612   [EcmOff_start] sys_go & EcmOff_go & EcmOff_applicable &  
613     ECM_ENABLED -> (EcmOff_used'=true) & (EcmOff_go'=false);  
614   // Tactic applicable, but do not start it  
615   [EcmOff_pass] sys_go & EcmOff_go & EcmOff_applicable ->  
616     (EcmOff_go'=false);  
617   // Pass if the tactic is not applicable  
618   [EcmOff_invalid] sys_go & EcmOff_go & !EcmOff_applicable -> 1 :  
619     (EcmOff_go'=false);  
620   [tick] !EcmOff_go -> 1: (EcmOff_go'=true) & (EcmOff_used'=false);  
621 endmodule  
622 *****  
623 // TACTIC: GoTight  
624 *****  
625 // Applicability conditions  
626 formula GoTight_applicable = GoTight_compatible & f=0;  
627 module GoTight  
628   GoTight_used : bool init false;  
629   GoTight_go : bool init true;  
630   // Tactic applicable, start it  
631   [GoTight_start] sys_go & GoTight_go & GoTight_applicable ->  
632     (GoTight_used'=true) & (GoTight_go'=false);  
633   // Tactic applicable, but do not start it  
634   [GoTight_pass] sys_go & GoTight_go & GoTight_applicable ->  
635     (GoTight_go'=false);  
636   // Pass if the tactic is not applicable  
637   [GoTight_invalid] sys_go & GoTight_go & !GoTight_applicable -> 1 :  
638     (GoTight_go'=false);  
639   [tick] !GoTight_go -> 1: (GoTight_go'=true) & (GoTight_used'=false);  
640 endmodule  
641 *****  
642 // TACTIC: GoLoose  
643 *****  
644 // Applicability conditions  
645 formula GoLoose_applicable = GoLoose_compatible & f=1;  
646 module GoLoose  
647   GoLoose_used : bool init false;  
648   GoLoose_go : bool init true;  
649   // Tactic applicable, start it  
650   [GoLoose_start] sys_go & GoLoose_go & GoLoose_applicable ->  
651     (GoLoose_used'=true) & (GoLoose_go'=false);  
652   // Tactic applicable, but do not start it  
653   [GoLoose_pass] sys_go & GoLoose_go & GoLoose_applicable ->  
654     (GoLoose_go'=false);  
655   // Pass if the tactic is not applicable  
656   [GoLoose_invalid] sys_go & GoLoose_go & !GoLoose_applicable -> 1 :  
657     (GoLoose_go'=false);  
658   [tick] !GoLoose_go -> 1: (GoLoose_go'=true) &  
659   (GoLoose_used'=false);  
660 endmodule  
661 *****  
662 // TACTIC: IncAlt  
663 *****  
664 const int IncAlt_LATENCY_PERIODS = ceil(IncAlt_LATENCY/PERIOD);  
665 // Applicability conditions  
666 formula IncAlt_applicable = IncAlt_compatible & a < MAX_ALT_LEVEL;  
667 module IncAlt  
668   IncAlt_state : [0..IncAlt_LATENCY_PERIODS] init ini_IncAlt_state;  
669   IncAlt_go : bool init true;
```

```

684 // Tactic applicable, start it
685 [IncAlt_start] sys_go & IncAlt_go & IncAlt_state=0 & IncAlt_applicable &
686   ONE_LEVEL_ENABLED ->
687     (IncAlt_state'=IncAlt_LATENCY_PERIODS) & (IncAlt_go'=false);
688 // Tactic applicable, but do not start it
689 [IncAlt_pass] sys_go & IncAlt_go & IncAlt_state=0 & IncAlt_applicable
690   -> (IncAlt_go'=false);
691 // Pass if the tactic is not applicable
692 [IncAlt_invalid] sys_go & IncAlt_go & IncAlt_state=0 & !IncAlt_applicable
693   -> 1 : (IncAlt_go'=false);
694 // Progress of the tactic
695 [IncAlt_progress] sys_go & IncAlt_go & IncAlt_state > 1 -> 1:
696   (IncAlt_state'=IncAlt_state-1) & (IncAlt_go'=false);
697 // Completion of the tactic
698 [IncAlt_complete] sys_go & IncAlt_go & IncAlt_state=1 -> 1:
699   (IncAlt_state'=0) & (IncAlt_go'=true);
700 [tick] !IncAlt_go -> 1: (IncAlt_go'=true);
701 endmodule
702
703 //*****// TACTIC: DecAlt
704 //*****// TACTIC: DecAlt
705 //*****// TACTIC: DecAlt
706 //*****// TACTIC: DecAlt
707
708 const int DecAlt_LATENCY_PERIODS = ceil(DecAlt_LATENCY/PERIOD);
709
710 // Applicability conditions
711 formula DecAlt_applicable = DecAlt_compatible & a > 0;
712
713 module DecAlt
714   DecAlt_state : [0..DecAlt_LATENCY_PERIODS] init ini_DecAlt_state;
715   DecAlt_go : bool init true;
716
717 // Tactic applicable, start it
718 [DecAlt_start] sys_go & DecAlt_go & DecAlt_state=0 &
719   DecAlt_applicable & ONE_LEVEL_ENABLED ->
720     (DecAlt_state'=DecAlt_LATENCY_PERIODS) &
721     (DecAlt_go'=false);
722 // Tactic applicable, but do not start it
723 [DecAlt_pass] sys_go & DecAlt_go & DecAlt_state=0 &
724   DecAlt_applicable -> (DecAlt_go'=false);
725 // Pass if the tactic is not applicable
726 [DecAlt_invalid] sys_go & DecAlt_go & DecAlt_state=0 &
727   !DecAlt_applicable -> 1 : (DecAlt_go'=false);
728 // Progress of the tactic
729 [DecAlt_progress] sys_go & DecAlt_go & DecAlt_state > 1 -> 1:
730   (DecAlt_state'=DecAlt_state-1) & (DecAlt_go'=false);
731 // Completion of the tactic
732 [DecAlt_complete] sys_go & DecAlt_go & DecAlt_state=1 -> 1:
733   (DecAlt_state'=0) & (DecAlt_go'=true);
734 [tick] !DecAlt_go -> 1: (DecAlt_go'=true);
735 endmodule
736
737 //*****// TACTIC: IncAlt2
738 //*****// TACTIC: IncAlt2
739 // Applicability conditions
740 formula IncAlt2_applicable = IncAlt2_compatible & a <
741   MAX_ALT_LEVEL-1;
742
743 module IncAlt2
744   IncAlt2_state : [0..IncAlt_LATENCY_PERIODS] init ini_IncAlt2_state;
745   IncAlt2_go : bool init true;
746
747 // Tactic applicable, start it
748 [IncAlt2_start] sys_go & IncAlt2_go & IncAlt2_state=0 &
749   IncAlt2_applicable & TWO_LEVEL_ENABLED ->
750     (IncAlt2_state'=IncAlt_LATENCY_PERIODS) &
751     (IncAlt2_go'=false);
752 // Pass if the tactic is not applicable
753 [IncAlt2_invalid] sys_go & IncAlt2_go & IncAlt2_state=0 &
754   !IncAlt2_applicable -> 1 : (IncAlt2_go'=false);
755 // Progress of the tactic
756 [IncAlt2_progress] sys_go & IncAlt2_go & IncAlt2_state > 1 -> 1:
757   (IncAlt2_state'=IncAlt2_state-1) & (IncAlt2_go'=false);
758 // Completion of the tactic
759 [IncAlt2_complete] sys_go & IncAlt2_go & IncAlt2_state=1 -> 1:
760   (IncAlt2_state'=0) & (IncAlt2_go'=true);
761 [tick] !IncAlt2_go -> 1: (IncAlt2_go'=true);
762 endmodule
763
764 //*****// TACTIC: DecAlt2
765 //*****// TACTIC: DecAlt2
766 //*****// TACTIC: DecAlt2
767 //*****// TACTIC: DecAlt2
768
769 const int DecAlt2_LATENCY_PERIODS = ceil(DecAlt_LATENCY/PERIOD);
770
771 // Applicability conditions
772 formula DecAlt2_applicable = DecAlt2_compatible & a > 1;
773
774 module DecAlt2
775   DecAlt2_state : [0..DecAlt2_LATENCY_PERIODS] init
776     ini_DecAlt2_state;
777   DecAlt2_go : bool init true;
778
779 // Tactic applicable, start it
780 [DecAlt2_start] sys_go & DecAlt2_go & DecAlt2_state=0 &
781   DecAlt2_applicable & TWO_LEVEL_ENABLED ->
782     (DecAlt2_state'=DecAlt2_LATENCY_PERIODS) &
783     (DecAlt2_go'=false);
784 // Tactic applicable, but do not start it
785 [DecAlt2_pass] sys_go & DecAlt2_go & DecAlt2_state=0 &
786   DecAlt2_applicable -> (DecAlt2_go'=false);
787 // Pass if the tactic is not applicable
788 [DecAlt2_invalid] sys_go & DecAlt2_go & DecAlt2_state=0 &
789   !DecAlt2_applicable -> 1 : (DecAlt2_go'=false);
790 // Progress of the tactic
791 [DecAlt2_progress] sys_go & DecAlt2_go & DecAlt2_state > 1 -> 1:
792   (DecAlt2_state'=DecAlt2_state-1) & (DecAlt2_go'=false);
793 // Completion of the tactic
794 [DecAlt2_complete] sys_go & DecAlt2_go & DecAlt2_state=1 -> 1:
795   (DecAlt2_state'=0) & (DecAlt2_go'=true);
796 [tick] !DecAlt2_go -> 1: (DecAlt2_go'=true);
797 endmodule
798
799 //*****// Utility Function
800 const int LOOSE = 0;
801 const int TIGHT = 1;
802 const int EMC_ON = 1;
803
804 formula probOfThreat = stateValue;
805
806 formula probabilityOfDestruction = probOfThreat
807   * ((f = LOOSE) ? 1.0 : (1.0 / destructionFormationFactor))
808   * ((c = EMC_ON) ? ecm_threat_prob : 1.0)
809   * max(0.0, threatRange - (a + 1)) / threatRange; // +1 because
810   // level 0 is one level above ground
811
812 module constraint // in this case the constraint is surviving
813   satisfied: bool init true;
814   [tick2] satisfied -> (1.0 - probabilityOfDestruction): (satisfied'=true)
815   + probabilityOfDestruction: (satisfied'=false);
816   [tick2] lsatisfied -> true;
817 endmodule
818
819 formula probOfTarget= stateValue1;

```

```

820
821 formula probOfDetection = probOfTarget
822   * ((f = LOOSE) ? 1.0 : (1.0 / detectionFormationFactor))
823   * ((c = EMC_ON) ? ecm_target_prob : 1.0)
824   * max(0.0, sensorRange - (a + 1)) / sensorRange; // +1 because level 0
825     is one level above ground
826
827 module sensor
828   targetDetected: bool init false;
829   [tack2] true -> probOfDetection: (targetDetected'=true) + (1.0 -
830     probOfDetection): (targetDetected'=false);
831 endmodule
832
833 rewards "util"
834   [tack] (time < HORIZON) & satisfied & targetDetected : 1;
835   [tack] (time = HORIZON) & satisfied : (targetDetected ? 1 : 0) +
836     survival_reward;
837
838 // give slight preference to not adapting
839 [tack] time = 0 & IncAlt_state=ini_IncAlt_state &
840   DecAlt_state=ini_DecAlt_state & a=init_a & f=init_f :
841   0.00000001;
842
843 endrewards

```

Listing 3. PRISM specification for short horizon MDP planning

*Long Horizon MDP Planning Specification:* To model uncertainty in targets and threats along a route, we adopt the approach suggested by Moreno et al. [35] since they also used the combination of DARTSim and MDP planning to evaluate their ideas. In short, two independent random variables are used in the environment state to represent the probabilities that a segment contains a target and a threat, respectively. Using the target and threat variables, we construct independent environment models for targets and threats, and then join them to produce a joint environment model, which is used by  $\rho_{mdps}$  and  $\rho_{mdpl}$ .

```

1 mdp
2 const double PERIOD = 60;
3 const int HORIZON = 5; // Planning horizon for deliberative planning
4 const double IncAlt_LATENCY = 60;
5 const double DecAlt_LATENCY = 60;
6 const int MAX_ALT_LEVEL = 3;
7 const double destructionFormationFactor = 1.5;
8 const double threatRange = 3;
9 const double detectionFormationFactor = 1.2;
10 const double sensorRange = 4;
11 const init_a = 0;
12 const init_c = 0;
13 const init_f = 0;
14 const bool ECM_ENABLED = true;
15 const bool ONE_LEVEL_ENABLED = true; // Unlike reactive planning, one
16   level increase/decrease altitude enabled
17 const bool TWO_LEVEL_ENABLED = true; // Two level increase/decrease
18   altitude also enabled
19 const int ini_IncAlt_state = 0;
20 const int ini_DecAlt_state = 0;
21 const int ini_IncAlt2_state = 0;
22 const int ini_DecAlt2_state = 0;
23 const double ecm_threat_prob = 0.15;
24 const double ecm_target_prob = 0.3;
25 const double survival_reward = 1;
26
27 //*****
28 // CLOCK
29 //*****
30 const int TO_TICK = 0;
31 const int TO_TICK2 = 1; // intermediate tick for constraint satisf. update
32 const int TO_TACK = 2;
33
34 label "final" = time = HORIZON & clockstep=TO_TICK;
35 formula sys_go = clockstep=TO_TICK;
36
37 module clk
38   time : [0..HORIZON] init 0;
39   clockstep : [0..2] init TO_TICK;
40   [tick] clockstep=TO_TICK & time < HORIZON -> 1: (time'=time+1) &
41     (clockstep'=TO_TICK2);
42   [tick2] clockstep=TO_TICK2 -> 1: (clockstep'=TO_TACK);
43   [tack] clockstep=TO_TACK -> 1: (clockstep'=TO_TICK);
44 endmodule
45
46 module env
47   s : [0..45] init 0;
48   [tick] s = 0 ->
49     0.034225 : (s' = 1)
50     + 0.11655 : (s' = 2)
51     + 0.034225 : (s' = 3)
52     + 0.11655 : (s' = 4)
53     + 0.3969 : (s' = 5)
54     + 0.11655 : (s' = 6)
55     + 0.034225 : (s' = 7)
56     + 0.11655 : (s' = 8)
57     + 0.034225 : (s' = 9);
58   [tick] s = 1 ->
59     0.034225 : (s' = 10)
60     + 0.11655 : (s' = 11)
61     + 0.034225 : (s' = 12)
62     + 0.11655 : (s' = 13)
63     + 0.3969 : (s' = 14)
64     + 0.11655 : (s' = 15)
65     + 0.034225 : (s' = 16)
66     + 0.11655 : (s' = 17)

```

```

66      + 0.034225 : (s' = 18);
67  [tick] s = 2 ->
68      0.034225 : (s' = 10)
69      + 0.11655 : (s' = 11)
70      + 0.034225 : (s' = 12)
71      + 0.11655 : (s' = 13)
72      + 0.3969 : (s' = 14)
73      + 0.11655 : (s' = 15)
74      + 0.034225 : (s' = 16)
75      + 0.11655 : (s' = 17)
76      + 0.034225 : (s' = 18);
77  [tick] s = 3 ->
78      0.034225 : (s' = 10)
79      + 0.11655 : (s' = 11)
80      + 0.034225 : (s' = 12)
81      + 0.11655 : (s' = 13)
82      + 0.3969 : (s' = 14)
83      + 0.11655 : (s' = 15)
84      + 0.034225 : (s' = 16)
85      + 0.11655 : (s' = 17)
86      + 0.034225 : (s' = 18);
87  [tick] s = 4 ->
88      0.034225 : (s' = 10)
89      + 0.11655 : (s' = 11)
90      + 0.034225 : (s' = 12)
91      + 0.11655 : (s' = 13)
92      + 0.3969 : (s' = 14)
93      + 0.11655 : (s' = 15)
94      + 0.034225 : (s' = 16)
95      + 0.11655 : (s' = 17)
96      + 0.034225 : (s' = 18);
97  [tick] s = 5 ->
98      0.034225 : (s' = 10)
99      + 0.11655 : (s' = 11)
100     + 0.034225 : (s' = 12)
101     + 0.11655 : (s' = 13)
102     + 0.3969 : (s' = 14)
103     + 0.11655 : (s' = 15)
104     + 0.034225 : (s' = 16)
105     + 0.11655 : (s' = 17)
106     + 0.034225 : (s' = 18);
107  [tick] s = 6 ->
108     0.034225 : (s' = 10)
109     + 0.11655 : (s' = 11)
110     + 0.034225 : (s' = 12)
111     + 0.11655 : (s' = 13)
112     + 0.3969 : (s' = 14)
113     + 0.11655 : (s' = 15)
114     + 0.034225 : (s' = 16)
115     + 0.11655 : (s' = 17)
116     + 0.034225 : (s' = 18);
117  [tick] s = 7 ->
118     0.034225 : (s' = 10)
119     + 0.11655 : (s' = 11)
120     + 0.034225 : (s' = 12)
121     + 0.11655 : (s' = 13)
122     + 0.3969 : (s' = 14)
123     + 0.11655 : (s' = 15)
124     + 0.034225 : (s' = 16)
125     + 0.11655 : (s' = 17)
126     + 0.034225 : (s' = 18);
127  [tick] s = 8 ->
128     0.034225 : (s' = 10)
129     + 0.11655 : (s' = 11)
130     + 0.034225 : (s' = 12)
131     + 0.11655 : (s' = 13)
132     + 0.3969 : (s' = 14)
133     + 0.11655 : (s' = 15)
134     + 0.034225 : (s' = 16)
135     + 0.11655 : (s' = 17)
136     + 0.034225 : (s' = 18);
137  [tick] s = 9 ->
138     0.034225 : (s' = 10)
139     + 0.11655 : (s' = 11)
140     + 0.034225 : (s' = 12)
141     + 0.11655 : (s' = 13)
142     + 0.3969 : (s' = 14)
143     + 0.11655 : (s' = 15)
144     + 0.034225 : (s' = 16)
145     + 0.11655 : (s' = 17)
146     + 0.034225 : (s' = 18);
147  [tick] s = 10 ->
148     0.034225 : (s' = 19)
149     + 0.11655 : (s' = 20)
150     + 0.034225 : (s' = 21)
151     + 0.11655 : (s' = 22)
152     + 0.3969 : (s' = 23)
153     + 0.11655 : (s' = 24)
154     + 0.034225 : (s' = 25)
155     + 0.11655 : (s' = 26)
156     + 0.034225 : (s' = 27);
157  [tick] s = 11 ->
158     0.034225 : (s' = 19)
159     + 0.11655 : (s' = 20)
160     + 0.034225 : (s' = 21)
161     + 0.11655 : (s' = 22)
162     + 0.3969 : (s' = 23)
163     + 0.11655 : (s' = 24)
164     + 0.034225 : (s' = 25)
165     + 0.11655 : (s' = 26)
166     + 0.034225 : (s' = 27);
167  [tick] s = 12 ->
168     0.034225 : (s' = 19)
169     + 0.11655 : (s' = 20)
170     + 0.034225 : (s' = 21)
171     + 0.11655 : (s' = 22)
172     + 0.3969 : (s' = 23)
173     + 0.11655 : (s' = 24)
174     + 0.034225 : (s' = 25)
175     + 0.11655 : (s' = 26)
176     + 0.034225 : (s' = 27);
177  [tick] s = 13 ->
178     0.034225 : (s' = 19)
179     + 0.11655 : (s' = 20)
180     + 0.034225 : (s' = 21)
181     + 0.11655 : (s' = 22)
182     + 0.3969 : (s' = 23)
183     + 0.11655 : (s' = 24)
184     + 0.034225 : (s' = 25)
185     + 0.11655 : (s' = 26)
186     + 0.034225 : (s' = 27);
187  [tick] s = 14 ->
188     0.034225 : (s' = 19)
189     + 0.11655 : (s' = 20)
190     + 0.034225 : (s' = 21)
191     + 0.11655 : (s' = 22)
192     + 0.3969 : (s' = 23)
193     + 0.11655 : (s' = 24)
194     + 0.034225 : (s' = 25)
195     + 0.11655 : (s' = 26)
196     + 0.034225 : (s' = 27);
197  [tick] s = 15 ->
198     0.034225 : (s' = 19)
199     + 0.11655 : (s' = 20)
200     + 0.034225 : (s' = 21)
201     + 0.11655 : (s' = 22)
202     + 0.3969 : (s' = 23)
203     + 0.11655 : (s' = 24)
204     + 0.034225 : (s' = 25)
205     + 0.11655 : (s' = 26)
206     + 0.034225 : (s' = 27);
207  [tick] s = 16 ->
208     0.034225 : (s' = 19)
209     + 0.11655 : (s' = 20)
210     + 0.034225 : (s' = 21)
211     + 0.11655 : (s' = 22)
212     + 0.3969 : (s' = 23)
213     + 0.11655 : (s' = 24)
214     + 0.034225 : (s' = 25)
215     + 0.11655 : (s' = 26)
216     + 0.034225 : (s' = 27);
217  [tick] s = 17 ->
218     0.034225 : (s' = 19)
219     + 0.11655 : (s' = 20)
220     + 0.034225 : (s' = 21)
221     + 0.11655 : (s' = 22)
222     + 0.3969 : (s' = 23)
223     + 0.11655 : (s' = 24)
224     + 0.034225 : (s' = 25)
225     + 0.11655 : (s' = 26)
226     + 0.034225 : (s' = 27);
227  [tick] s = 18 ->
228     0.034225 : (s' = 19)
229     + 0.11655 : (s' = 20)
230     + 0.034225 : (s' = 21)
231     + 0.11655 : (s' = 22)

```



```

398 0.034225 : (s' = 37)          (s = 13 ? 0 : 0) +
399 + 0.11655 : (s' = 38)          (s = 14 ? 0 : 0) +
400 + 0.034225 : (s' = 39)          (s = 15 ? 0 : 0) +
401 + 0.11655 : (s' = 40)          (s = 16 ? 0 : 0) +
402 + 0.3969 : (s' = 41)          (s = 17 ? 0 : 0) +
403 + 0.11655 : (s' = 42)          (s = 18 ? 0 : 0) +
404 + 0.034225 : (s' = 43)          (s = 19 ? 0.0156741 : 0) +
405 + 0.11655 : (s' = 44)          (s = 20 ? 0.0719057 : 0) +
406 + 0.034225 : (s' = 45);      (s = 21 ? 0.190204 : 0) +
407 [tick] s = 36 ->           (s = 22 ? 0.0156741 : 0) +
408 0.034225 : (s' = 37)          (s = 23 ? 0.0719057 : 0) +
409 + 0.11655 : (s' = 38)          (s = 24 ? 0.190204 : 0) +
410 + 0.034225 : (s' = 39)          (s = 25 ? 0.0156741 : 0) +
411 + 0.11655 : (s' = 40)          (s = 26 ? 0.0719057 : 0) +
412 + 0.3969 : (s' = 41)          (s = 27 ? 0.190204 : 0) +
413 + 0.11655 : (s' = 42)          (s = 28 ? 0 : 0) +
414 + 0.034225 : (s' = 43)          (s = 29 ? 0 : 0) +
415 + 0.11655 : (s' = 44)          (s = 30 ? 0 : 0) +
416 + 0.034225 : (s' = 45);      (s = 31 ? 0 : 0) +
417 endmodule                   (s = 32 ? 0 : 0) +
418 // environment has 2 components. stateValue for threats and statevalue1 is
419 // for targets
420 formula stateValue = (s = 0 ? 0 : 0) +
421           (s = 1 ? 0.00605639 : 0) +
422           (s = 2 ? 0.00605639 : 0) +
423           (s = 3 ? 0.00605639 : 0) +
424           (s = 4 ? 0.0282836 : 0) +
425           (s = 5 ? 0.0282836 : 0) +
426           (s = 6 ? 0.0282836 : 0) +
427           (s = 7 ? 0.0778979 : 0) +
428           (s = 8 ? 0.0778979 : 0) +
429           (s = 9 ? 0.0778979 : 0) +
430           (s = 10 ? 0 : 0) +
431           (s = 11 ? 0 : 0) +
432           (s = 12 ? 0 : 0) +
433           (s = 13 ? 0 : 0) +
434           (s = 14 ? 0 : 0) +
435           (s = 15 ? 0 : 0) +
436           (s = 16 ? 0 : 0) +
437           (s = 17 ? 0 : 0) +
438           (s = 18 ? 0 : 0) +
439           (s = 19 ? 0.750751 : 0) +
440           (s = 20 ? 0.750751 : 0) +
441           (s = 21 ? 0.750751 : 0) +
442           (s = 22 ? 0.885424 : 0) +
443           (s = 23 ? 0.885424 : 0) +
444           (s = 24 ? 0.885424 : 0) +
445           (s = 25 ? 0.963485 : 0) +
446           (s = 26 ? 0.963485 : 0) +
447           (s = 27 ? 0.963485 : 0) +
448           (s = 28 ? 0.435626 : 0) +
449           (s = 29 ? 0.435626 : 0) +
450           (s = 30 ? 0.435626 : 0) +
451           (s = 31 ? 0.676196 : 0) +
452           (s = 32 ? 0.676196 : 0) +
453           (s = 33 ? 0.676196 : 0) +
454           (s = 34 ? 0.864925 : 0) +
455           (s = 35 ? 0.864925 : 0) +
456           (s = 36 ? 0.864925 : 0) +
457           (s = 37 ? 0.368403 : 0) +
458           (s = 38 ? 0.368403 : 0) +
459           (s = 39 ? 0.368403 : 0) +
460           (s = 40 ? 0.793701 : 0) +
461           (s = 41 ? 0.793701 : 0) +
462           (s = 42 ? 0.793701 : 0) +
463           (s = 43 ? 0.983048 : 0) +
464           (s = 44 ? 0.983048 : 0) +
465           (s = 45 ? 0.983048 : 0);
466
467 formula stateValue1 = (s = 0 ? 0 : 0) +
468           (s = 1 ? 0.830037 : 0) +
469           (s = 2 ? 0.904439 : 0) +
470           (s = 3 ? 0.954777 : 0) +
471           (s = 4 ? 0.830037 : 0) +
472           (s = 5 ? 0.904439 : 0) +
473           (s = 6 ? 0.954777 : 0) +
474           (s = 7 ? 0.830037 : 0) +
475           (s = 8 ? 0.904439 : 0) +
476           (s = 9 ? 0.954777 : 0) +
477           (s = 10 ? 0 : 0) +
478           (s = 11 ? 0 : 0) +
479           (s = 12 ? 0 : 0) +
480
481           (s = 13 ? 0 : 0) +
482           (s = 14 ? 0 : 0) +
483           (s = 15 ? 0 : 0) +
484           (s = 16 ? 0 : 0) +
485           (s = 17 ? 0 : 0) +
486           (s = 18 ? 0 : 0) +
487           (s = 19 ? 0.0156741 : 0) +
488           (s = 20 ? 0.0719057 : 0) +
489           (s = 21 ? 0.190204 : 0) +
490           (s = 22 ? 0.0156741 : 0) +
491           (s = 23 ? 0.0719057 : 0) +
492           (s = 24 ? 0.190204 : 0) +
493           (s = 25 ? 0.0156741 : 0) +
494           (s = 26 ? 0.0719057 : 0) +
495           (s = 27 ? 0.190204 : 0) +
496           (s = 28 ? 0 : 0) +
497           (s = 29 ? 0 : 0) +
498           (s = 30 ? 0 : 0) +
499           (s = 31 ? 0 : 0) +
500           (s = 32 ? 0 : 0) +
501           (s = 33 ? 0 : 0) +
502           (s = 34 ? 0 : 0) +
503           (s = 35 ? 0 : 0) +
504           (s = 36 ? 0 : 0) +
505           (s = 37 ? 0 : 0) +
506           (s = 38 ? 0 : 0) +
507           (s = 39 ? 0 : 0) +
508           (s = 40 ? 0 : 0) +
509           (s = 41 ? 0 : 0) +
510           (s = 42 ? 0 : 0) +
511           (s = 43 ? 0 : 0) +
512           (s = 44 ? 0 : 0) +
513           (s = 45 ? 0 : 0);
514
515 // #ENV ENDS
516 //***** SYSTEM *****
517 // SYSTEM
518 //*****
519 // Variable range and initialization
520 const a_MIN=0; const a_MAX=MAX_ALT_LEVEL; const a_INIT=init_a;
521 const f_MIN=0; const f_MAX=1; const f_INIT=init_f;
522 const c_MIN=0; const c_MAX=1; const c_INIT=init_c;
523
524 module sys
525   a : [a_MIN..a_MAX] init a_INIT;
526   f : [f_MIN..f_MAX] init f_INIT;
527   c : [c_MIN..c_MAX] init c_INIT;
528
529   [EcmOn_start] c=0 & ECM_ENABLED -> 1: (c'=c_EcmOn_impact);
530   [EcmOff_start] c=1 & ECM_ENABLED -> 1: (c'=c_EcmOff_impact);
531
532   [GoTight_start] f=0 -> 1: (a'=a_GoTight_impact)
533     & (f'=f_GoTight_impact);
534   [GoLoose_start] f=1 -> 1: (a'=a_GoLoose_impact)
535     & (f'=f_GoLoose_impact);
536
537   [IncAlt_complete] a < MAX_ALT_LEVEL & ONE_LEVEL_ENABLED ->
538     1: (a'=a_IncAlt_impact)
539     & (f'=f_IncAlt_impact);
540   [IncAlt2_complete] a < MAX_ALT_LEVEL-1 &
541     TWO_LEVEL_ENABLED -> 1: (a'=a_IncAlt2_impact);
542
543   [DecAlt_complete] a > 0 & ONE_LEVEL_ENABLED -> 1:
544     (a'=a_DecAlt_impact)
545     & (f'=f_DecAlt_impact);
546   [DecAlt2_complete] a > 1 & TWO_LEVEL_ENABLED -> 1:
547     (a'=a_DecAlt2_impact);
548
549 endmodule
550
551 formula c_EcmOn_impact = c + (1) >= c_MIN ? (c+(1)<=c_MAX? c+(1):
552   c_MAX) : c_MIN;
553 formula c_EcmOff_impact = c + (-1) >= c_MIN ? (c+(-1)<=c_MAX?
554   c+(-1) : c_MAX) : c_MIN;
555 formula a_GoTight_impact = a + (0) >= a_MIN ? (a+(0)<=a_MAX? a+(0):
556   a_MAX) : a_MIN;
557 formula f_GoTight_impact = f + (1) >= f_MIN ? (f+(1)<=f_MAX? f+(1):
558   f_MAX) : f_MIN;
559 formula a_GoLoose_impact = a + (0) >= a_MIN ? (a+(0)<=a_MAX? a+(0):
560   a_MAX) : a_MIN;
561 formula f_GoLoose_impact = f + (-1) >= f_MIN ? (f+(-1)<=f_MAX? f+(-1)

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554   : f_MAX) : f_MIN;
555 formula a_IncAlt_impact = a + (1) >= a_MIN ? ( a+(1)<=a_MAX? a+(1) :
556   a_MAX) : a_MIN;
557 formula f_IncAlt_impact = f + (0) >= f_MIN ? ( f+(0)<=f_MAX? f+(0) :
558   f_MAX) : f_MIN;
559 formula a_DecAlt_impact = a + (-1) >= a_MIN ? ( a+(-1)<=a_MAX?
560   a+(-1) : a_MAX) : a_MIN;
561 formula f_DecAlt_impact = f + (0) >= f_MIN ? ( f+(0)<=f_MAX? f+(0) :
562   f_MAX) : f_MIN;
563 formula a_IncAlt2_impact = a + (2) >= a_MIN ? ( a+(2)<=a_MAX? a+(2) :
564   a_MAX) : a_MIN;
565 formula a_DecAlt2_impact = a + (-2) >= a_MIN ? ( a+(-2)<=a_MAX?
566   a+(-2) : a_MAX) : a_MIN;
567 // tactic concurrency rules
568 formula IncAlt_used = IncAlt_state != 0;
569 formula DecAlt_used = DecAlt_state != 0;
570 formula IncAlt2_used = IncAlt2_state != 0;
571 formula DecAlt2_used = DecAlt2_state != 0;
572 formula EcmOn_compatible = !EcmOn_used;
573 formula EcmOff_compatible = !EcmOff_used;
574 formula GoTight_compatible = !GoLoose_used;
575 formula GoLoose_compatible = !GoTight_used;
576 formula IncAlt_compatible = (!DecAlt_used) & (!IncAlt2_used) &
577   (!DecAlt2_used);
578 formula DecAlt_compatible = (!IncAlt_used) & (!IncAlt2_used) &
579   (!DecAlt2_used);
580 formula IncAlt2_compatible = (!DecAlt_used) & (!IncAlt_used) &
581   (!DecAlt2_used);
582 formula DecAlt2_compatible = (!DecAlt_used) & (!IncAlt_used) &
583   (!IncAlt2_used);

584 //*****// TACTIC: EcmOn
585 //*****// Applicability conditions
586 formula EcmOn_applicable = EcmOn_compatible & c=0;
587 module EcmOn
588   EcmOn_used : bool init false;
589   EcmOn_go : bool init true;
590   // Tactic applicable, start it
591   [EcmOn_start] sys_go & EcmOn_go & EcmOn_applicable &
592     ECM_ENABLED -> (EcmOn_used'=true) & (EcmOn_go'=false);
593   // Tactic applicable, but do not start it
594   [EcmOn_pass] sys_go & EcmOn_go & EcmOn_applicable ->
595     (EcmOn_go=false);
596   // Pass if the tactic is not applicable
597   [EcmOn_invalid] sys_go & EcmOn_go & !EcmOn_applicable -> 1 :
598     (EcmOn_go=false);
599   [tick] !EcmOn_go -> 1: (EcmOn_go'=true) & (EcmOn_used=false);
600 endmodule

601 //*****// TACTIC: EcmOff
602 //*****// Applicability conditions
603 formula EcmOff_applicable = EcmOff_compatible & c=1;
604 module EcmOff
605   EcmOff_used : bool init false;
606   EcmOff_go : bool init true;
607   // Tactic applicable, start it
608   [EcmOff_start] sys_go & EcmOff_go & EcmOff_applicable &
609     ECM_ENABLED -> (EcmOff_used'=true) & (EcmOff_go=false);
610   // Tactic applicable, but do not start it
611   [EcmOff_pass] sys_go & EcmOff_go & EcmOff_applicable ->
612     (EcmOff_go=false);
613   // Pass if the tactic is not applicable
614   [EcmOff_invalid] sys_go & EcmOff_go & !EcmOff_applicable -> 1 :
615     (EcmOff_go=false);

616   [tick] !EcmOff_go -> 1: (EcmOff_go'=true) & (EcmOff_used=false);
617 endmodule

618 //*****// TACTIC: GoTight
619 //*****// Applicability conditions
620   [tick] !EcmOff_go -> 1: (EcmOff_go'=true) & (EcmOff_used=false);
621 endmodule
622 //*****// TACTIC: GoTight
623 //*****// Applicability conditions
624 formula GoTight_applicable = GoTight_compatible & f=0;
625 module GoTight
626   GoTight_used : bool init false;
627   GoTight_go : bool init true;
628   // Tactic applicable, start it
629   [GoTight_start] sys_go & GoTight_go & GoTight_applicable ->
630     (GoTight_used'=true) & (GoTight_go=false);
631   // Tactic applicable, but do not start it
632   [GoTight_pass] sys_go & GoTight_go & GoTight_applicable ->
633     (GoTight_go=false);
634   // Pass if the tactic is not applicable
635   [GoTight_invalid] sys_go & GoTight_go & !GoTight_applicable -> 1 :
636     (GoTight_go=false);
637   [tick] !GoTight_go -> 1: (GoTight_go'=true) & (GoTight_used=false);
638 endmodule
639 //*****// TACTIC: GoLoose
640 //*****// Applicability conditions
641 formula GoLoose_applicable = GoLoose_compatible & f=1;
642 module GoLoose
643   GoLoose_used : bool init false;
644   GoLoose_go : bool init true;
645   // Tactic applicable, start it
646   [GoLoose_start] sys_go & GoLoose_go & GoLoose_applicable ->
647     (GoLoose_used'=true) & (GoLoose_go=false);
648   // Tactic applicable, but do not start it
649   [GoLoose_pass] sys_go & GoLoose_go & GoLoose_applicable ->
650     (GoLoose_go=false);
651   // Pass if the tactic is not applicable
652   [GoLoose_invalid] sys_go & GoLoose_go & !GoLoose_applicable -> 1 :
653     (GoLoose_go=false);
654   [tick] !GoLoose_go -> 1: (GoLoose_go'=true) &
655     (GoLoose_used=false);
656 endmodule
657 //*****// TACTIC: IncAlt
658 //*****// Applicability conditions
659 const int IncAlt_LATENCY_PERIODS = ceil(IncAlt_LATENCY/PERIOD);
660 formula IncAlt_applicable = IncAlt_compatible & a < MAX_ALT_LEVEL;
661 module IncAlt
662   IncAlt_state : [0..IncAlt_LATENCY_PERIODS] init ini_IncAlt_state;
663   IncAlt_go : bool init true;
664   // Tactic applicable, start it
665   [IncAlt_start] sys_go & IncAlt_go & IncAlt_state=0 & IncAlt_applicable &
666     ONE_LEVEL_ENABLED ->
667       (IncAlt_state'=IncAlt_LATENCY_PERIODS) & (IncAlt_go=false);
668   // Tactic applicable, but do not start it
669   [IncAlt_pass] sys_go & IncAlt_go & IncAlt_state=0 & IncAlt_applicable
670     -> (IncAlt_go=false);
671   // Pass if the tactic is not applicable
672 
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```

693 [IncAlt_invalid] sys_go & IncAlt_go & IncAlt_state=0 & !IncAlt_applicable  

694     -> 1 : (IncAlt_go'=false);  

695  

696 // Progress of the tactic  

697 [IncAlt_progress] sys_go & IncAlt_go & IncAlt_state > 1 -> 1:  

698     (IncAlt_state'=IncAlt_state-1) & (IncAlt_go'=false);  

699  

700 // Completion of the tactic  

701 [IncAlt_complete] sys_go & IncAlt_go & IncAlt_state=1 -> 1:  

702     (IncAlt_state'=0) & (IncAlt_go'=true);  

703  

704 [tick] !IncAlt_go -> 1: (IncAlt_go'=true);  

705 endmodule  

706  

707 //*****  

708 // TACTIC: DecAlt  

709 //*****  

710  

711 const int DecAlt_LATENCY_PERIODS = ceil(DecAlt_LATENCY/PERIOD);  

712  

713 // Applicability conditions  

714 formula DecAlt_applicable = DecAlt_compatible & a > 0;  

715  

716 module DecAlt  

717     DecAlt_state : [0..DecAlt_LATENCY_PERIODS] init ini_DecAlt_state;  

718     DecAlt_go : bool init true;  

719  

720 // Tactic applicable, start it  

721 [DecAlt_start] sys_go & DecAlt_go & DecAlt_state=0 &  

722     DecAlt_applicable & ONE_LEVEL_ENABLED ->  

723     (DecAlt_state=DecAlt_LATENCY_PERIODS) &  

724     (DecAlt_go'=false);  

725  

726 // Tactic applicable, but do not start it  

727 [DecAlt_pass] sys_go & DecAlt_go & DecAlt_state=0 &  

728     DecAlt_applicable -> (DecAlt_go'=false);  

729  

730 // Pass if the tactic is not applicable  

731 [DecAlt_invalid] sys_go & DecAlt_go & DecAlt_state=0 &  

732     !DecAlt_applicable -> 1 : (DecAlt_go'=false);  

733  

734 // Progress of the tactic  

735 [DecAlt_progress] sys_go & DecAlt_go & DecAlt_state > 1 -> 1:  

736     (DecAlt_state'=DecAlt_state-1) & (DecAlt_go'=false);  

737  

738 // Completion of the tactic  

739 [DecAlt_complete] sys_go & DecAlt_go & DecAlt_state=1 -> 1:  

740     (DecAlt_state'=0) & (DecAlt_go'=true);  

741  

742 [tick] !DecAlt_go -> 1: (DecAlt_go'=true);  

743 endmodule  

744  

745 //*****  

746 // TACTIC: IncAlt2  

747 //*****  

748  

749 // Applicability conditions  

750 formula IncAlt2_applicable = IncAlt2_compatible & a <  

751     MAX_ALT_LEVEL-1;  

752  

753 module IncAlt2  

754     IncAlt2_state : [0..IncAlt2_LATENCY_PERIODS] init ini_IncAlt2_state;  

755     IncAlt2_go : bool init true;  

756  

757 // Tactic applicable, start it  

758 [IncAlt2_start] sys_go & IncAlt2_go & IncAlt2_state=0 &  

759     IncAlt2_applicable & TWO_LEVEL_ENABLED ->  

760     (IncAlt2_state'=IncAlt2_LATENCY_PERIODS) &  

761     (IncAlt2_go'=false);  

762  

763 // Tactic applicable, but do not start it  

764 [IncAlt2_pass] sys_go & IncAlt2_go & IncAlt2_state=0 &  

765     IncAlt2_applicable -> (IncAlt2_go'=false);  

766  

767 // Pass if the tactic is not applicable  

768 [IncAlt2_invalid] sys_go & IncAlt2_go & IncAlt2_state=0 &  

769     !IncAlt2_applicable -> 1 : (IncAlt2_go'=false);  

770  

771 // Progress of the tactic  

772 [IncAlt2_progress] sys_go & IncAlt2_go & IncAlt2_state > 1 -> 1:  

773     (IncAlt2_state'=IncAlt2_state-1) & (IncAlt2_go'=false);  

774  

775 // Completion of the tactic  

776 [IncAlt2_complete] sys_go & IncAlt2_go & IncAlt2_state=1 -> 1:  

777     (IncAlt2_state'=0) & (IncAlt2_go'=true);  

778  

779 // Applicability conditions  

780 formula DecAlt2_applicable = DecAlt2_compatible & a > 1;  

781  

782 module DecAlt2  

783     DecAlt2_state : [0..DecAlt2_LATENCY_PERIODS] init  

784         ini_DecAlt2_state;  

785     DecAlt2_go : bool init true;  

786  

787 // Tactic applicable, start it  

788 [DecAlt2_start] sys_go & DecAlt2_go & DecAlt2_state=0 &  

789     DecAlt2_applicable & TWO_LEVEL_ENABLED ->  

790     (DecAlt2_state=DecAlt2_LATENCY_PERIODS) &  

791     (DecAlt2_go'=false);  

792  

793 // Tactic applicable, but do not start it  

794 [DecAlt2_pass] sys_go & DecAlt2_go & DecAlt2_state=0 &  

795     DecAlt2_applicable -> (DecAlt2_go'=false);  

796  

797 // Pass if the tactic is not applicable  

798 [DecAlt2_invalid] sys_go & DecAlt2_go & DecAlt2_state=0 &  

799     !DecAlt2_applicable -> 1 : (DecAlt2_go'=false);  

800  

801 // Progress of the tactic  

802 [DecAlt2_progress] sys_go & DecAlt2_go & DecAlt2_state > 1 -> 1:  

803     (DecAlt2_state'=DecAlt2_state-1) & (DecAlt2_go'=false);  

804  

805 // Completion of the tactic  

806 [DecAlt2_complete] sys_go & DecAlt2_go & DecAlt2_state=1 -> 1:  

807     (DecAlt2_state'=0) & (DecAlt2_go'=true);  

808  

809 [tick] !DecAlt2_go -> 1: (DecAlt2_go'=true);  

810 endmodule  

811  

812 //*****  

813 // Utility Function  

814 //*****  

815 const int LOOSE = 0;  

816 const int TIGHT = 1;  

817 const int EMC_ON = 1;  

818  

819 formula probOfThreat = stateValue;  

820  

821 formula probabilityOfDestruction = probOfThreat  

822     * ((f = LOOSE) ? 1.0 : (1.0 / destructionFormationFactor))  

823     * ((c = EMC_ON) ? ecm_threat_prob : 1.0)  

824     * max(0.0, threatRange - (a + 1)) / threatRange; // +1 because  

825     level 0 is one level above ground  

826  

827 module constraint // in this case the constraint is surviving  

828     satisfied: bool init true;  

829     [tick2] satisfied -> (1.0 - probabilityOfDestruction): (satisfied'=true)  

830         + probabilityOfDestruction: (satisfied'=false);  

831     [tick2] satisfied -> true;  

832 endmodule  

833  

834  

835 formula probOfTarget= stateValue1;  

836  

837 formula probOfDetection = probOfTarget  

838     * ((f = LOOSE) ? 1.0 : (1.0 / detectionFormationFactor))  

839     * ((c = EMC_ON) ? ecm_target_prob : 1.0)  

840     * max(0.0, sensorRange - (a + 1)) / sensorRange; // +1 because level 0  

841     is one level above ground  

842  

843 module sensor  

844     targetDetected: bool init false;  

845     [tick2] true -> probOfDetection: (targetDetected'=true) + (1.0 -  

846         probOfDetection): (targetDetected'=false);  

847

```

```

830 endmodule
831
832 rewards "util"
833   //[[tack] satisfied & targetDetected : 1;
834
835   [tack] (time < HORIZON) & satisfied & targetDetected : 1;
836   [tack] (time = HORIZON) & satisfied : (targetDetected ? 1 : 0) +
837     survival_reward;
838
839   // give slight preference to not adapting
840   [tick] time = 0 & IncAlt_state=ini_IncAlt_state &
841     DecAlt_state=ini_DecAlt_state & a=init_a & f=init_f :
842     0.000000001;
843
endrewards

```

Listing 4. PRISM specification for long horizon MDP planning

## VI. MATERIALS FOR TRACE PATTERNS

*Q: What Are the Load Patterns for the Cloud-based System?*

To construct a realistic environment of users accessing the cloud-based system, we used a research dataset with online traffic common in web analytics — the daily traces of user requests from the FIFA-98 WorldCup website. These traces are independent day-by-day recordings of user website activity during the championship, with rapid load changes and periods of low variation. We picked these traces because they contain the patterns for high-demand cloud systems. As shown in Figure 2.

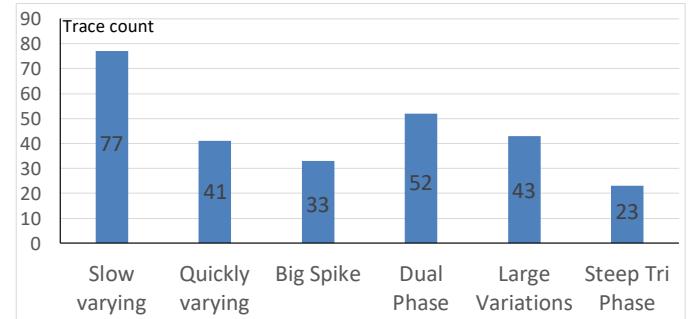
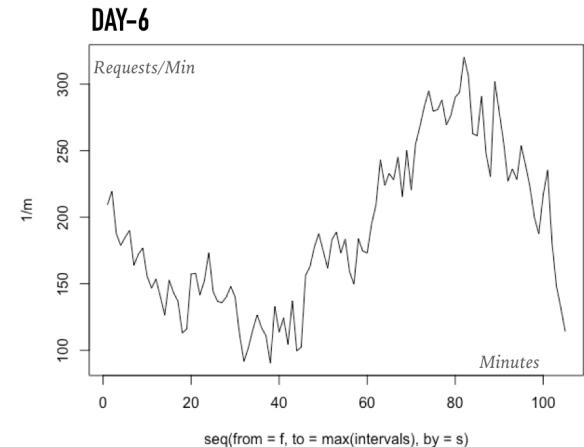


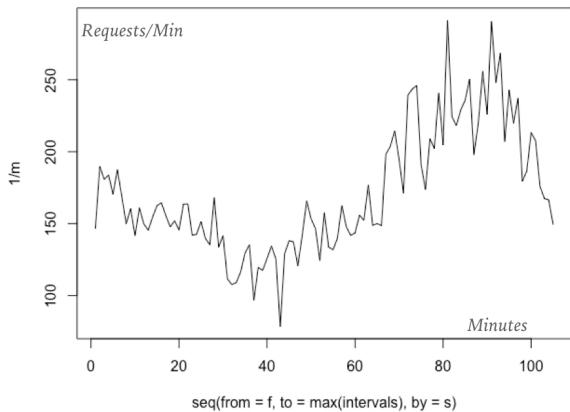
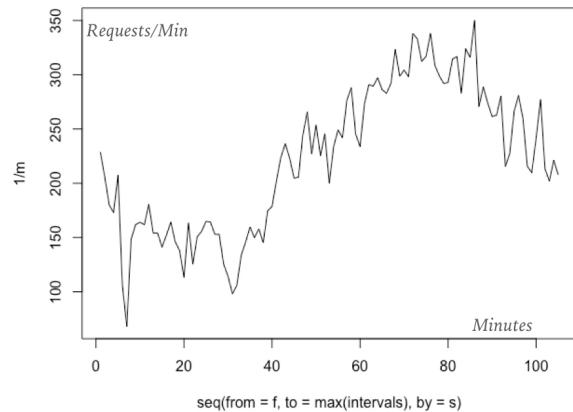
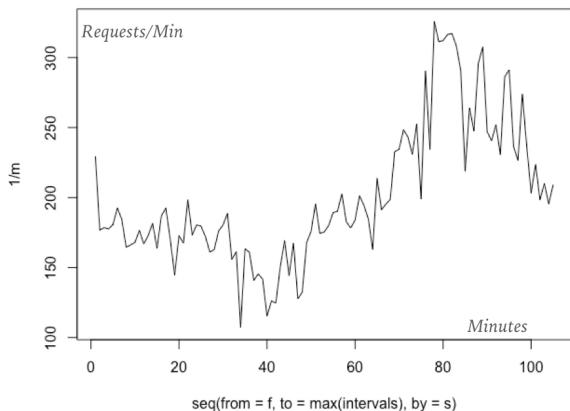
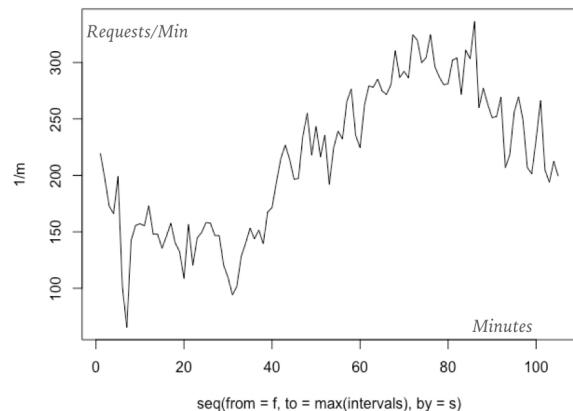
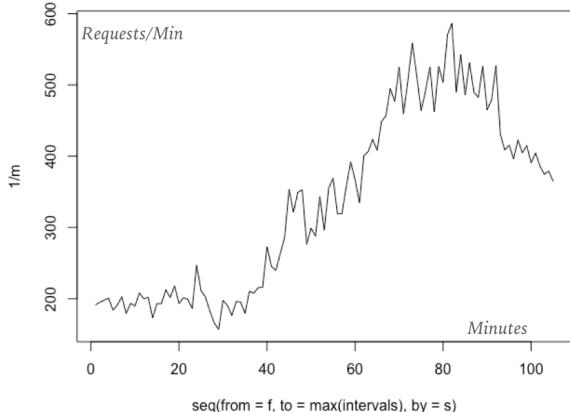
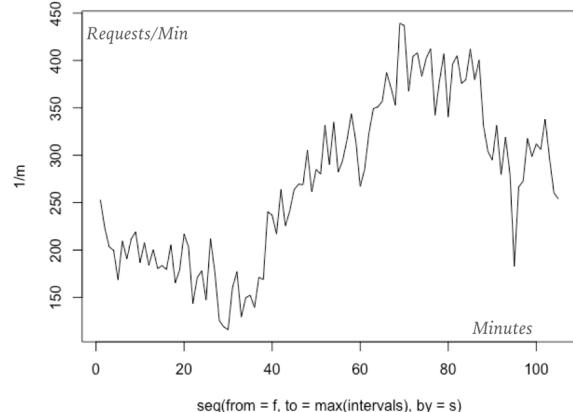
Figure 2. Patterns observed in traces. A single trace can have multiple patterns.

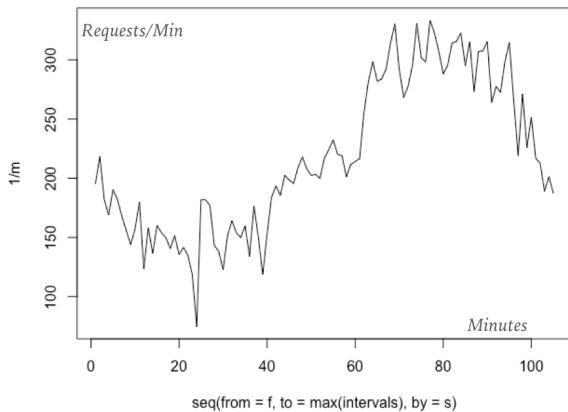
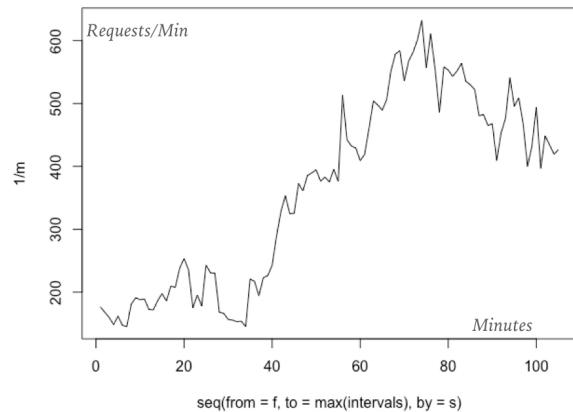
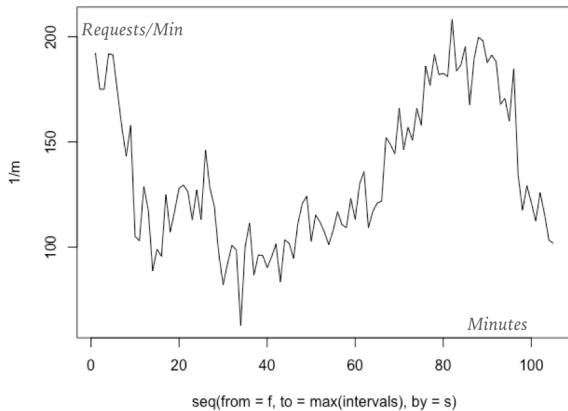
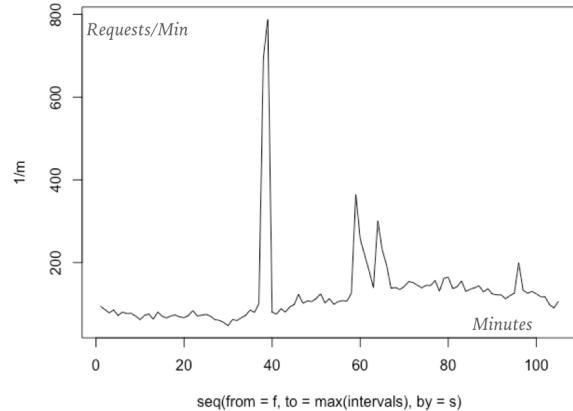
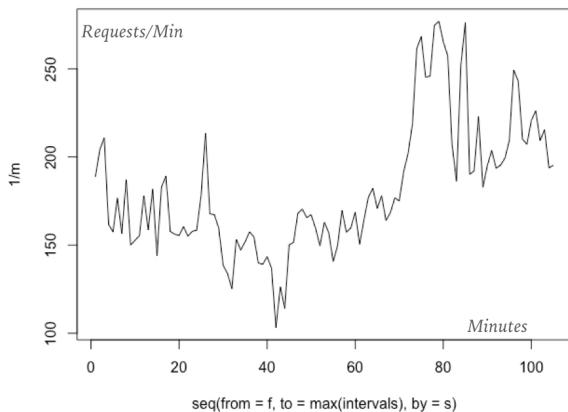
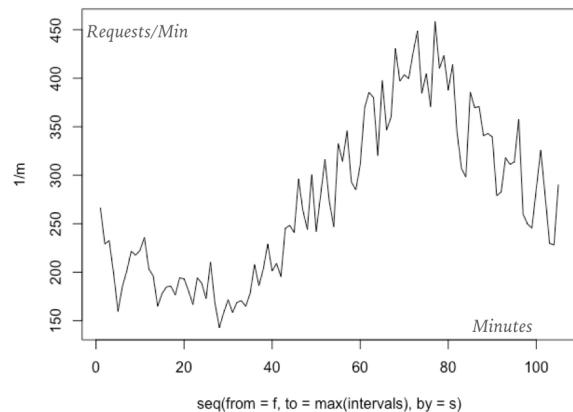
Total traces were 92 but 5 were incomplete/corrupted. Therefore, we used 87 traces for validation. Each trace is scaled such that

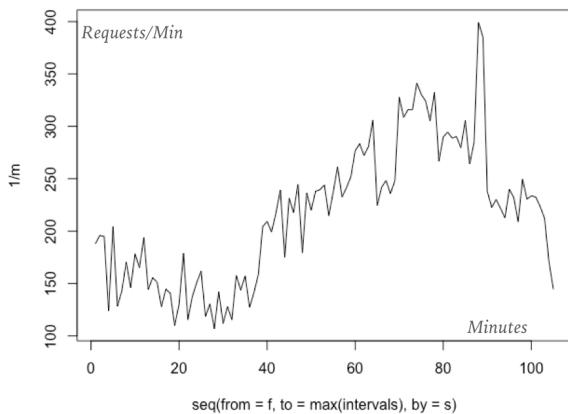
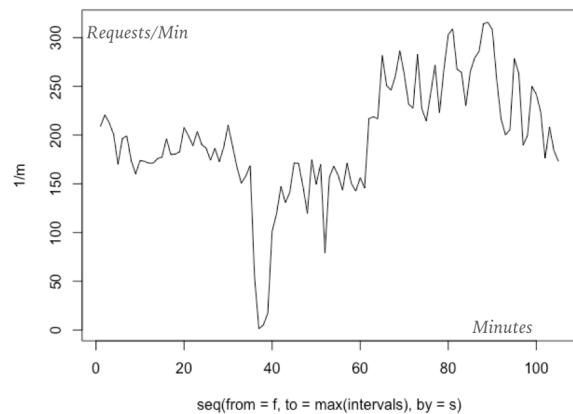
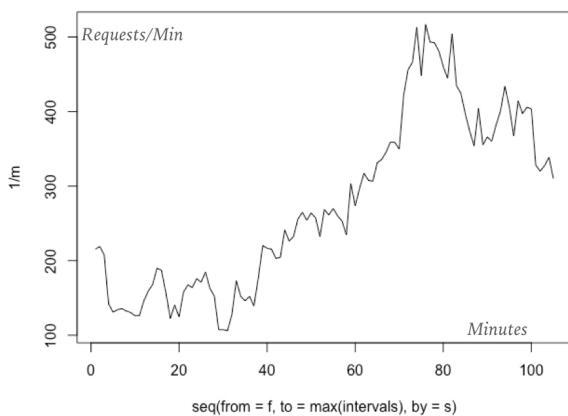
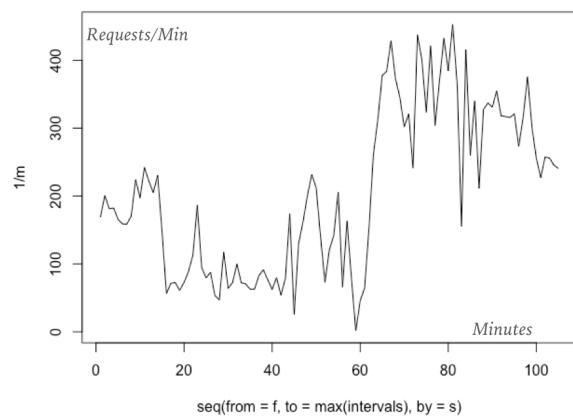
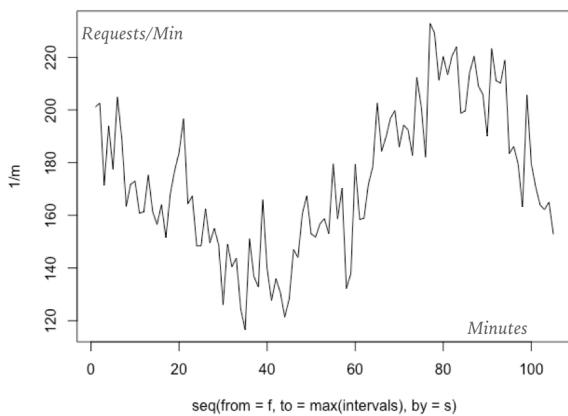
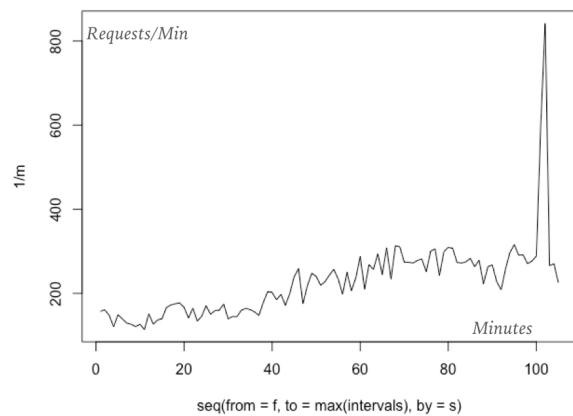
- duration is 105 minutes;
- starting request arrival rate is about 200 requests/min since active servers beginning of a simulation can server 200 requests/min. If workload goes beyond the capacity, the queueing model does not work;
- similarly, the highest workload is about 800, which is 90% of the total capacity (including all available servers with no optional content) of the system.

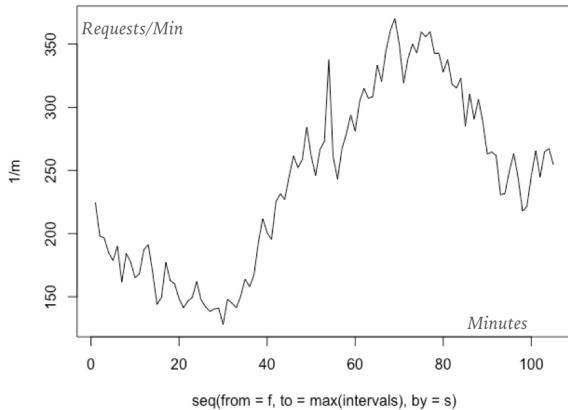
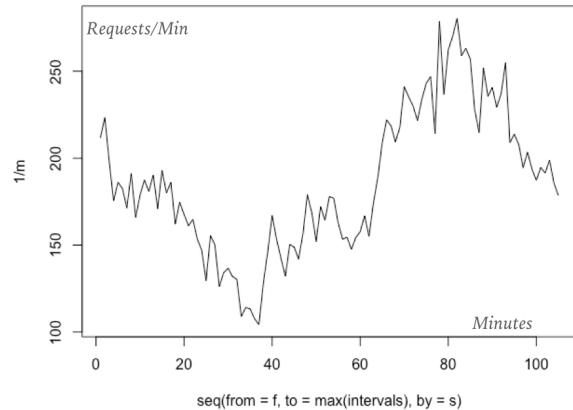
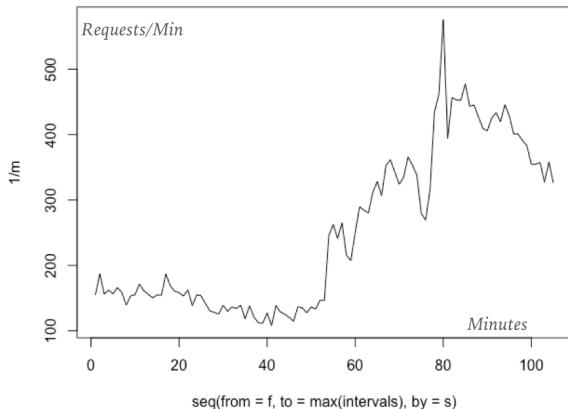
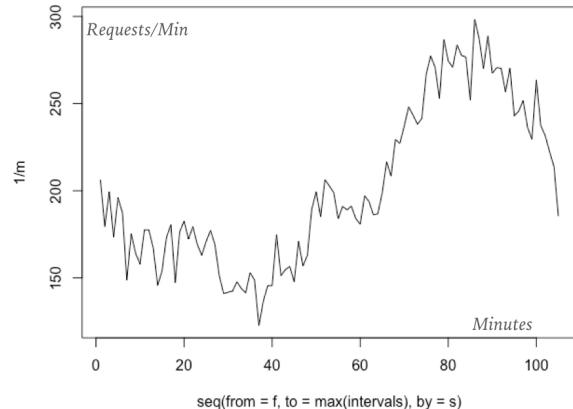
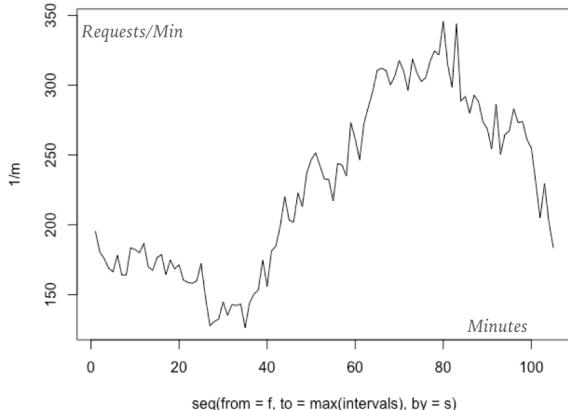
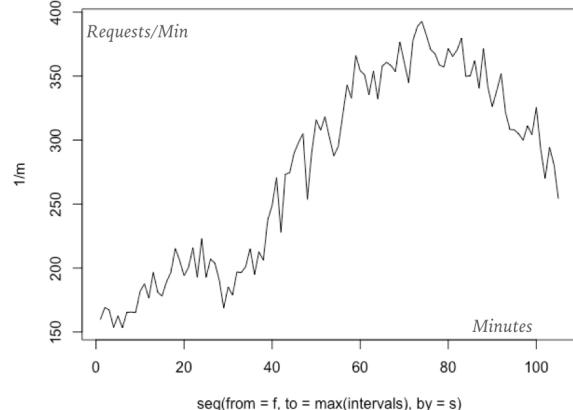
Below are the visualizations of load patterns for each day.

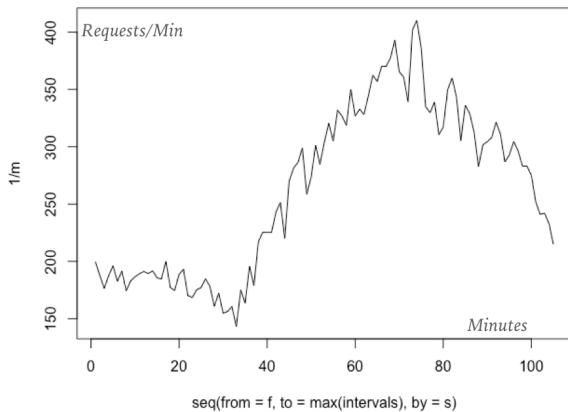
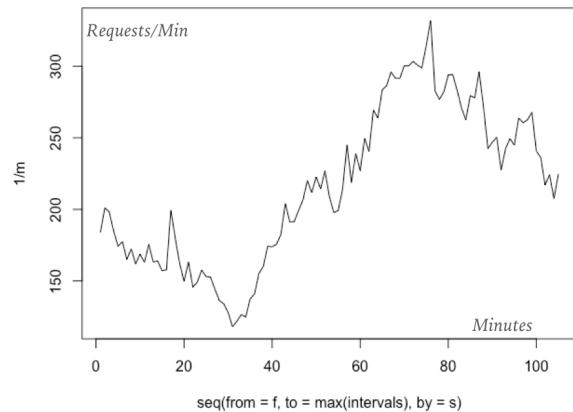
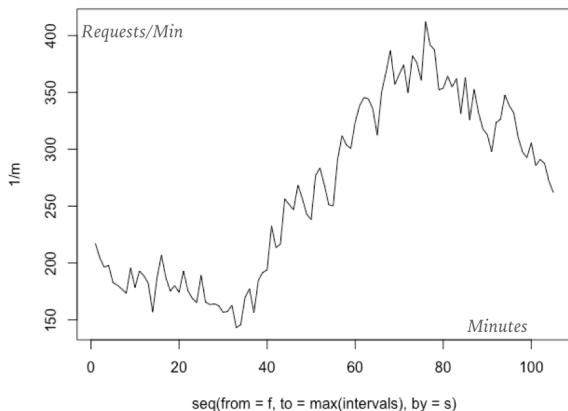
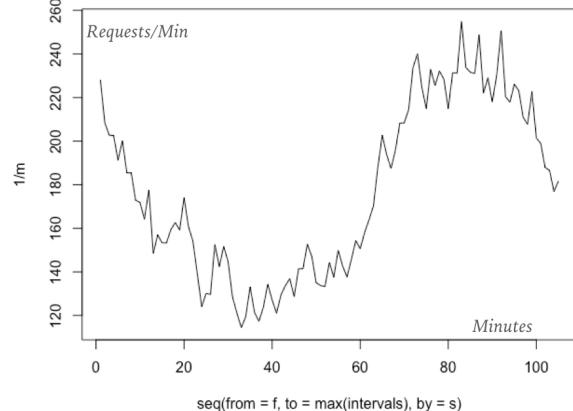
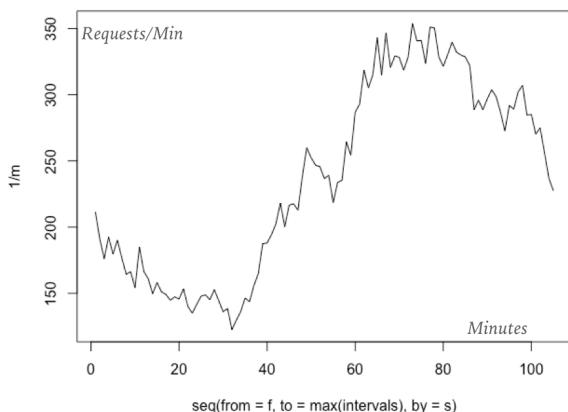
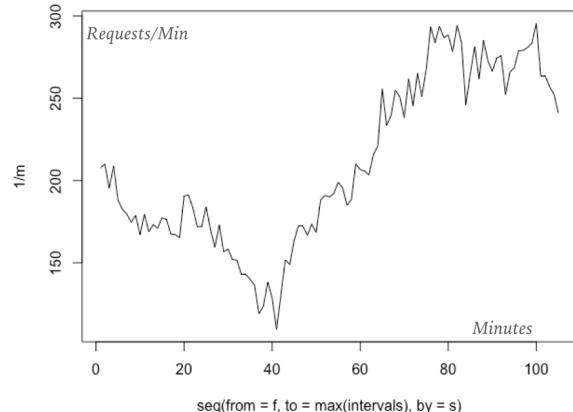


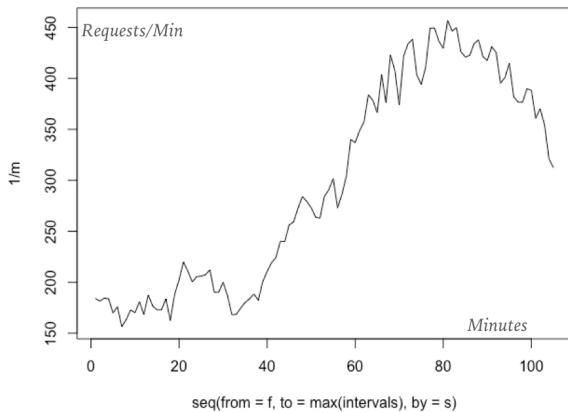
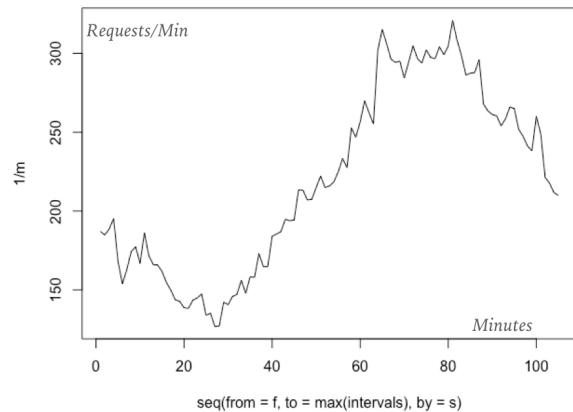
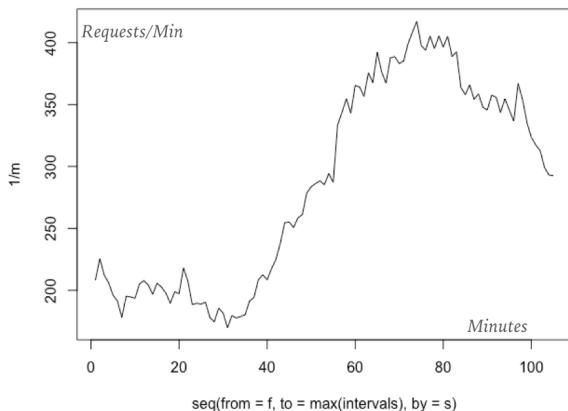
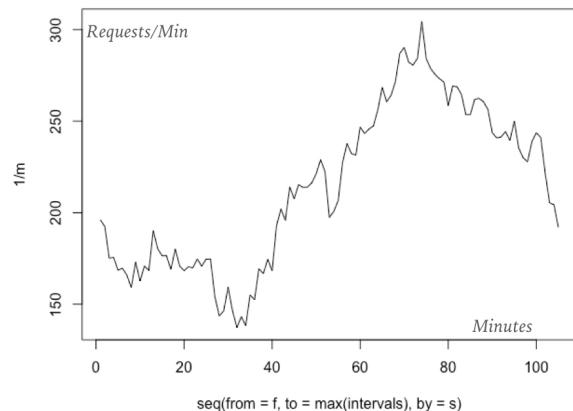
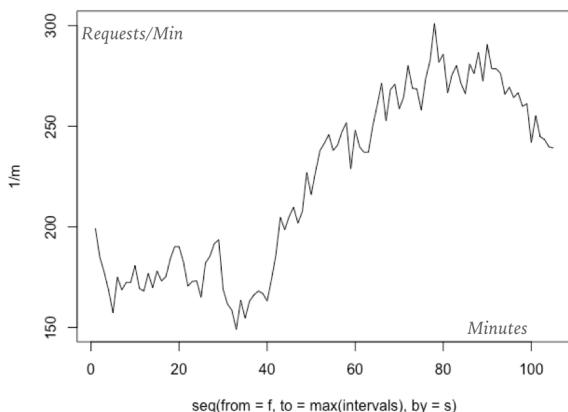
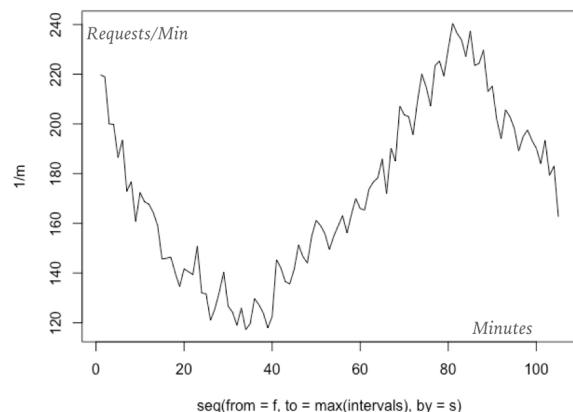
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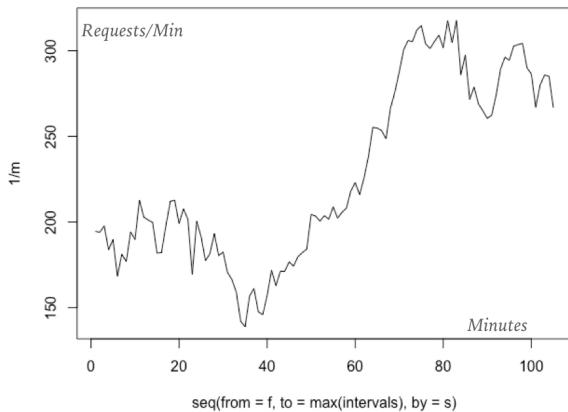
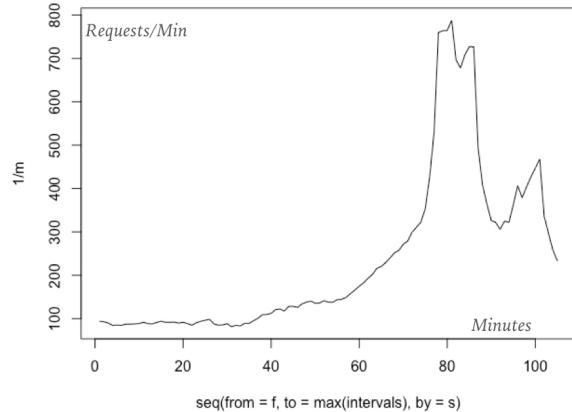
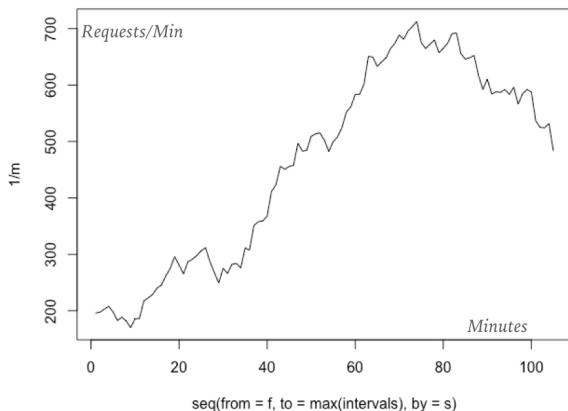
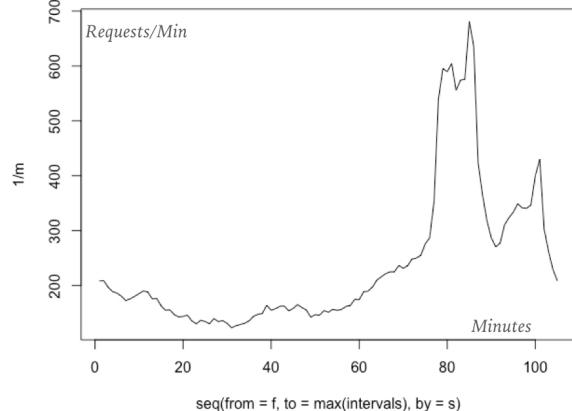
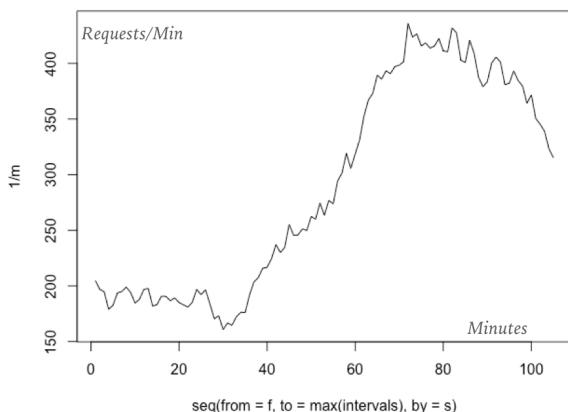
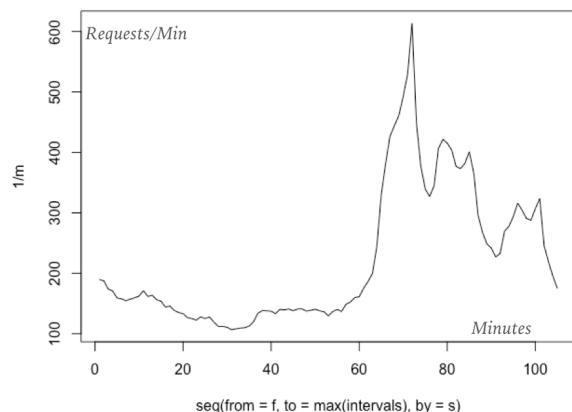
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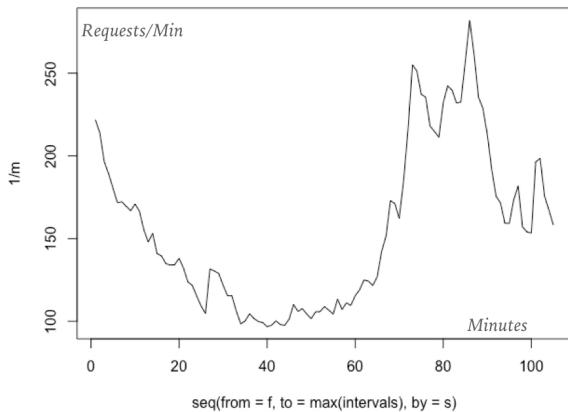
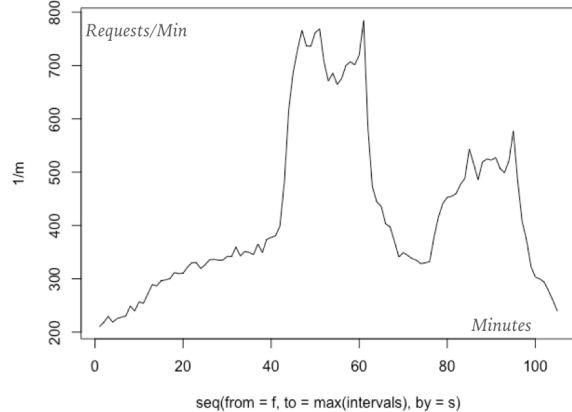
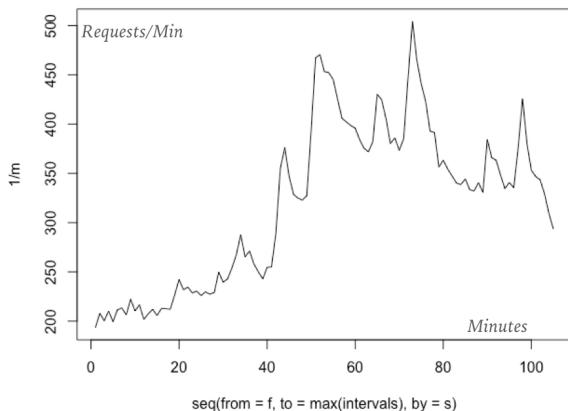
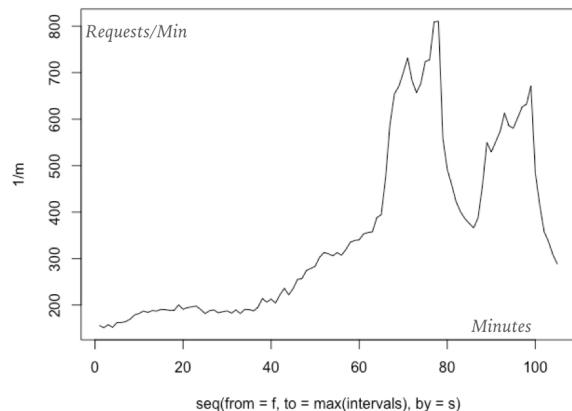
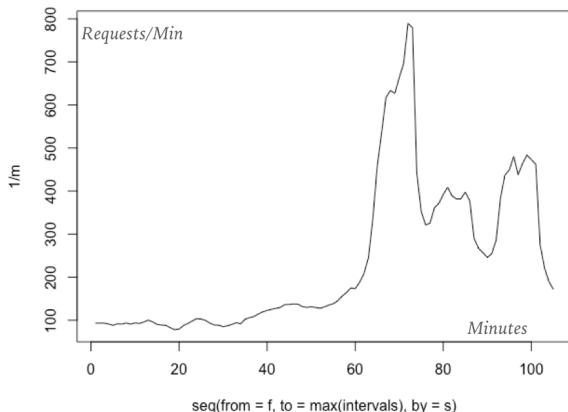
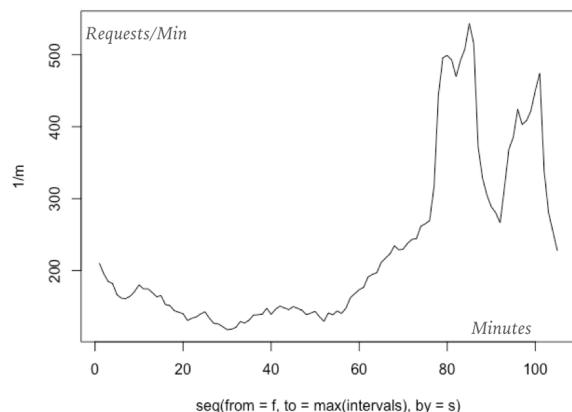
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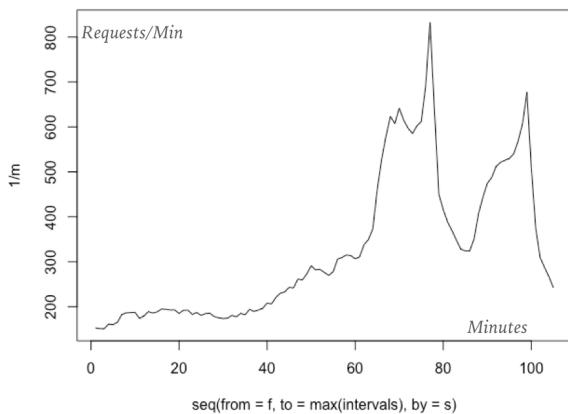
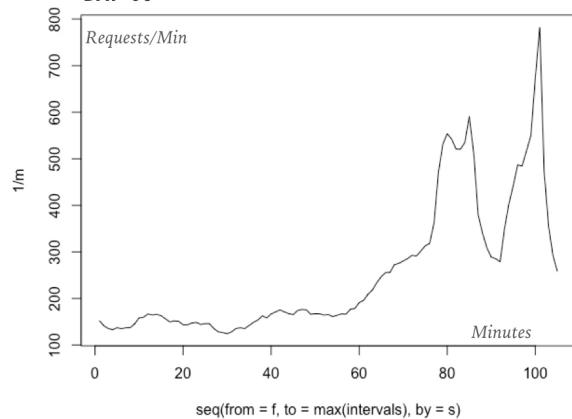
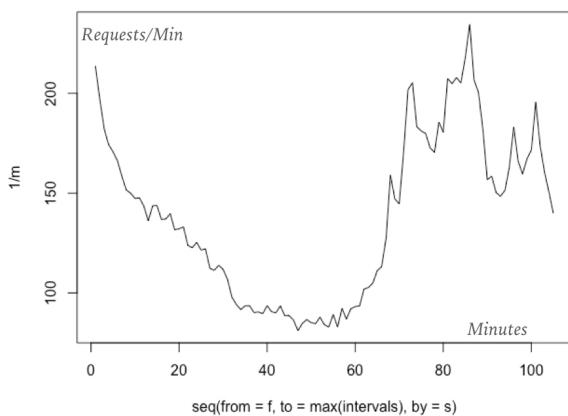
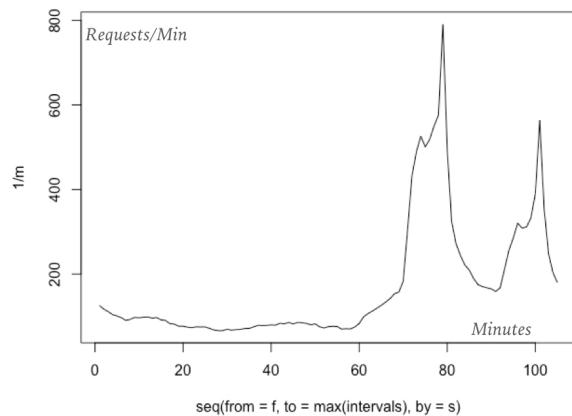
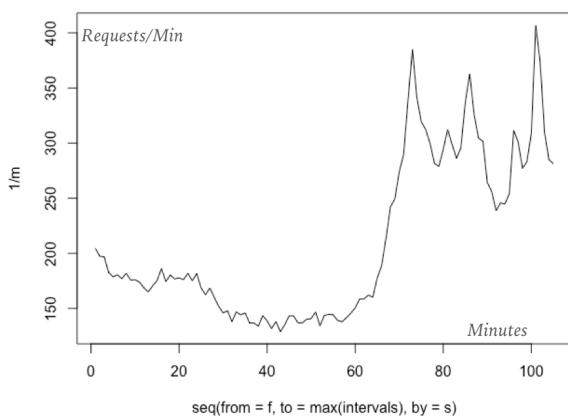
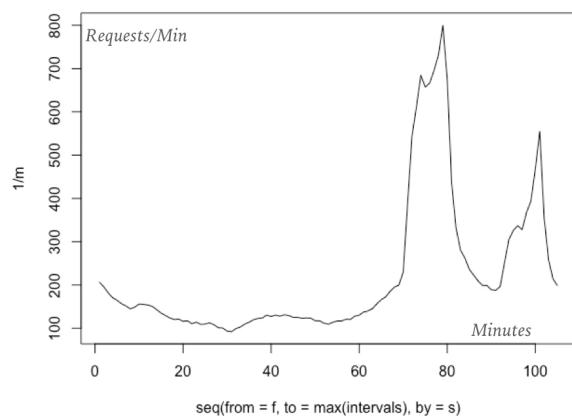
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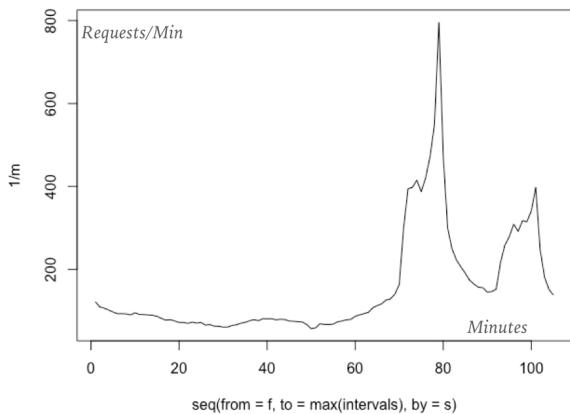
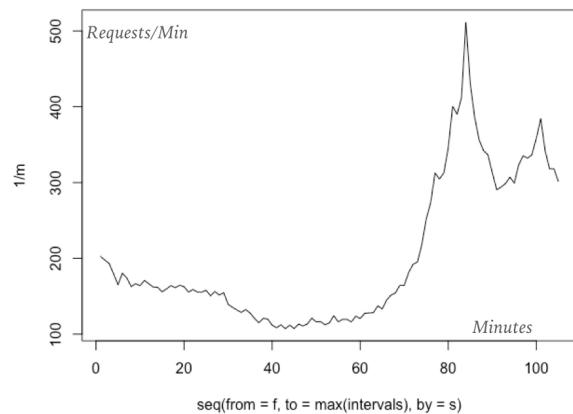
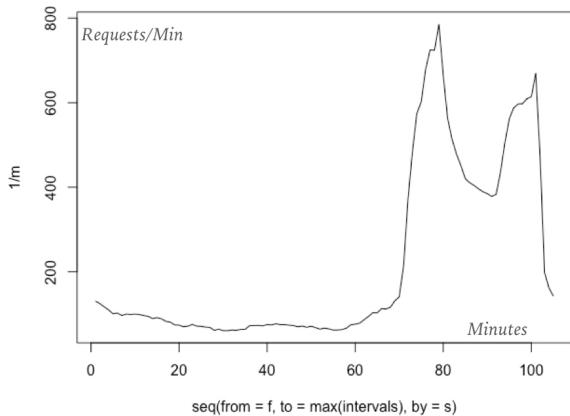
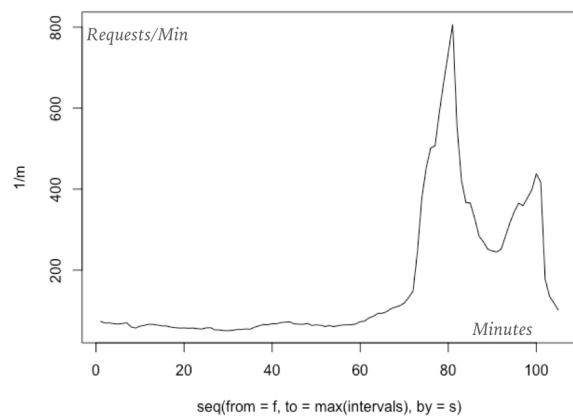
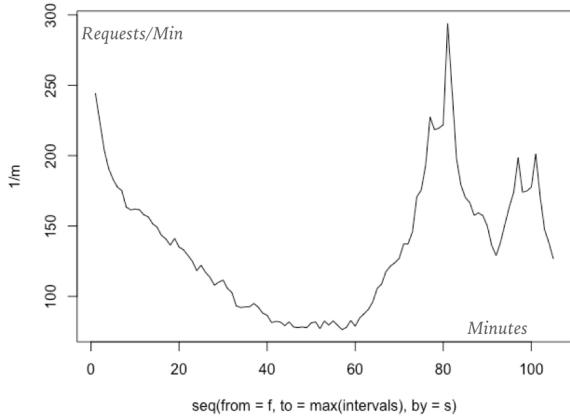
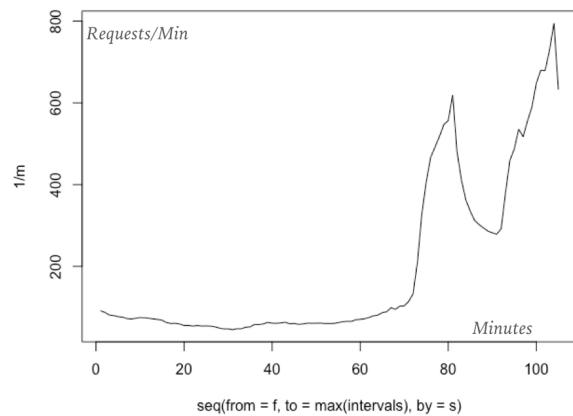
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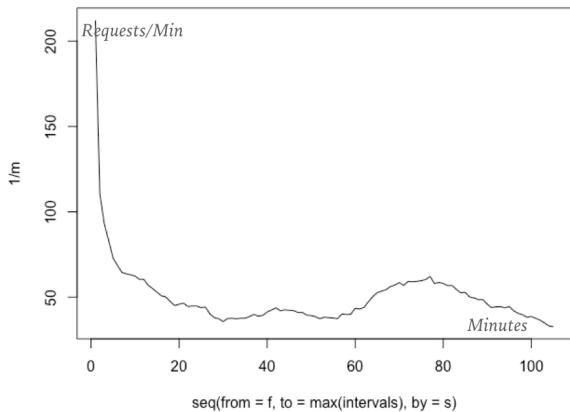
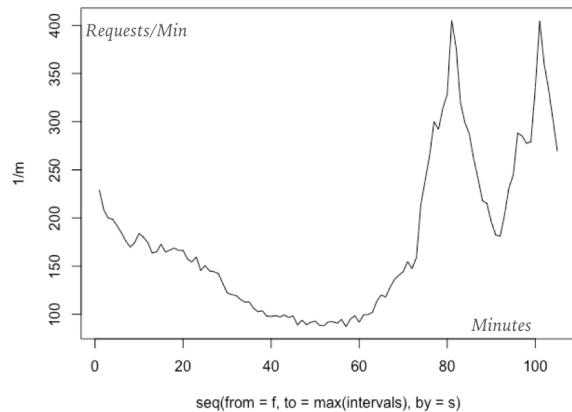
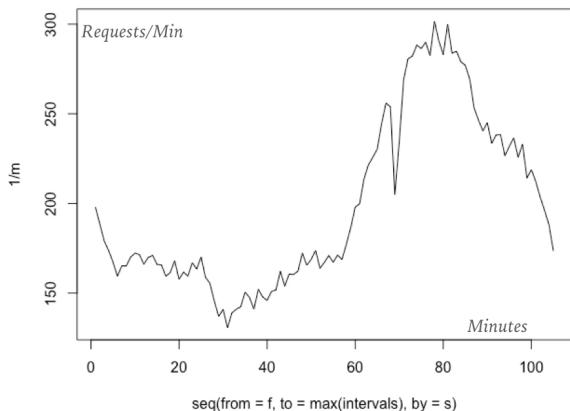
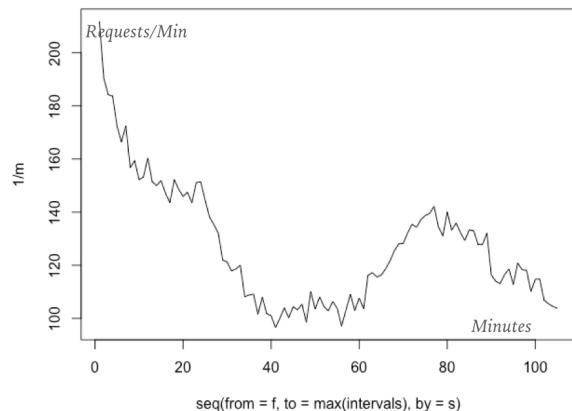
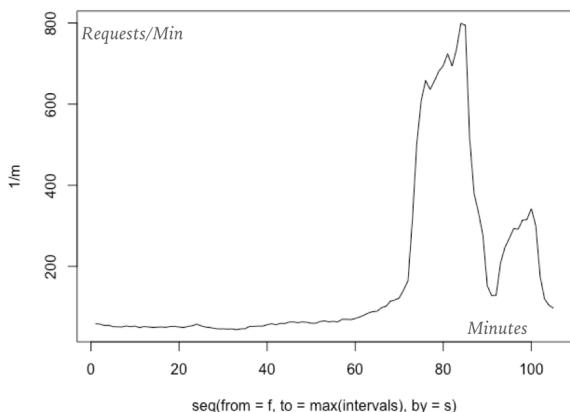
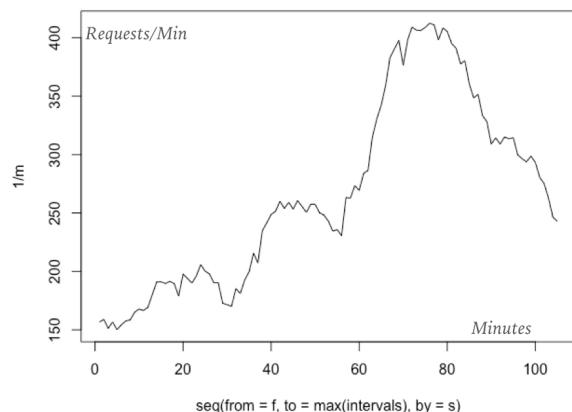
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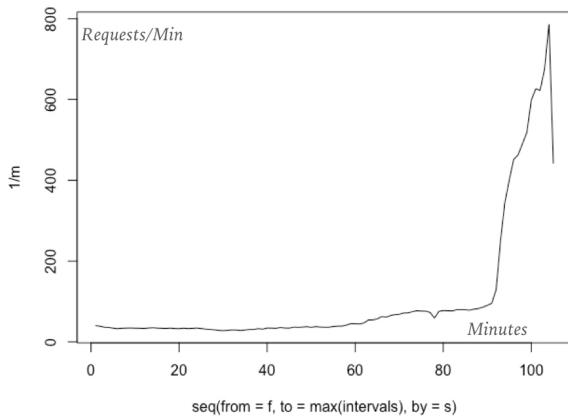
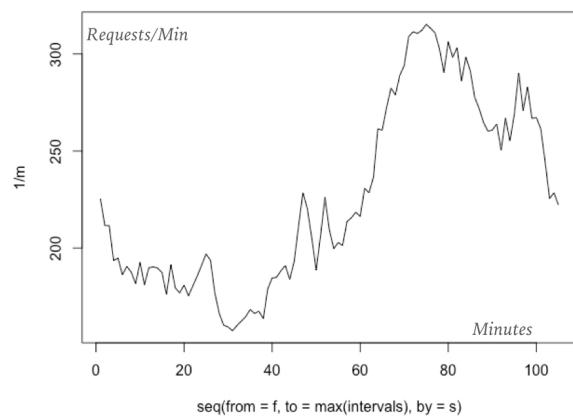
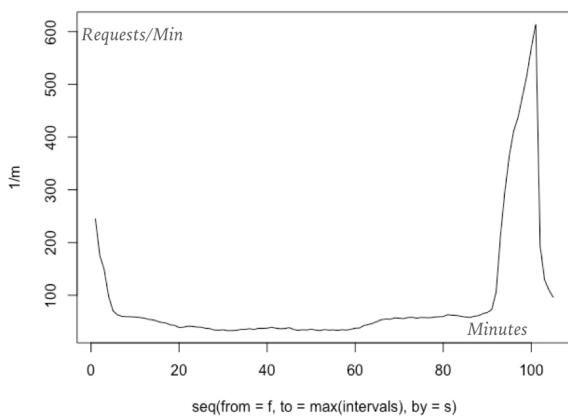
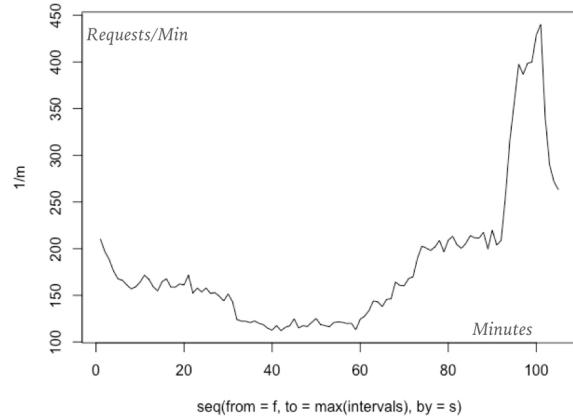
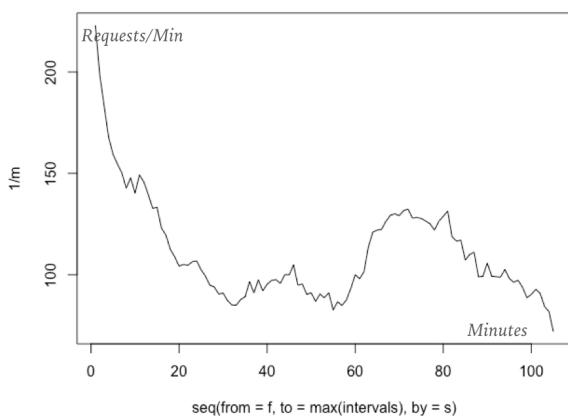
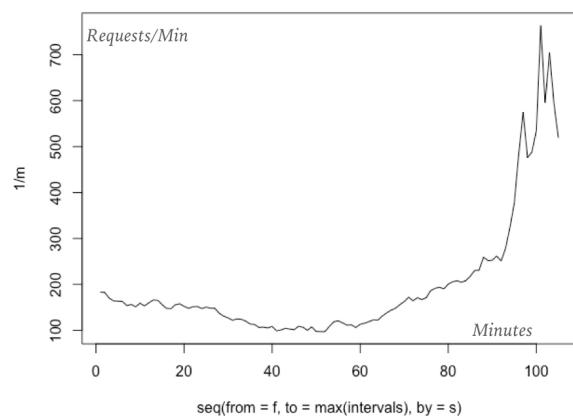
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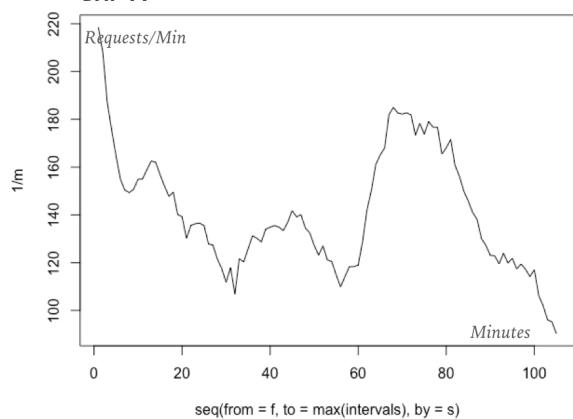
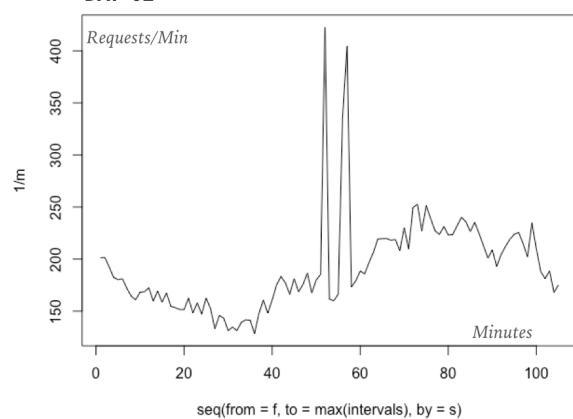
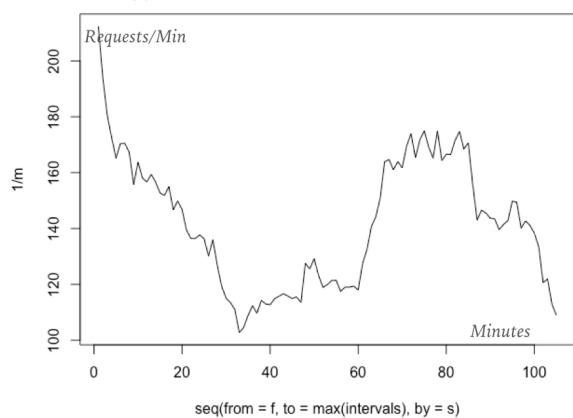
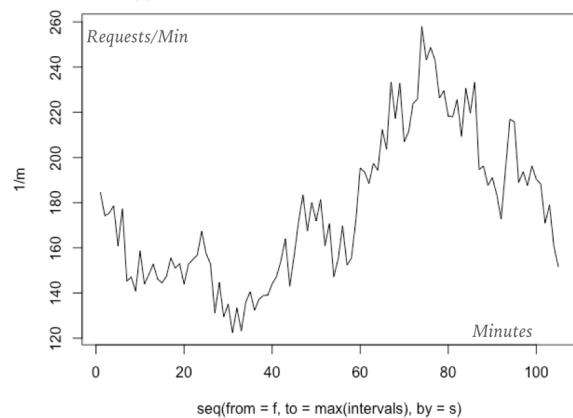
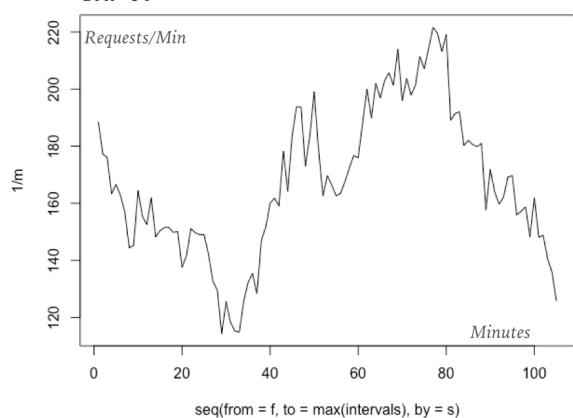
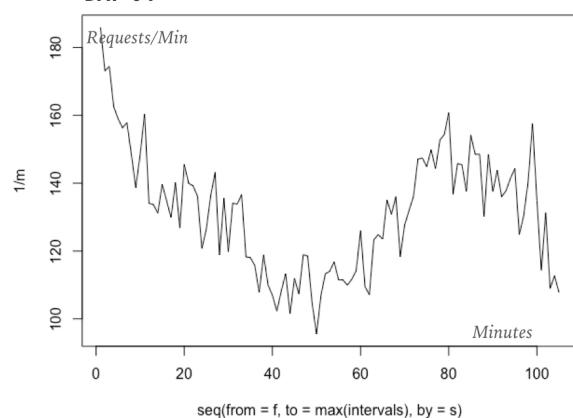
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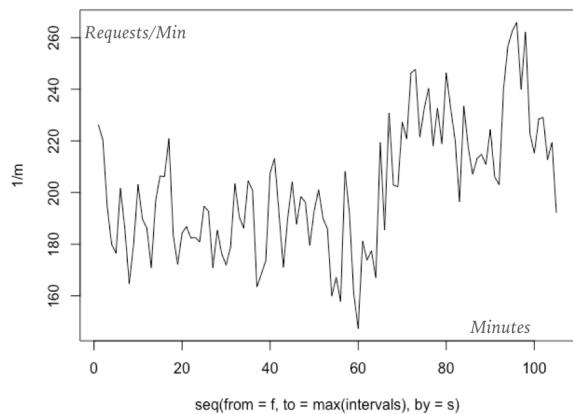
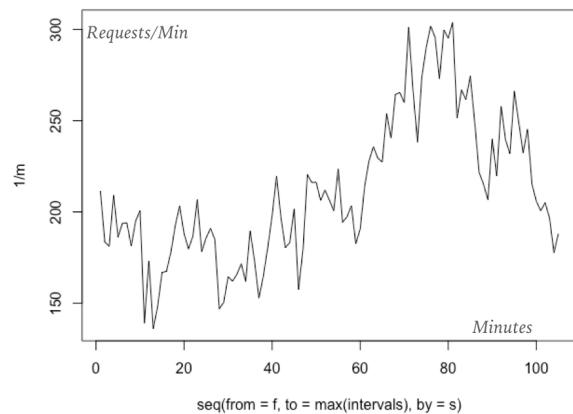
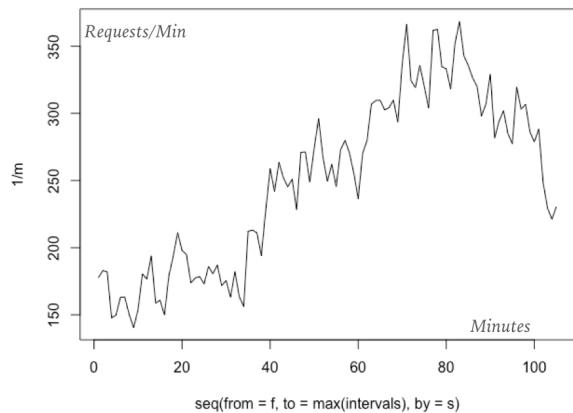
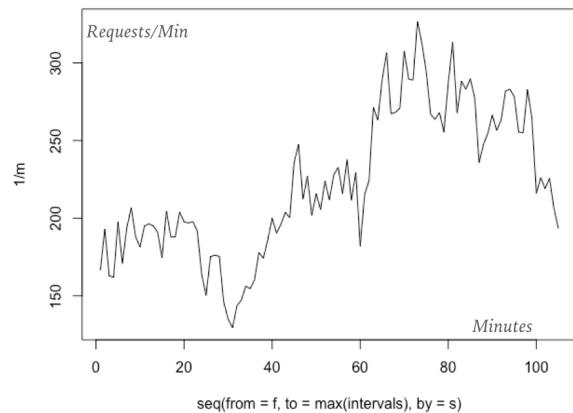
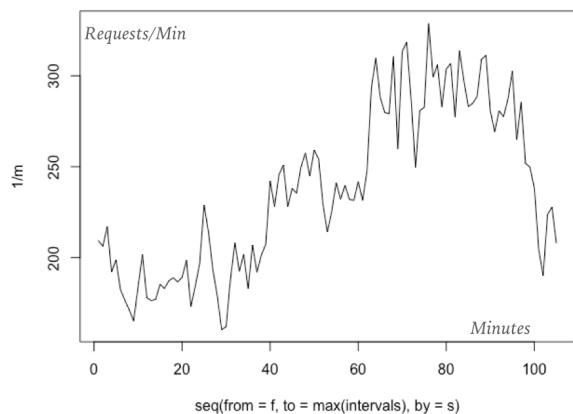
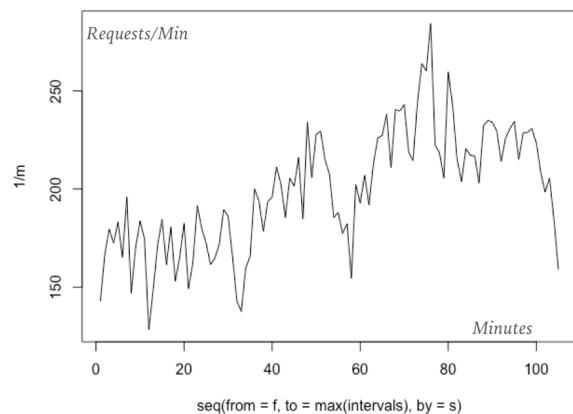
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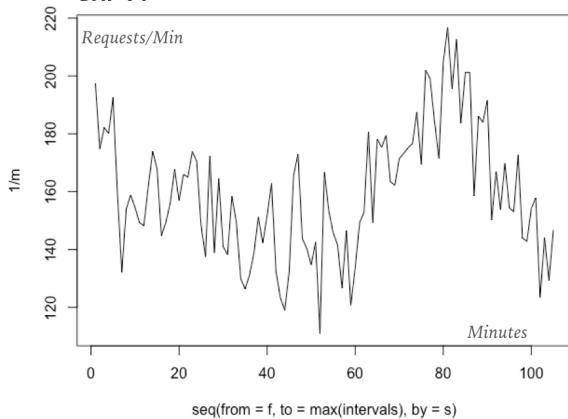
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**DAY-79****DAY-82****DAY-80****DAY-83****DAY-81****DAY-84**

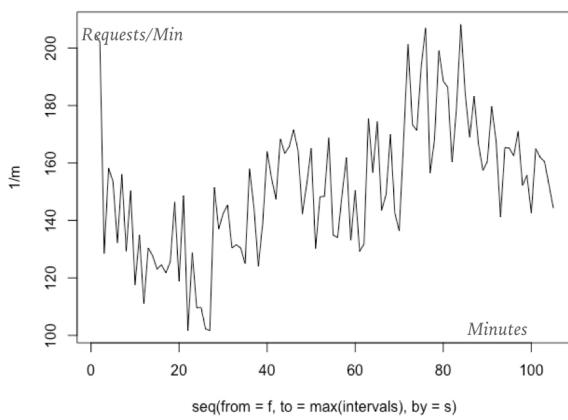
**DAY-85****DAY-88****DAY-86****DAY-89****DAY-87****DAY-90**

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**DAY-91**



**DAY-92**



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